

Midterm exam - October 3, 2022 - 1h00

Name firstname:

Diploma (IA2R/M3): .

Instructions:

- 1. When necessary, you can answer in French or in English.
- 2. The only material you can consult is your personal A4 recto-verso piece of paper.
- 3. You may use a hand calculator with no communication capabilities.
- 4. Marking rule: for each question, +2 points for a correct answer and 0 point for a wrong or no answer
- 5. Good luck!

List 3 examples of feedback control systems (1 point per correct answer):

First example: asservissement d'altitude d'un drone Second example: régulation de vitesse d'une voiture Third example: régulation de température d'un four

Multiple choice questions (there is one correct answer from the choices only)

Control engineering is applicable to which of the following engineering fields?

Would you classify the step response from the previous question as

 \square undamped

 \Box critically damped

 \Box underdamped

■ overdamped

Match each of the zero-pole plots labelled with a number (1 to 3) displayed in Figure 1.1

Figure 1.1: Zero-pole plot of 3 different linear systems

with one of the transfer functions $G_i(s)$ for $i = 1, ..., 6$ given below

^G1(s) = ^K(^s [−] 3) s + 3 ; ^G2(s) = ^K s ² + 12s + 20 ; ^G3(s) = ^K (s + 3)(s + 6) ^G4(s) = ^K (s + 6)² ; ^G5(s) = ^K s ² + 12s + 45 ; ^G6(s) = ^K (s + 6 − 3i)(s − 6 + 3i) Your answer : 1 - G2(s) 2 - G5(s) 3 - G1(s)

Match each of the four pole-zero diagrams labelled with a number (1 to 4) with one of the unit step responses labelled with a letter (A to D) displayed in Figure 1.2.

Figure 1.2: Pole-zero diagrams and step responses to be paired

Your answer :

From the pole-zero diagram shown in Figure 1.3, the system is

■ stable

 \Box marginally stable

 \square unstable

Figure 1.3: Pole-zero diagram.

Assuming the system has unit steady-state gain, from the pole-zero diagram shown in Figure 1.3, determine its transfer function: $G(s) = \frac{25}{(s+5)(s^2+2s+5)}$

A system has the following characteristic equation: $s^3 + s^2 + 2s + 24 = 0$.

Select the number of roots in the right half of s-plane that the system has: \Box one

zero

 two \Box four

The closed-loop block-diagram for a system is shown in Figure 1.4.

Figure 1.4: Closed-loop block-diagram of a feedback control system

The range of values for k_p that ensures the stability of the closed-loop system is: $\Box \ 0 < k_p < 2$ $\Box k_p > 1$

 \Box $k_p > 13$ $-2 < k_p < 13$

The block-diagram of a traditional closed-loop feedback system is shown in Figure 1.5 (the correct answer gives 3 points).

Figure 1.5: Block-diagram of a traditional closed-loop feedback system

Derive the closed-loop transfer function: $F_{CL}(s) = \dfrac{Y(s)}{R(s)}$. Explain how you get it!

$$
Y(s) = G(s)U(s)
$$

\n
$$
U(s) = C(s)\varepsilon(s)
$$

\n
$$
\varepsilon(s) = R(s) - Y_m(s)
$$

\n
$$
Y_m(s) = H(s)Y(s)
$$

\n
$$
F_{CL}(s) = \frac{Y(s)}{R(s)} = \frac{C(s)G(s)}{1 + C(s)G(s)H(s)}
$$

Some useful properties of the Laplace transform

$$
L(\alpha x(t) + \beta y(t)) = \alpha X(s) + \beta Y(s)
$$

\n
$$
L(\dot{x}(t)) = sX(s) - x(0)
$$

\n
$$
\lim_{t \to +\infty} x(t) = \lim_{s \to 0} sX(s)
$$
 if the limit exists

Some Laplace transform pairs

First-order systems

$$
G(s) = \frac{K}{1 + Ts}
$$

The 2 characteristic parameters of a first order system are:

- K: steady-state gain: $K = \lim_{s \to 0} G(s)$
- $T:$ time-constant

Characteristic values of a first-order system step response

Rise-time at 63% $T_{m}^{63\%} = T_{m}^{63\%}$ Rise-time at 95% $T_m^{95\%} \approx 3T$ Settling-time at 5 % $T_r^{5\%} \approx 3T$

Second-order systems

$$
G(s) = \frac{K}{\frac{s^2}{\omega_0^2} + 2\frac{z}{\omega_0}s + 1} = \frac{K\omega_0^2}{s^2 + 2z\omega_0s + \omega_0^2}
$$

- $K:$ steady-state gain
- z : damping ratio $(z > 0)$
- ω_0 : undamped natural frequency

Characteristic values of a underdamped second-order system step response

Value of the first overshoot in $\%$ $\frac{y(T_{D_1}) - y(+\infty)}{y(+\infty) - y(0)} \times 100 = e$ $-\pi z$ $\sqrt{1-z^2} \times 100$ Damping coefficient as a function of D_1 (not in $\%)$ $\int (\ln(D_1))^2$ $(\ln(D_1))^2 + \pi^2$ Time-instant of the first overshoot π ω_0 √ $1 - z^2$ Value of the n^{th} overshoot in $%$ th overshoot in % $D_{n\%} = -(-D_1)^n \times 100$ Time-instant of the n^{th} overshoot th overshoot $T_{D_n} = n T_{D_1}$