

Advancements in Unsupervised Prognostics

Dr. Mayank S JHA



Research

Centre de Recherche en Automatique de Nancy
(CRAN) UMR 7039,
Faculté des Sciences et Technologies
Boulevard des Aiguillettes - BP 70239 - Bât.
1er cycle 54506 Vandoeuvre-lès-Nancy
Cedex France

Associate Professor
(Maitre de Conférences)

mayank-shekhar.jha@univ-lorraine.fr



Teaching

Polytech Nancy (ESSTIN),
2 Rue Jean Lamour 54509
Vandoeuvre-lès-Nancy,
Cedex France



Contents

- Prognostics and Deep learning (supervised)
- Unsupervised Prognostics through Data Augmentation
 - Data Augmentation
 - Health Index Extraction
 - RUL Prediction

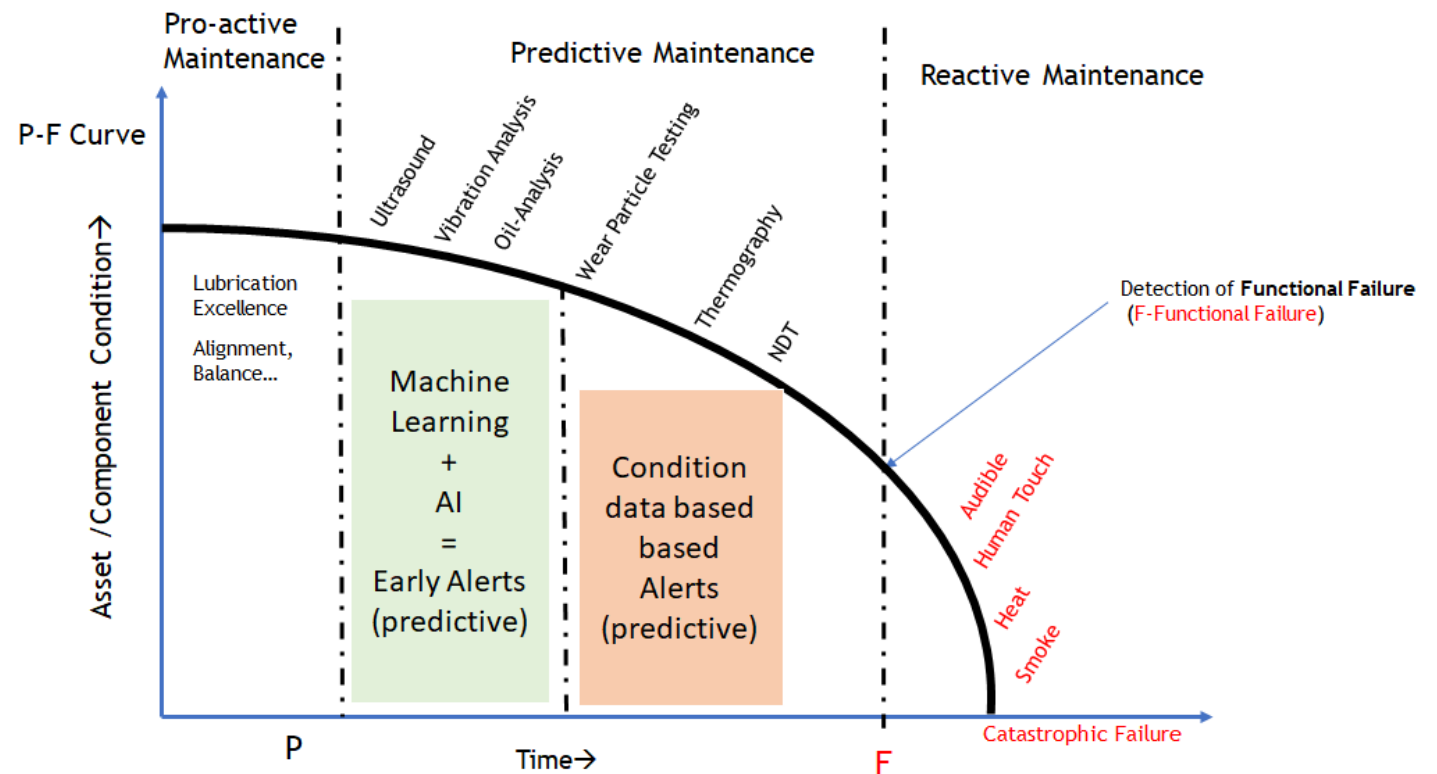


Prognostics

Prognostics

Prognostics:

