# Observer design for state and clinker hardness estimation in cement mill

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#### 1. A short presentation about our lab



The « Centre de Recherche en Automatique de Nancy » (Automatic Control) is a Research Centre funded by the "Centre National de la Recherche Scientifique (CNRS)" and two universities in Nancy : UHP (Université Henri Poincaré) and INPL (Institut National Polytechnique de Lorraine). The CRAN was set up in Nancy (France) in 1980. It totals 180 persons. The research activities concentrate on 5 principal themes :

- Systems Observation and Control
- System Identification and Signal Processing
- Dependability and System Diagnosis
- Health Engineering
- Ambient Manufacturing Systems.



### 2. A short presentation of process diagnosis



#### 2. A short presentation of process diagnosis

For the elaboration of a global approach for the design and the operation (supervision, maintenance, reconfiguration) of complex automated industrial systems, it is necessary :

- to guarantee the system safety, i.e. to guarantee that the system will operate according to the given specifications
- to forecast alternate modes allowing the system to continue to operate even if some parts of it are out of order
- to detect any fault, i.e. to decide that the system does not operate normally, using the overall available information on the actual behavior (obtained through the measurements) and on the expected behavior (forecast by a system model)
- to isolate the faults, i.e. to decide which function (or, at least, which component) is faulty based on data redundancy
- to identify the faults, i.e. to estimate the magnitude of the fault and to estimate its time evolution
- to compensate for the faults, i.e. to implement a fault tolerant control (that leads eventually to a degraded system performance) or reconfigure either the control architecture or the process architecture itself.







## 3. System under investigation. Flowsheet



FIGURE: Cement mill process



Separator
$$T_f \dot{y}_f(t) = -y_f(t) + (1 - \alpha(v))\varphi(w(t), d(t))$$
Ball - mill $T_r \dot{y}_r(t) = -y_r(t) + \alpha(v)\varphi(w(t), d(t))$ Load $\dot{w}(t) = -\varphi(w(t), d(t)) + y_r(t) + u(t)$ 

where

$$\varphi(w(t), d(t)) = p_1 w(t) \exp(-p_2 d(t) w(t))$$
  
$$\alpha(v(t)) = p_3 v^3(t) + p_4 v^4(t) + p_5 v^5(t)$$

## 3. System under investigation. Mathematical model

Then, the system is described by the following state equations

$$\begin{cases} \dot{x}(t) = f(x(t), d(t)) + Bu(t) \\ y(t) = Cx(t) \end{cases}$$

where

$$\begin{aligned} x(t) &= \begin{bmatrix} y_f(t) \\ y_r(t) \\ w(t) \end{bmatrix} \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} \quad C = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \end{bmatrix} \\ f(x(t), d(t)) &= \begin{bmatrix} \frac{1}{T_f} \left( -x_1(t) + (1 - \alpha(v))\varphi(x_3(t), d(t)) \right) \\ \frac{1}{T_r} \left( -x_2(t) + \alpha(v)\varphi(x_3(t), d(t)) \right) \\ x_2(t) - \varphi(x_3(t), d(t)) \end{bmatrix} \end{bmatrix}$$

in which the hardness d(t) is unknown.

$$\begin{bmatrix} \dot{y}_f(t) \\ \dot{y}_r(t) \\ \dot{w}(t) \end{bmatrix} = \begin{bmatrix} -1/\mathcal{T}_f & 0 & 0 \\ 0 & -1/\mathcal{T}_r & 0 \\ 0 & 1 & 0 \end{bmatrix} \begin{bmatrix} y_f(t) \\ y_r(t) \\ w(t) \end{bmatrix} + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t) + \begin{bmatrix} (1-\alpha(v)) \\ \alpha(v)\varphi(x_3,d) \\ -\varphi(x_3,d) \end{bmatrix}$$

# 3. System under investigation. Objectives



- Estimate the hardness d(t)
- Difficulty : the system is non linear
- Proposed approach : multi-model representation of the system

#### 4. What is a multi-model? Definition

$$\mathcal{M}_{1} \qquad \mu(t) \qquad M_{2}$$

$$\mathcal{S} \begin{cases} M_{1} : \dot{y}(t) = a_{1}.y(t) + b_{1}.u(t), & \text{if } y(t) > 2.5 \\ M_{2} : \dot{y}(t) = a_{2}.y(t) + b_{2}.u(t), & \text{if } y(t) < 2.5 \end{cases}$$

$$\mathcal{S} \begin{cases} \dot{y}(t) = a(t).y(t) + b(t).u(t) \\ a(t) = \mu(t).a_{1} + (1 - \mu(t)).a_{2} \\ b(t) = \mu(t).b_{1} + (1 - \mu(t)).b_{2} \\ \mu(t) = \frac{1}{2}(1 + sign(y(t) - 2.5)) \end{cases} \qquad \mathcal{S} \begin{cases} \dot{y}(t) = \sum_{i=1}^{2} \mu_{i}(t)(a_{i}.y(t) + b_{i}.u(t)) \\ \mu_{1}(t) = \frac{1}{2}(1 + sign(y(t) - 2.5)) \\ \mu_{2}(t) = 1 - \mu_{1}(t) \end{cases}$$

