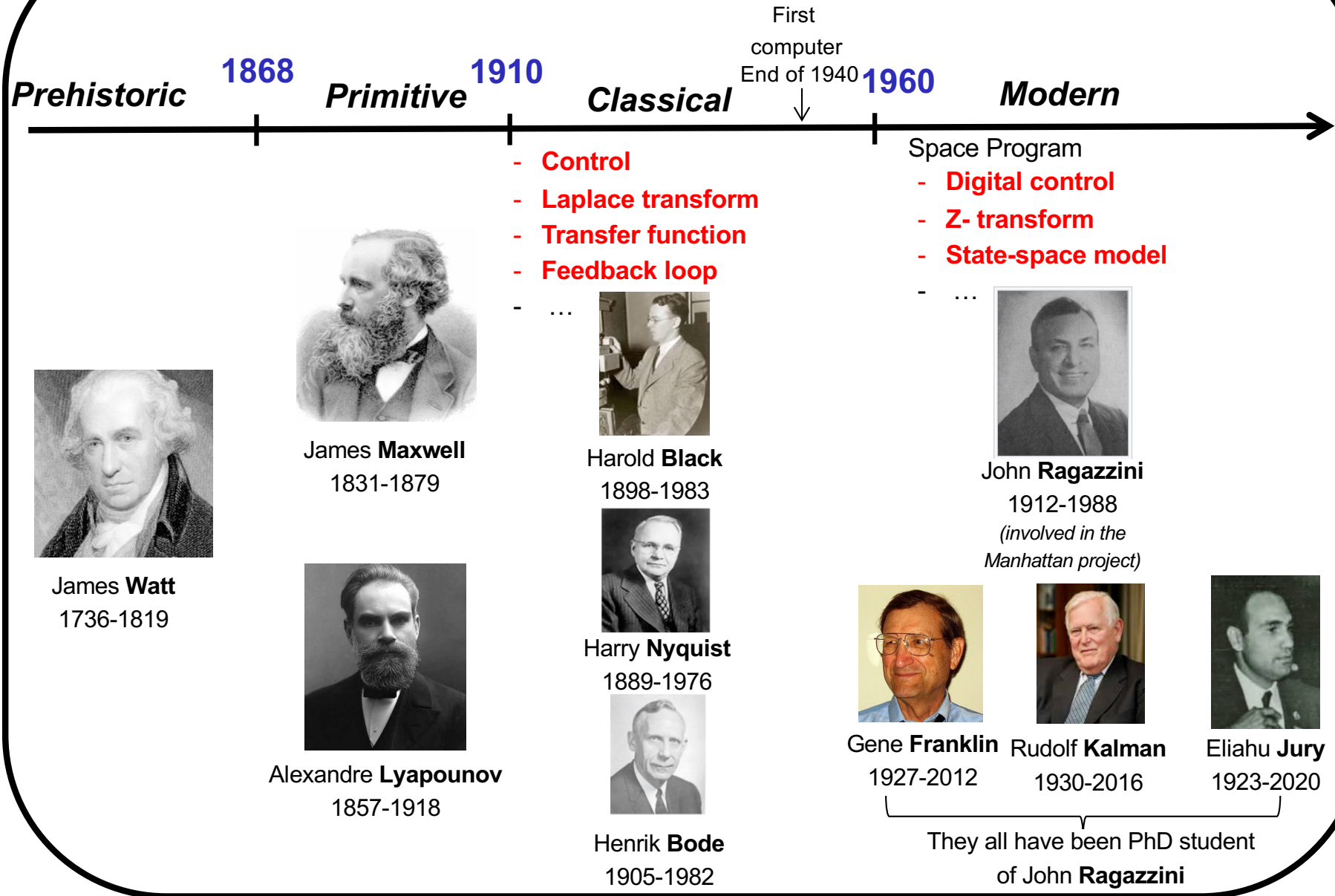
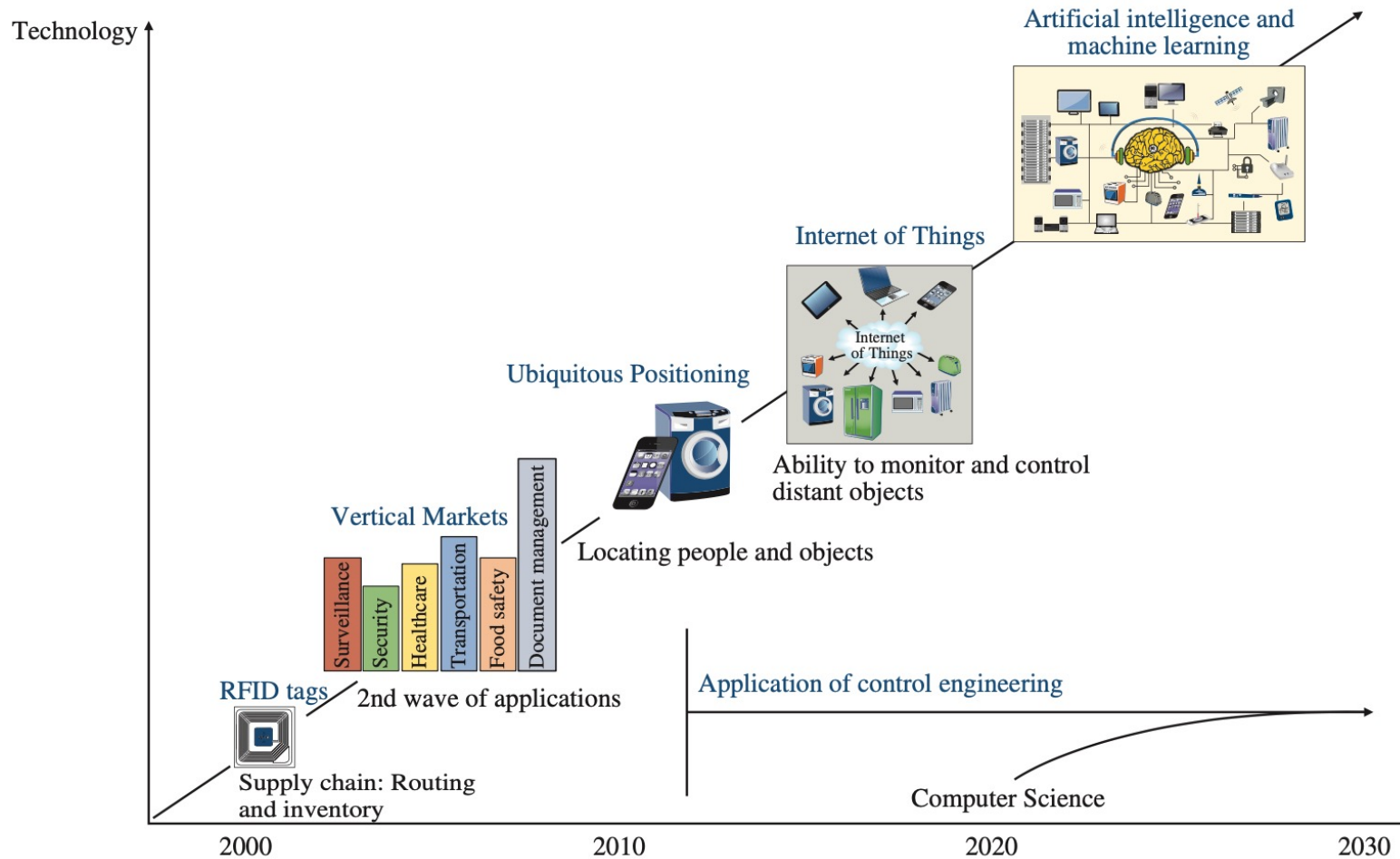


Timeline in Automatic Control



Technology roadmap to the IoT enhanced with IA with applications to control engineering (Source: SRI Business Intelligence)