- Estimate (state of health) → identification of degradation model.
- Prediction of future health + **Remaining Useful Life (RUL)**
- Evaluate: Decision “when failure occurs ???” “what maintenance strategy”



Prognostics

- Prognostics:
 - Estimate (state of health) → identification of degradation model.
 - Prediction of future health + **Remaining Useful Life (RUL)**
 - Evaluate: Decision “when failure occurs ???” “what maintenance strategy”

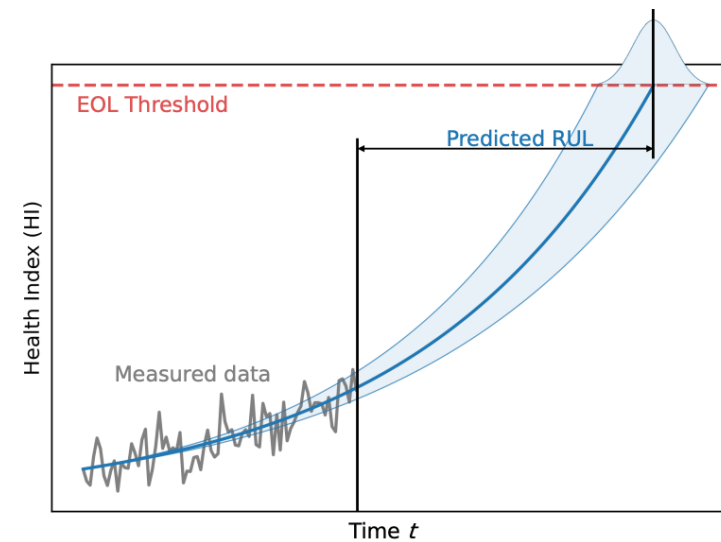
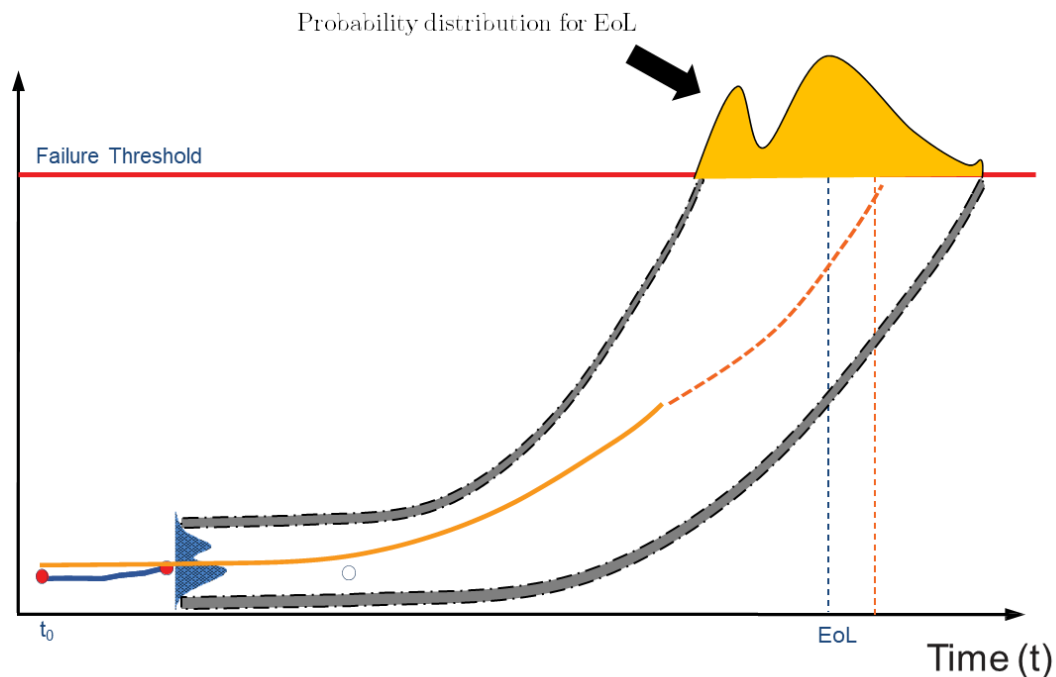


Figure: Traditional prognostics process.