Summarizing, a multi-model, or a multiple-model, is a weighting sum of local models. These local models are chosen linear in respect to the state and control variable

### 4. What is a multi-model? Definition

Two kinds of weighting functions

Switching



Smooth transition



$$\dot{x}(t) = \begin{bmatrix} -\frac{1}{T_f} & 0 & \frac{z_1(t)}{T_f} \\ 0 & -\frac{1}{T_r} & 0 \\ 0 & 1 & -\frac{z_1(t)}{T_f} \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t) + \begin{bmatrix} -\frac{z_2(t)}{T_f} \\ \frac{z_2(t)}{T_r} \\ 0 \end{bmatrix} d(t)$$

where the variables  $z_1(x(t), d(t))$  and  $z_2(t)$ , later selected as premise variables, are defined by

$$z_1(t) = p_1 \exp(-p_2 d(t) x_3(t))$$
  
$$z_2(t) = \alpha(v(t)) p_1 x_3(t) \frac{\exp(-p_2 d(t) x_3(t))}{d(t)}$$

$$egin{aligned} &z_1^{\min} \leq z_1(t) \leq z_1^{\max} \ &z_2^{\min} \leq z_2(t) \leq z_2^{\max} \end{aligned}$$

Since they are bounded, the premise variables can be written as a weighting sum of their bounds. For the first one :

$$z_{1}(t) = \mu_{1}^{0}(z_{1}(t))z_{1}^{\min} + \mu_{1}^{1}(z_{1}(t))z_{1}^{\max}$$
$$= \sum_{i=0}^{1} \mu_{1}^{i}(z_{1}(t))z_{1}^{i}$$

where the functions  $\mu_1^0$  and  $\mu_1^1$  are defined by

$$\mu_1^0(z_1(t)) = \frac{z_1^1 - z_1(t)}{z_1^1 - z_1^0}, \quad \mu_1^1(z_1(t)) = \frac{z_1(t) - z_1^0}{z_1^1 - z_1^0}$$

and satisfy the following property :

$$egin{aligned} 0 &\leq \mu_1^0(z_i(t)) \leq 1 \ 0 &\leq \mu_1^1(z_i(t)) \leq 1 \ \mu_1^0(z_i(t)) + \mu_1^1(z_i(t)) = 1 \end{aligned}$$

4. How to transform a non-linear model into a multi-model?

$$\begin{split} \dot{x}(t) &= \begin{bmatrix} -\frac{1}{T_{f}} & 0 & \frac{z_{1}(t)}{T_{f}} \\ 0 & -\frac{1}{T_{r}} & 0 \\ 0 & 1 & -\frac{z_{1}(t)}{T_{f}} \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t) + \begin{bmatrix} -\frac{z_{2}(t)}{T_{f}} \\ \frac{z_{2}(t)}{T_{r}} \\ 0 \end{bmatrix} d(t) \quad z_{1}(t) = \sum_{i=0}^{1} \mu_{1}^{i}(z_{1}(t)) \\ \dot{x}(t) &= \begin{bmatrix} -\frac{1}{T_{f}} & 0 & \frac{\sum_{i=0}^{1} \mu_{1}^{i}(z_{1}(t))z_{1}^{i}}{T_{f}} \\ 0 & -\frac{1}{T_{r}} & 0 \\ 0 & 1 & -\frac{\sum_{i=0}^{1} \mu_{1}^{i}(z_{1}(t))z_{1}^{i}}{T_{f}} \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t) + \begin{bmatrix} -\frac{z_{2}(t)}{T_{f}} \\ \frac{z_{2}(t)}{T_{r}} \\ 0 \end{bmatrix} d(t) \\ \dot{x}(t) &= \sum_{i=0}^{1} \mu_{1}^{i}(z_{1}(t)) \begin{pmatrix} \begin{bmatrix} -\frac{1}{T_{f}} & 0 & \frac{z_{1}^{i}}{T_{f}} \\ 0 & -\frac{1}{T_{r}} & 0 \\ 0 & 1 & -\frac{z_{1}^{i}}{T_{f}} \end{bmatrix} x(t) + \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix} u(t) + \begin{bmatrix} -\frac{z_{2}(t)}{T_{f}} \\ \frac{z_{2}(t)}{T_{f}} \\ \frac{z_{2}(t)}{T_{r}} \\ 0 \end{bmatrix} d(t) \end{split}$$

The same transformation is made for the variable  $z_2(t)$ .