Two separate parts for a total of 36 hours

- **Digital control**

- 6h of lecture
- 8 h of tutorials
- 4h of Labs

- **State-space control**

- 5h of lecture
- 6h of tutorials
- 4h of Labs

Course materials in English

- Lectures
 - Hugues Garnier
- Tutorials/Labs
 - Hugues Garnier
 - Floriane Collin

- Lectures/tutorials
 - Gilles Millérioux
- Labs
 - Hugues Garnier
 - Floriane Collin

Examination

- Exam 1 (2h00) – *Digital control*
 - In March
- Exam 2 (1h00) – *State-space model & control*
 - June 12, 16h30-17h30
- 1 Homework (HW)
 - In pairs
- 1 Lab report
 - In pairs
- Calculation of the final grade for the course

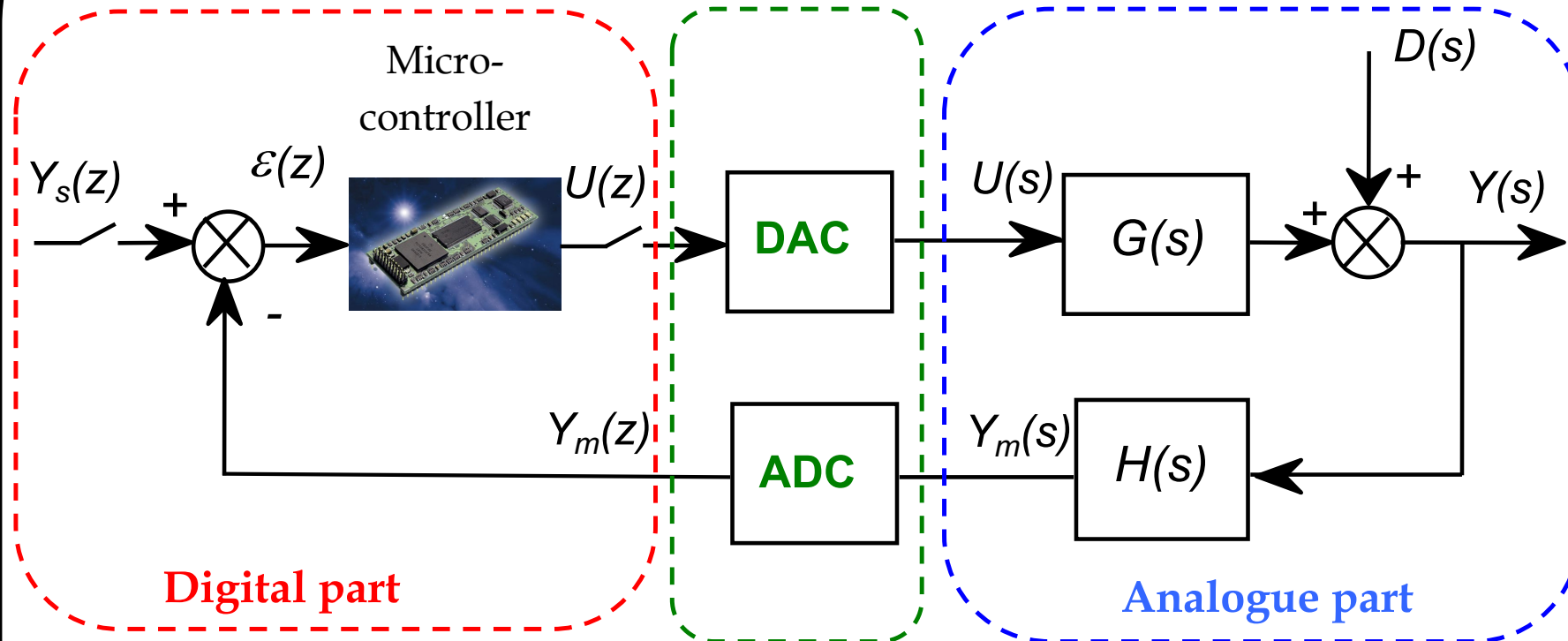
$$\text{Final grade} = 0,1 \text{ HW} + 0,4 \text{ Exam 1} + 0.25 \text{ Lab report} + 0.25 \text{ Exam 2}$$



Rule for the lectures

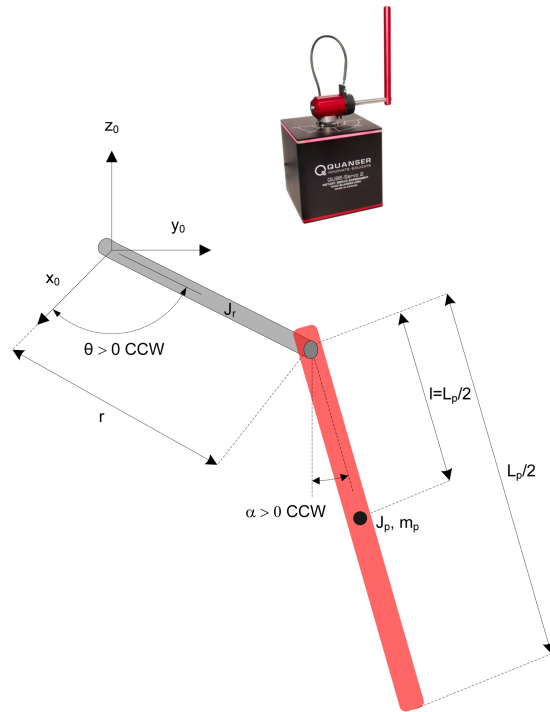
- It is forbidden to use your PC, tablet or cell phone during the course

First part of the course: digital control more appropriate to the current controller implementation



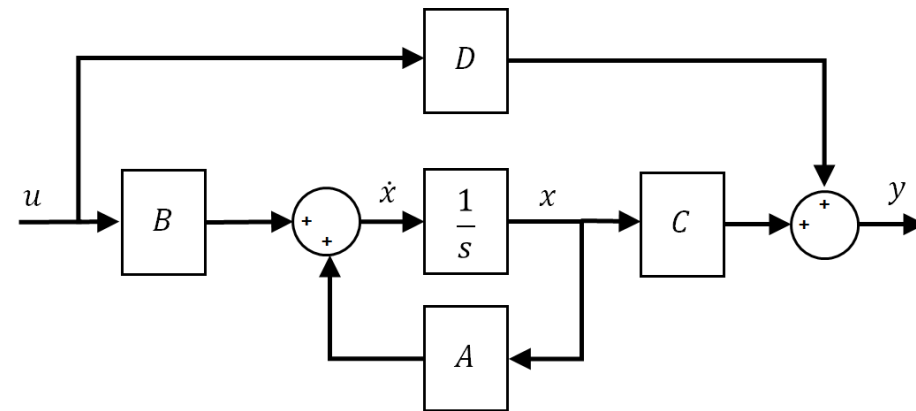
- Need for blocks to enable analogue and digital parts to interact : Digital to Analogue Converter (**DAC**) and **ADC**
- New mathematical tool to ease the analysis: the Z-transform
- PID controllers implemented digitally: discretization methods

Second part: State-space models and control more appropriate for the control of complex systems



$$\ddot{\theta} = \frac{1}{J_t} (m_p^2 l^2 r g \alpha - J_p b_r \dot{\theta} + m_p l r b_p \dot{\alpha} + J_p \tau)$$

$$\ddot{\alpha} = \frac{1}{J_t} (-m_p g l J_r \alpha + m_p l r b_r \dot{\theta} - J_p b_p \dot{\alpha} - m_p r l \tau)$$