Health Index (HI)

Indicator that estimates the true SOH of the system studied. Can be built by fusing multiple sensor signals [Lei et al., 2018].

Remaining Useful Life (RUL)

Time remaining between current instant t_k and EOL [Gouriveau et al., 2017].

$$RUL(t_k) = t_{EOL} - t_k \quad (1)$$

Degradation Data

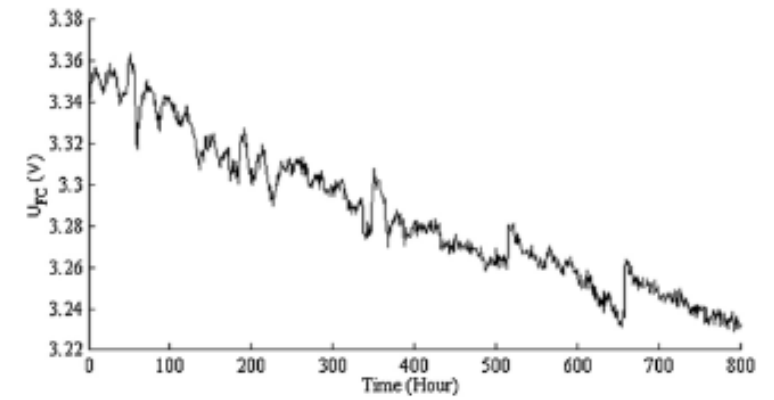
Degradation:

- unknown, non-linear varying dynamics
- sensor data: non-stationary → trend, seasonality, cyclic etc.
- depends on qualitative+ quantitative factors.

Degradation Data

Degradation:

- unknown, non-linear varying dynamics
- sensor data: non-stationary → trend, seasonality, cyclic etc.
- depends on qualitative+ quantitative factors.