$$\begin{aligned} \dot{x}(t) &= \sum_{i=1}^{4} \mu_i(z(t)) \left( A_i x(t) + Bu(t) + E_i d(t) \right) & 0 \le \mu_i \le 1, \quad \sum \mu_i = 1 \\ A_1 &= \begin{bmatrix} -\frac{1}{T_f} & 0 & -\frac{z_1^1}{T_f} \\ 0 & -\frac{1}{T_r} & 0 \\ 0 & 1 & -z_1^1 \end{bmatrix}, \quad A_3 &= \begin{bmatrix} -\frac{1}{T_f} & 0 & -\frac{z_1^0}{T_f} \\ 0 & -\frac{1}{T_r} & 0 \\ 0 & 1 & -z_1^0 \end{bmatrix}, \\ E_1 &= \begin{bmatrix} -\frac{z_2^1}{T_f} \\ \frac{z_2^1}{T_f} \\ 0 \end{bmatrix}, \quad E_2 &= \begin{bmatrix} -\frac{z_2^0}{T_f} \\ \frac{z_2^0}{T_r} \\ 0 \end{bmatrix}, \quad B = \begin{bmatrix} 0 \\ 0 \\ 1 \end{bmatrix}, \quad A_2 = A_1, \quad A_4 = A_3, \quad E_3 = E_1, \quad E_4 = E_2 \end{aligned}$$

Advantage of this formulation :

- a systematic representation into a weighting sum of simple local models
- the possibility use results established for linear systems (stability, observer, control)

#### Model of the observer

$$\begin{cases} \dot{\hat{x}}(t) &= \sum_{i=1}^{4} \mu_i(\hat{z}(t))(A_i \times (t) + Bu(t) + E_i \hat{d}(t) + L_i(y(t) - \hat{y}(t))) \\ \dot{\hat{d}}(t) &= \sum_{i=1}^{4} \mu_i(\hat{z}(t)) K_i(y(t) - \hat{y}(t)) \\ \hat{y}(t) &= C \hat{x}(t) \end{cases}$$

$$\begin{aligned} f' x_{a}(t) &= [x^{T}(t) \ d^{T}(t)]^{T} \\ e_{a}(t) &= x_{a}(t) - \hat{x}_{a}(t) \\ \dot{e}_{a}(t) &= \sum_{i=1}^{4} \mu_{i}(\hat{z}(t))(\mathscr{A}_{i} - \mathscr{M}_{i}\mathscr{C})e_{a}(t) + \Delta(t) \end{aligned}$$

where

$$\begin{aligned} \mathscr{A}_{i} &= \begin{pmatrix} A_{i} & E_{i} \\ 0 & 0 \end{pmatrix}, \quad \mathscr{M}_{i} &= \begin{pmatrix} L_{i} \\ K_{i} \end{pmatrix}, \quad \mathscr{C} &= \begin{pmatrix} C & 0 \end{pmatrix}, \\ \Delta(t) &= \sum_{i=1}^{4} (\mu_{i}(z(t)) - \mu_{i}(\hat{z}(t))) \mathscr{A}_{i} \times_{a}(t) \end{aligned}$$

 $\triangleright$  Design of the observer : adjust  $E_i$ ,  $L_i$  and  $K_i$  such that  $e_a$  is bounded.



Finished product rate  $y_f(tons/h)$ 

 $\ensuremath{\operatorname{Figure:}}$  System states and their estimates



 $\ensuremath{\mathsf{Figures}}$  : State estimation errors (top) and clinker hardness and its estimate with noised measurements



FIGURE: Cement mill process

Process equation

$$\begin{cases} T_f \dot{q}_f(t) &= -q_f(t) + (1 - \alpha(v)) \cdot q_b(t) \\ T_r \dot{q}_r(t) &= -q_r(t) + \alpha(v) \cdot q_b(t) \\ \dot{w}(t) &= -\varphi(t) + q_r(t) + u(t) \\ q_b(t) &= p_1 \cdot w(t) \cdot \exp(-p_2 \cdot d \cdot w(t)) \\ \frac{d(g_{b,i}(t))}{dt} &= \frac{1}{w(t)} \left( q_u(t)(g_{u,i}(t) - g_{b,i}(t)) + q_r(t)(g_{r,i}(t) - g_{b,i}(t)) \right) \\ -s_i g_{b,i}(t) + \sum_{j=i}^N g_{b,j}(t) s_j b_{ij}, \quad i = 1, \dots, N \end{cases}$$

Control loop equation

$$\begin{cases} u(t) = -q_r(t) + k_1(w^*(t) - w(t)) \\ v(t) = k_2(q_f(t) - q_f^*(t)) \end{cases}$$

 $\triangleright$  The goal of this paper is to design an observer for mill load and clinker hardness estimation in cement mill process with only the knowledge of the feeding *u*, the tailings *y<sub>r</sub>* and the finished product rate *y<sub>f</sub>*.

▷ Work is underway to extend the proposed state reconstruction when one takes into account, in addition to flow rates, the whole particle size distributions of the product throughout the separation-grinding loop.

#### Ladies and Gentleman, thank you very much for your attention !