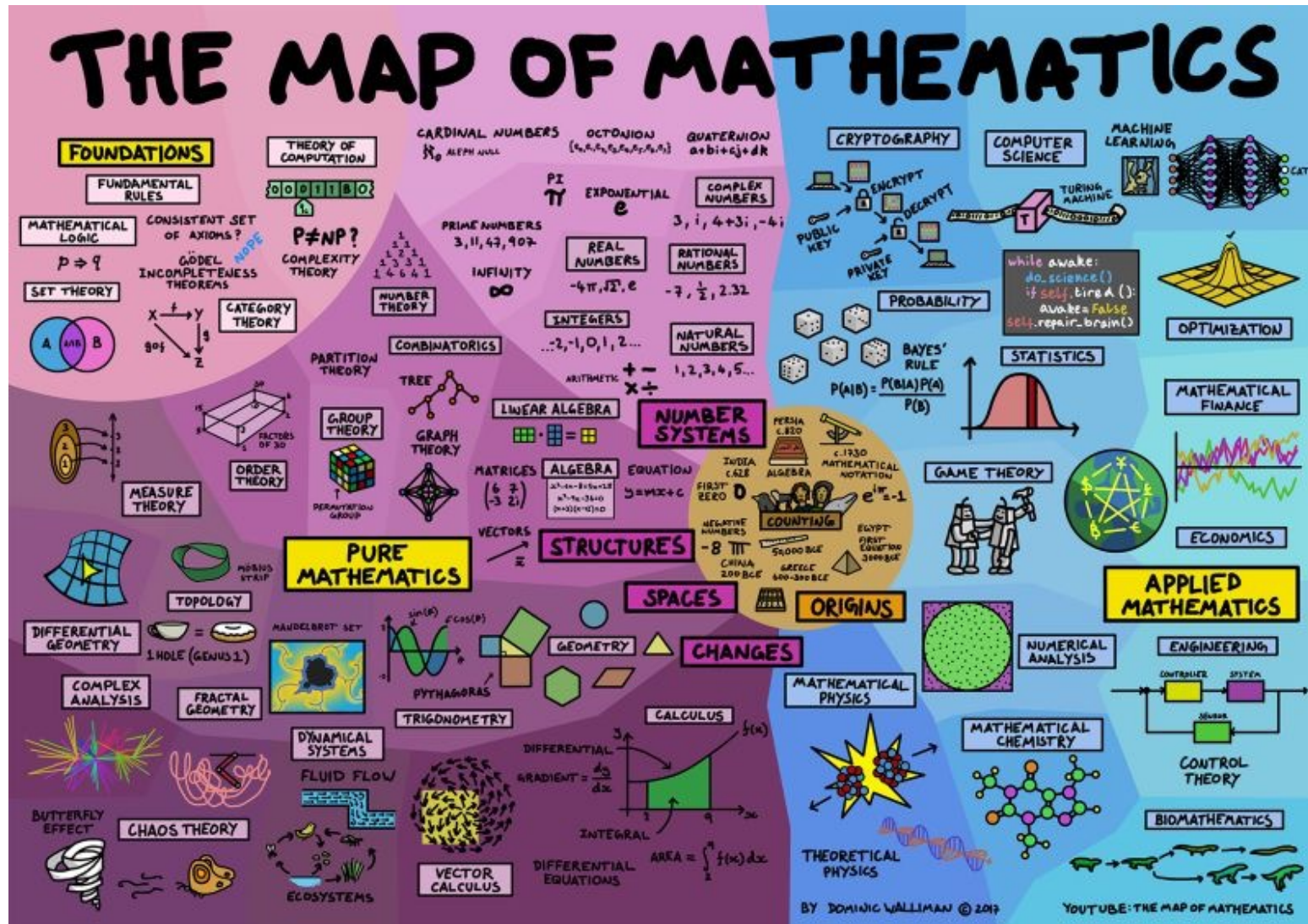


$$\begin{cases} \dot{x}(t) = Ax(t) + Bu(t) \\ y(t) = Cx(t) + Du(t) \end{cases}$$

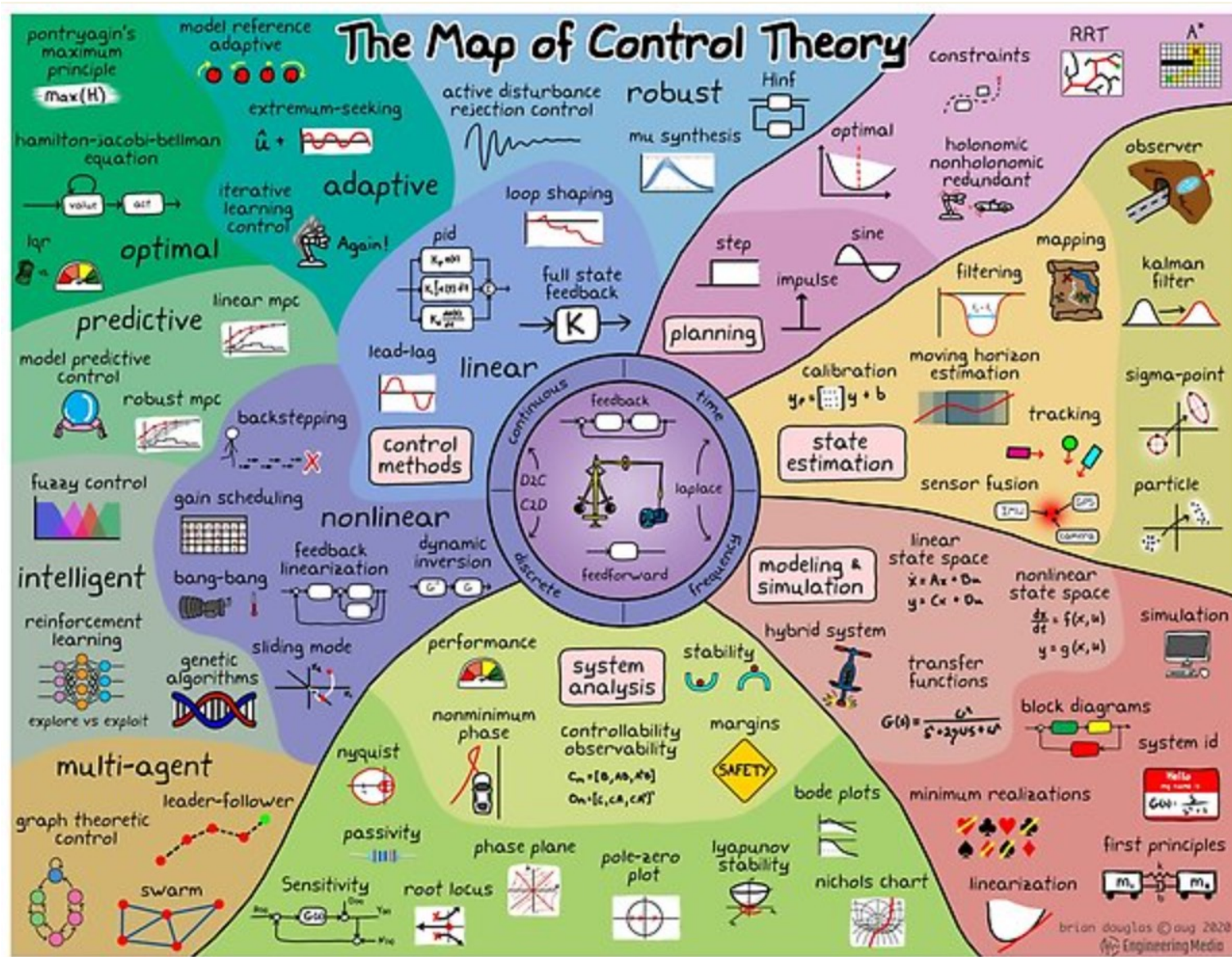
The state vector $x = [\theta \quad \alpha \quad \dot{\theta} \quad \dot{\alpha}]^T$

The two outputs
to be controlled $y = [\theta \quad \alpha]^T$

Where is *Charlie* ? euh... Where is *Control theory*?




From Brian Douglas



Website for the course

- w3.cran.univ-lorraine.fr/hugues.garnier/?q=content/teaching

Q



Hugues Garnier

Navigation

[Add content](#)

[Add file](#)

3 3 2 3 2

Teaching

Basic page *Teaching* has been updated. X

[View](#) [Edit](#)

Teaching activities

Since 2018, I have been head of the 3-year engineering programme (see [pdf](#)) in *Computer Science, Control Engineering, Robotics, IT Networks (IA2R)* at [Polytech Nancy](#).

where I teach the following courses:

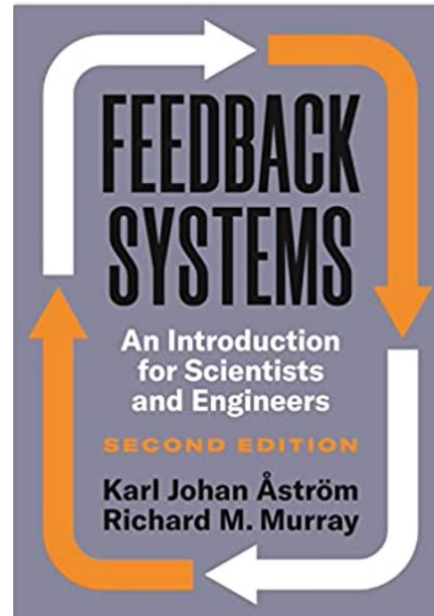
Digital control S6 (3A IA2R FISE)

- Slides for the course
 - [Digital control - Intro](#)
 - [The z-transform](#)
 - [Table of z-transforms](#)
 - Converters & Holds
 - Sampled data systems
 - Discrete-time systems
 - Synthesis of digital controllers
 - Digital PID controllers
- [Tutorials](#)
- Labs
 - Files for Lab 1
 - Files for Lab 2
- Exams

Recommended books

Feedback Systems

An Introduction for Scientists and Engineers, *K.J. Åström & R. Murray 2021*



➔ pdf version of the book available




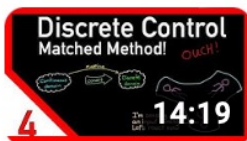
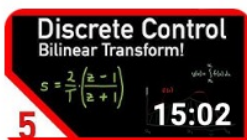

www.cds.caltech.edu/~murray/books/AM08/pdf/fbs-public_24Jul2020.pdf

See also

- K.J. Åström, B. Wittenmark, *Computer-controlled systems: theory and design* (3rd Ed.), Dover Publications, 2011

Videos available on Youtube

Discrete control by *Brian Douglas*

1		Discrete control #1: Introduction and overview Brian Douglas
2		Discrete control #2: Discretize! Going from continuous to Brian Douglas
3		Discrete control #3: Designing for the zero-order hold Brian Douglas
4		Discrete control #4: Discretize with the matched method Brian Douglas
5		Discrete control #5: The bilinear transform Brian Douglas
6		Discrete control #6: z-plane warping and the bilinear

Some other resommended videos on Youtube

Digital control by *Peter Corke*

ENB448/ENN580 part2:: Digital Control


Introduction & motivation

Peter Corke

Digital Control ×


Peter Corke - 1/5

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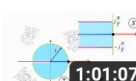
58:20

ENB458 lecture 1: Introduction to digital control

Peter Corke
- 


58:35

ENB458 lecture 2: Laplace transform to difference equation

Peter Corke
- 


1:01:07

ENB458 lecture 3: Welcome to the z-plane

Peter Corke
- 

1:08:43

ENB458: sampling time, aliasing and discrete-time state-space...

Peter Corke
- 

53:50

ENB458 lecture 5: creating a digital controller

Peter Corke

Youtube videos recommended for the course on State-space models and control

Matlab Tech Talks with *Brian Douglas* *State Space Models*

YouTube FR

Rechercher

State Space

MATLAB - 1/4

1 INTRODUCTION TO STATE SPACE EQUATIONS! 14:12 MATLAB

2 POLE PLACEMENT Understanding 14:55 MATLAB

3 Understanding CONTROLLABILITY & OBSERVABILITY 13:30 MATLAB

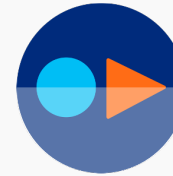
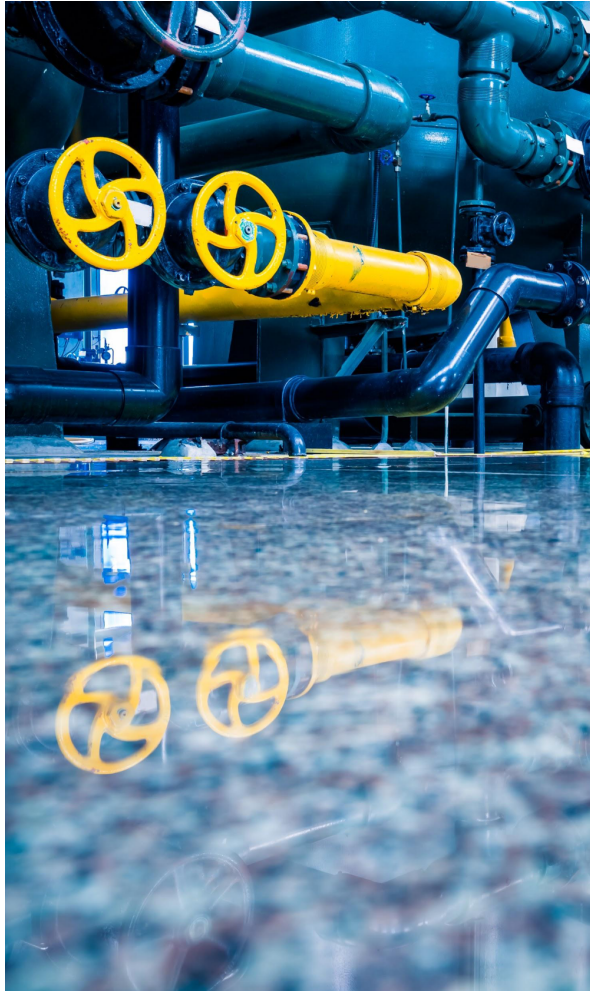
4 OPTIMAL CONTROL LQR! 17:24 MATLAB

Tout De la série Équations Leçons

Introduction to State-Space Equations | State Space, Part 1

Others resources in automatic control

Mobile textbook available from *Quanser*



Experience Controls by Quanser

Experience Controls is a free mobile textbook designed to give you real design intuition and relevant skills in a hands-on way in the control systems engineering space.

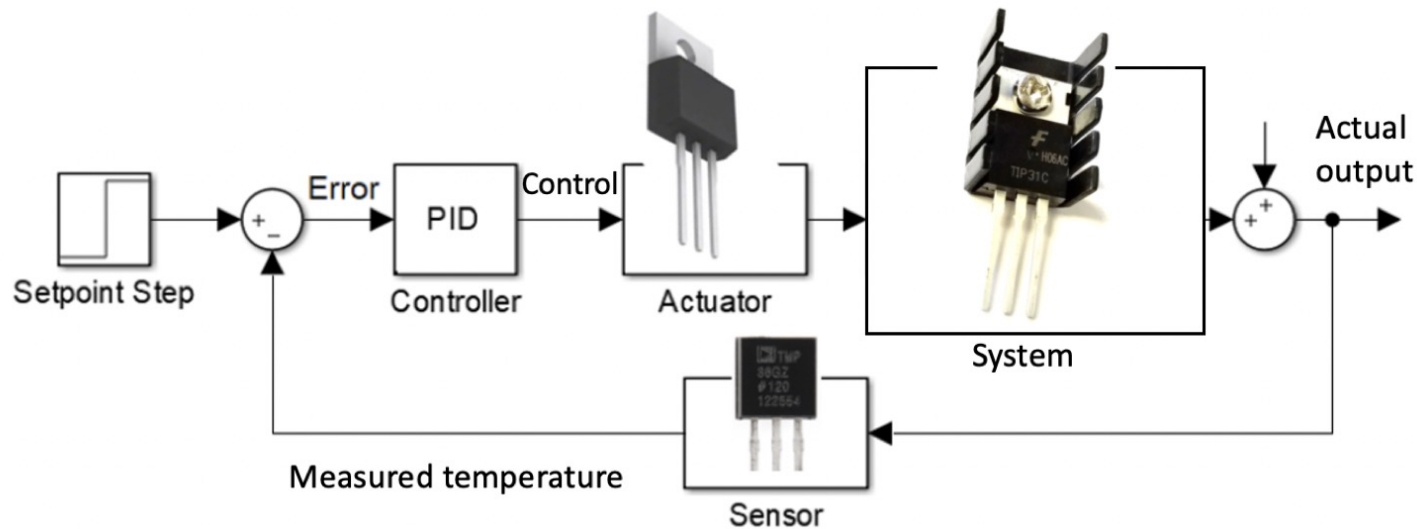
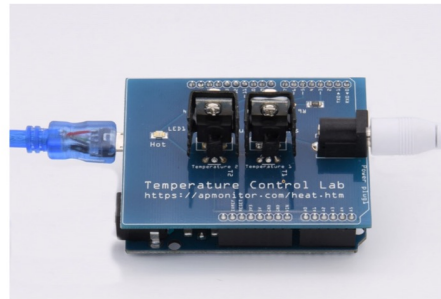
The textbook app includes:

- 50+ lesson modules covering introductory to advanced concepts
- Interactive simulations of industrial-level controls problems
- Mini-lecture podcasts that summarize key takeaways for each chapter, available in-app or in your preferred podcast player
- End-of-chapter review questions to check your understanding



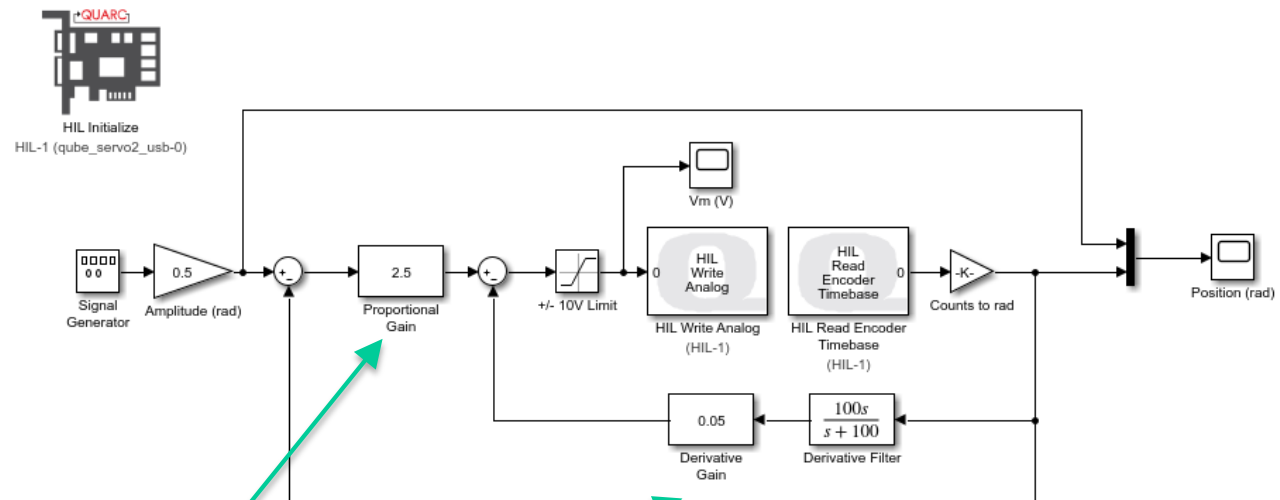
Reminder - Control Lab 1 S5

On-off and PID temperature control of the TCLab kit



Reminder - Control Lab 1 S5

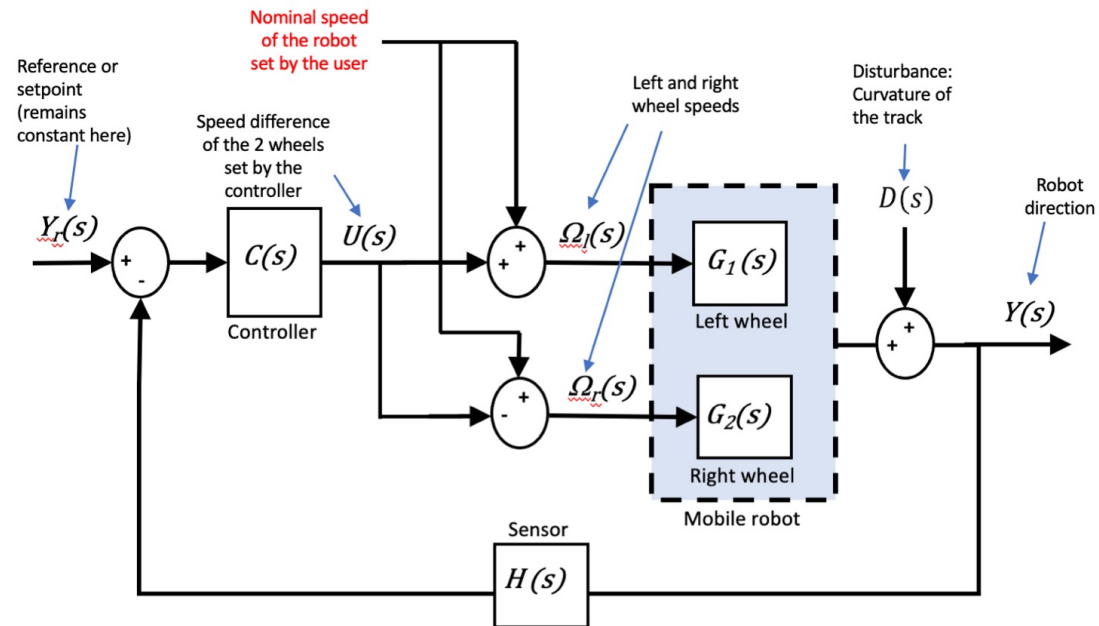
PID control of the angular position for the QUBE-servo 2



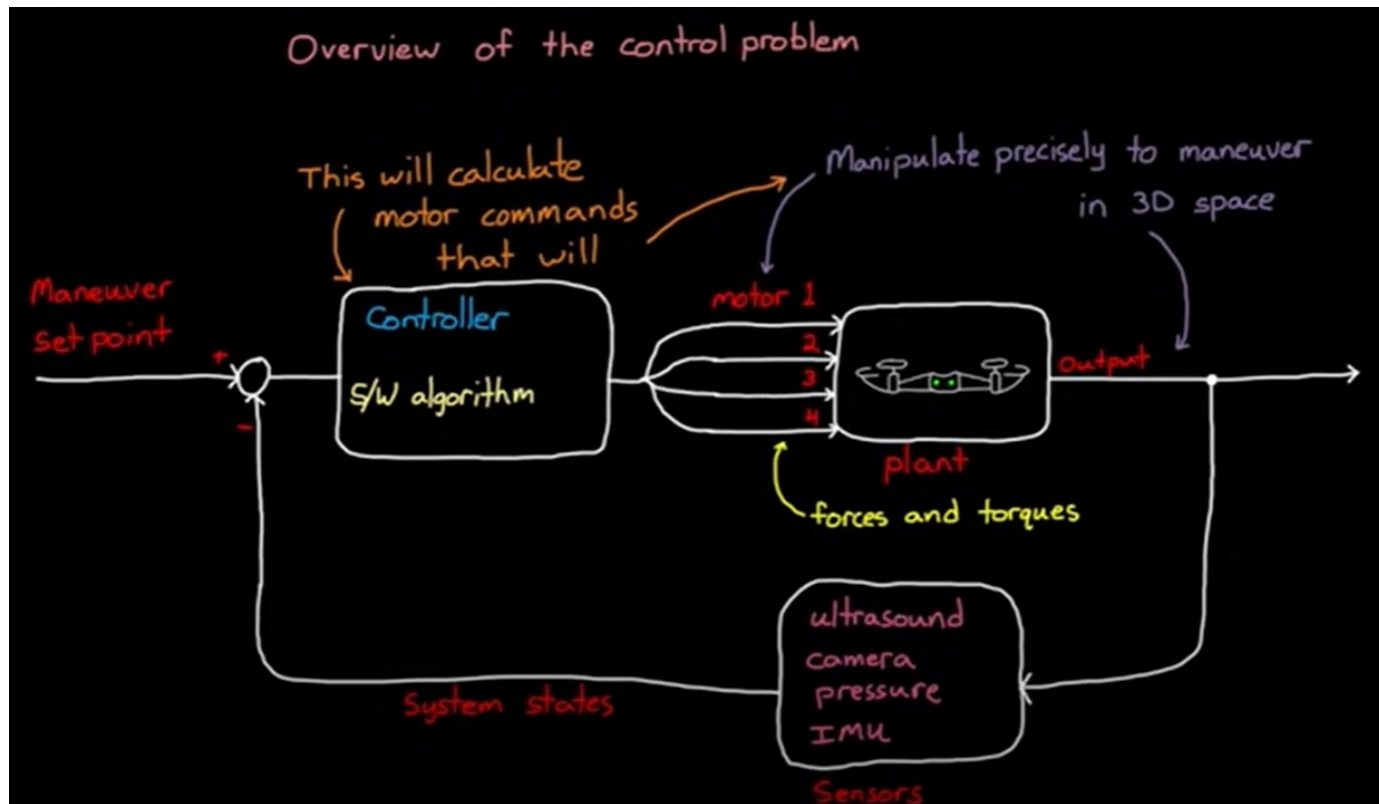
PD controller

Reminder - Control Lab 3 S5

Line tracking control for the 3pi+ mobile robot



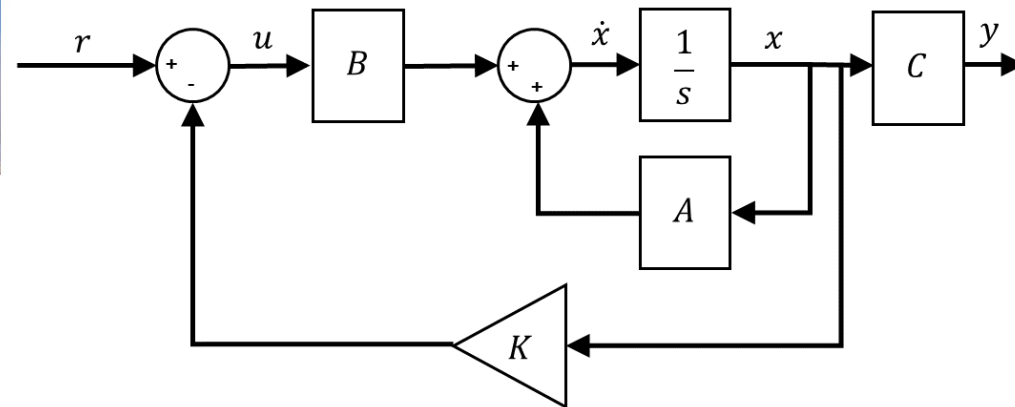
Lab 1 S6 - Altitude control for the Tello mini-drone



Lab 1 S6 - Altitude control for the Tello mini-drone



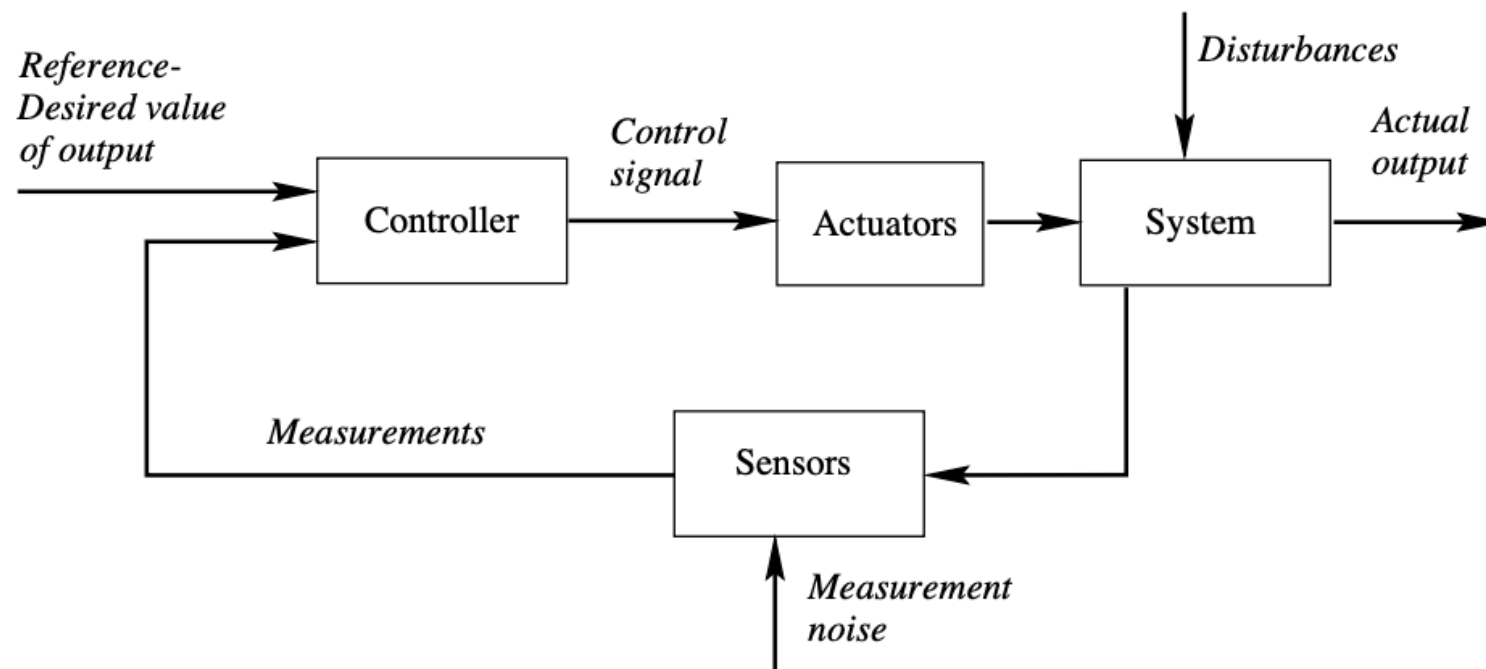
Lab 2 S6 – State feedback control of the rotary inverted pendulum



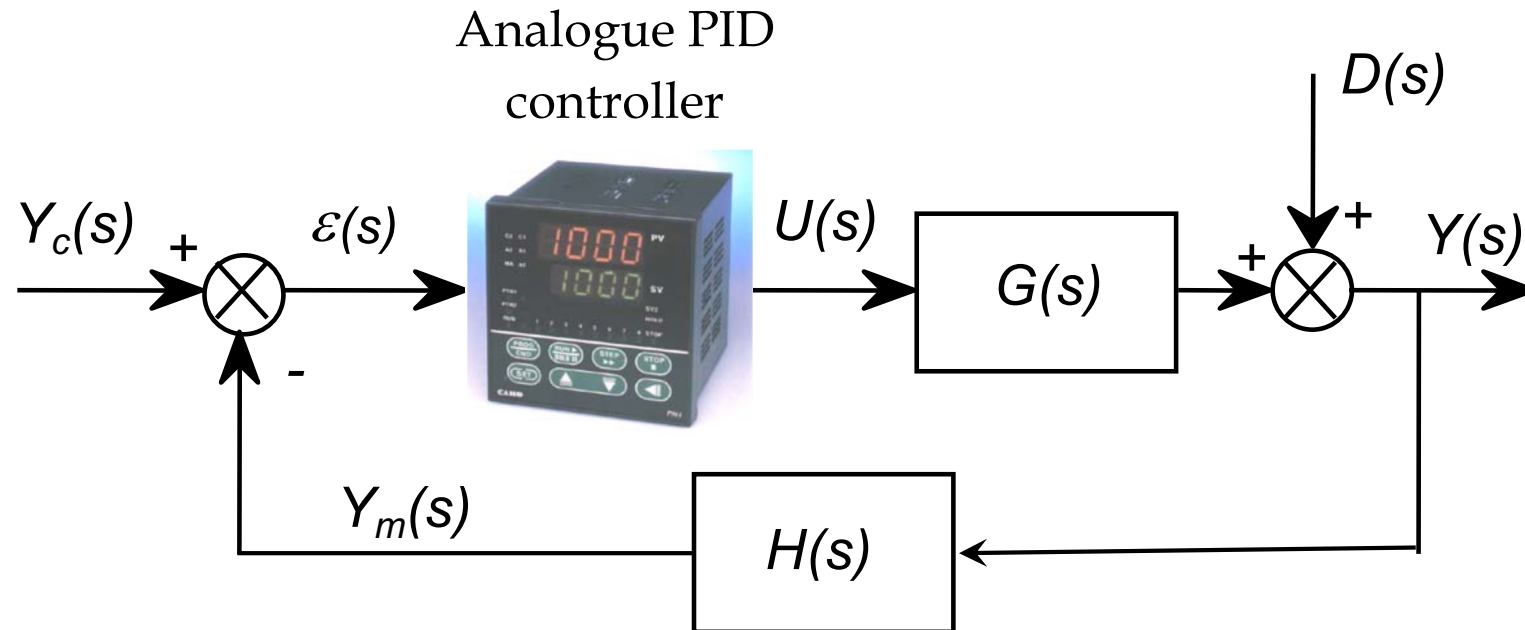
Synthesis of the controller gain by the pole placement method

Reminder - Principle of feedback control

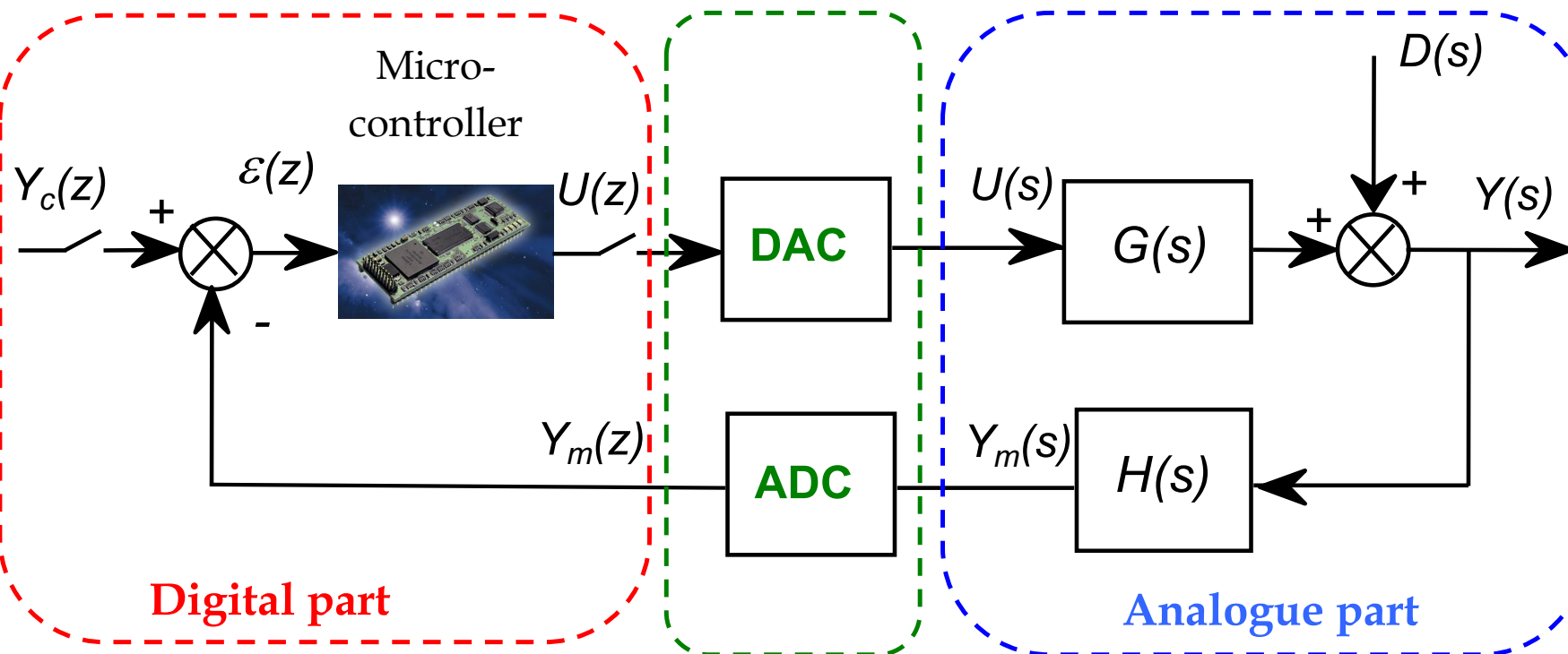
- Designing a control system means inserting:
 - a feedback loop
 - a control element: the controller or regulator



Typical feedback loop in analogue control

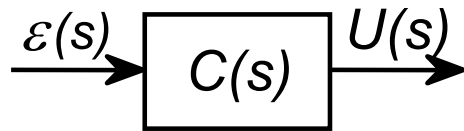


Typical feedback loop in digital control



- Advantages: low cost, speed, high accuracy, insensitivity to noise, ease of implementation and flexibility with regard to modifications
- Need for blocks to enable analogue and digital parts to interact: **DAC** and **ADC**

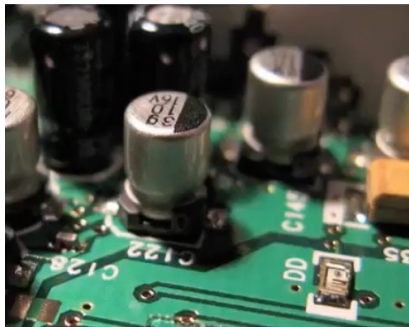
Technology of analogue/digital controllers



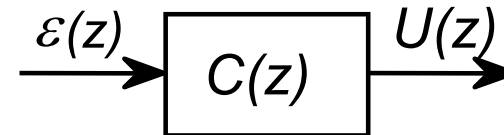
Tool: Laplace transform

$$u(t) = k_p \varepsilon(t) + k_i \int_0^t \varepsilon(\tau) d\tau + k_d \frac{\varepsilon(t)}{dt}$$

Differential equation



Electronic board



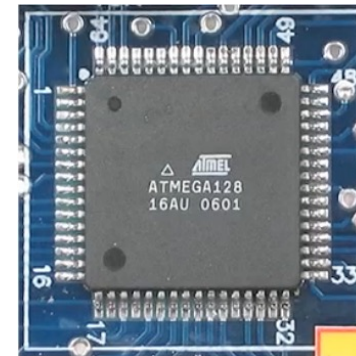
Tool: z transform

$$u(k) = K_p \varepsilon(k) + u_i(k) + u_d(k)$$

Difference equation

program CruiseControl

```
repeat
  r = getReferenceMeasurement
  y = getSpeedMeasurement
  u = K*(r-y);
  sendCommandToEngine(u)
end
```

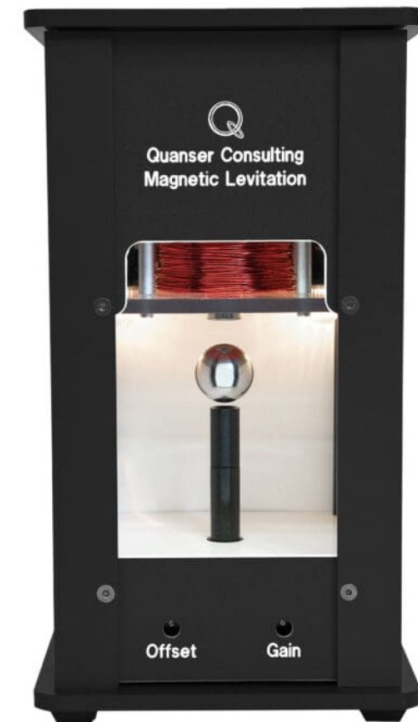


Micro-controller

Lab platform example: analogue versus digital PID controller for magnetic levitation

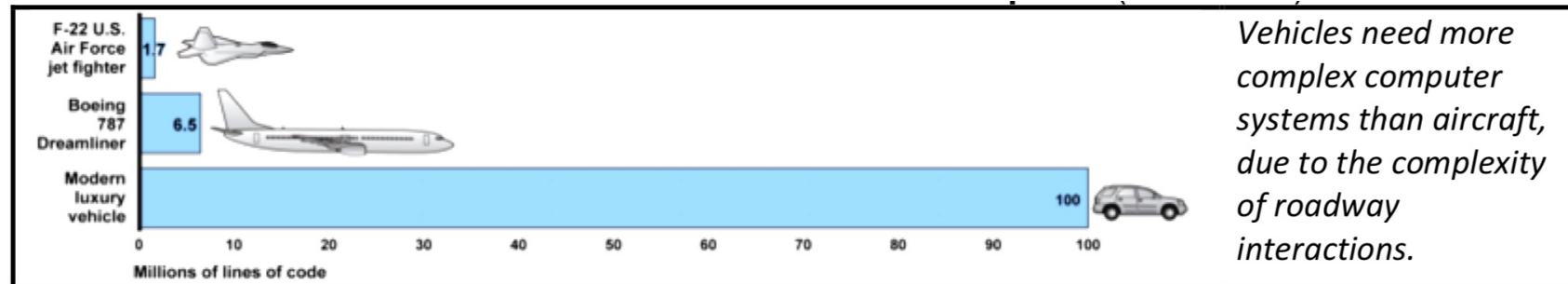
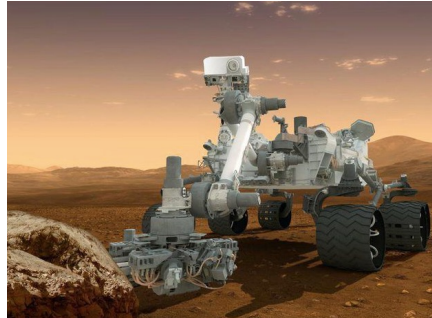


Implementation of the
analogue PID controller
Via electronic amplifiers

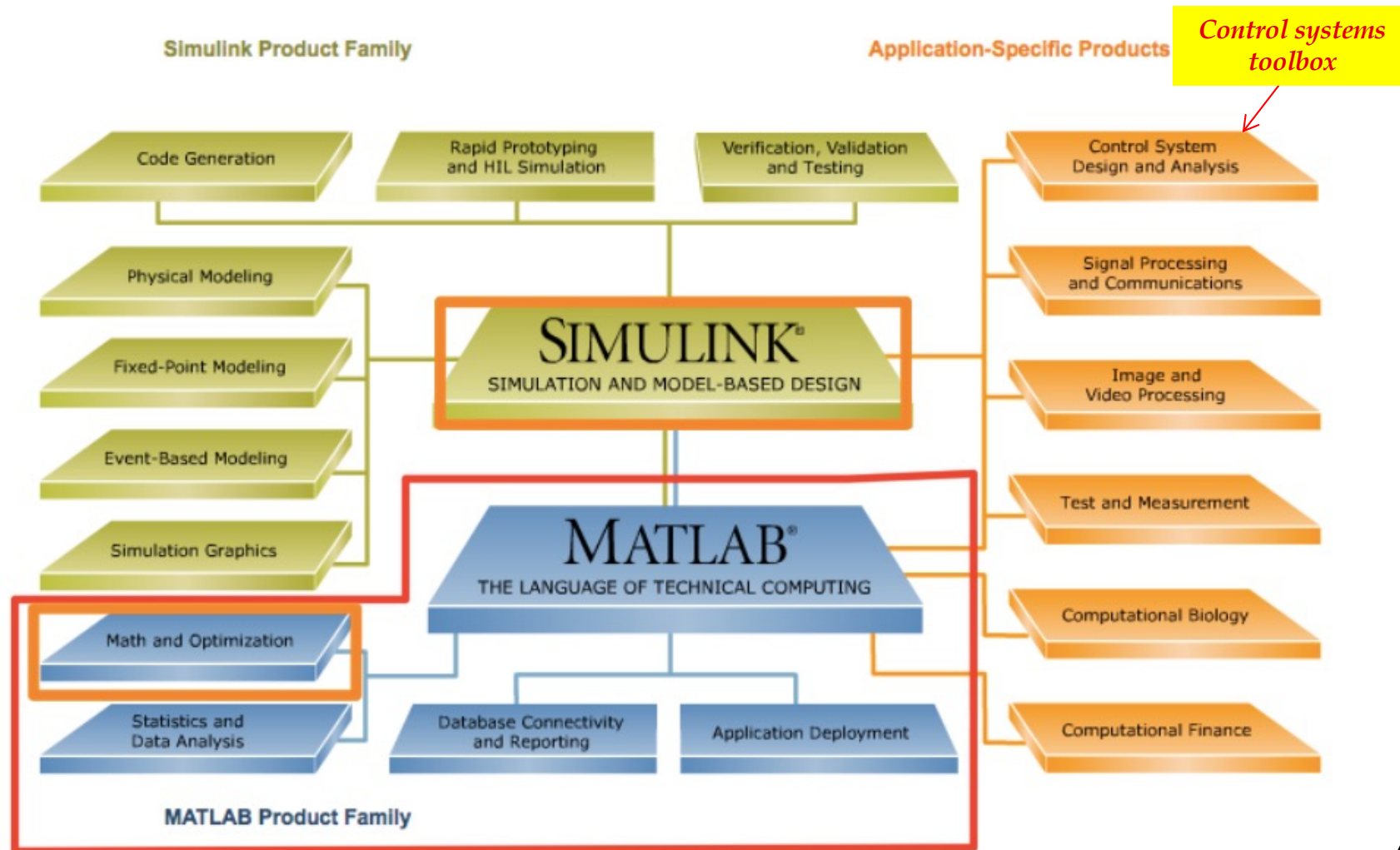


Implementation of the digital
PID controller
via code

Digital control is everywhere



Use of Matlab/Simulink in the tutorial and lab sessions



Objectives of the digital control course

- To provide tools and methods for:
 - analyzing digital control, i.e. the problem of using digital computers or micro-controllers in real time to control physical processes
 - modelling and studying the various interactions between analogue and digital components (ADC/DAC)
 - designing and implementing digital PID controllers

Outline of the digital control course

- I. The z-transform
- II. Analogue to digital converter
- III. Sampled systems
- IV. Discrete-time systems
- V. Design and implementation of digital PID controllers