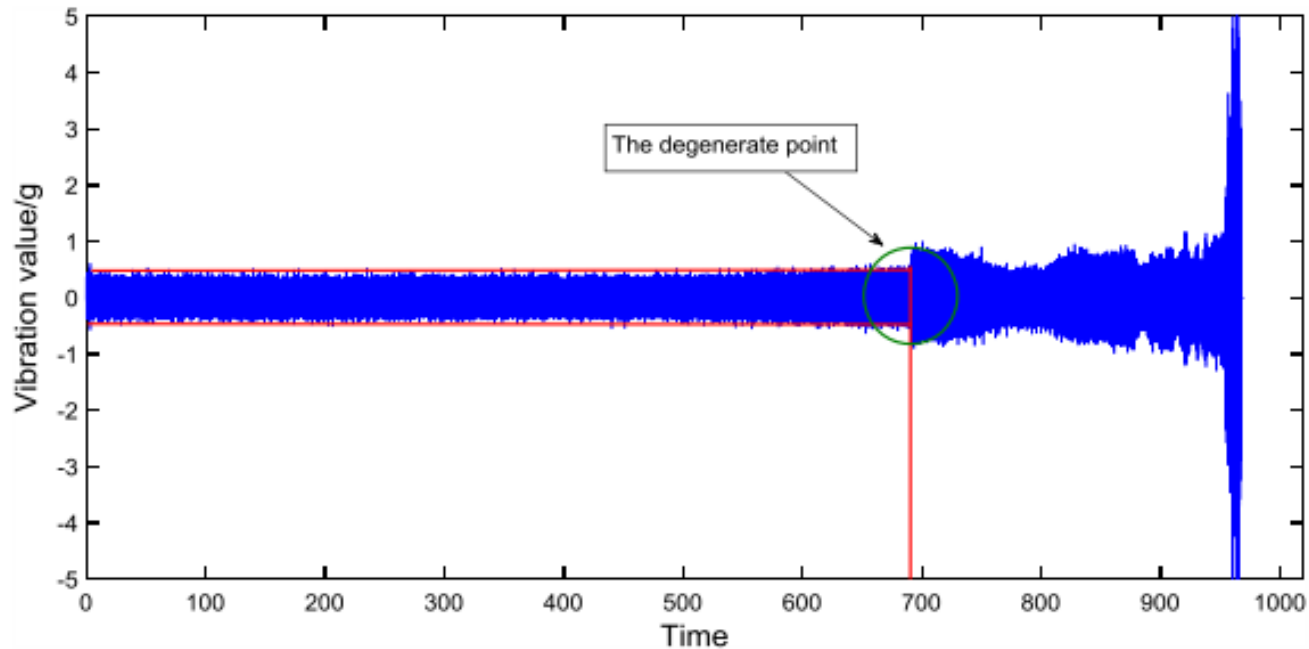


PEM Fuel Cell degradation (Jha et al. 2016)

Degradation Data: Sequentially related Time Series data

Degradation:

- unknown, non-linear varying dynamics
- sensor data: non-stationary → trend, seasonality, cyclic etc.
- depends on qualitative+ quantitative factors.

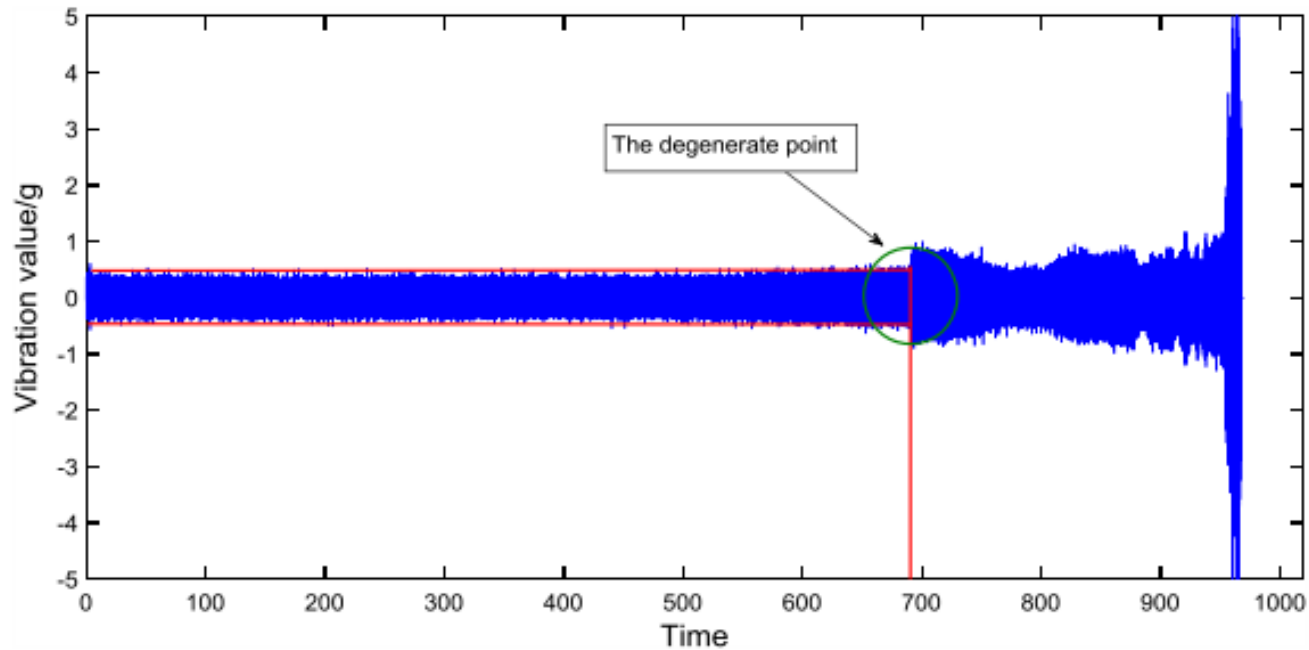


Roller bearing degradation (PRONOSTIA platform)

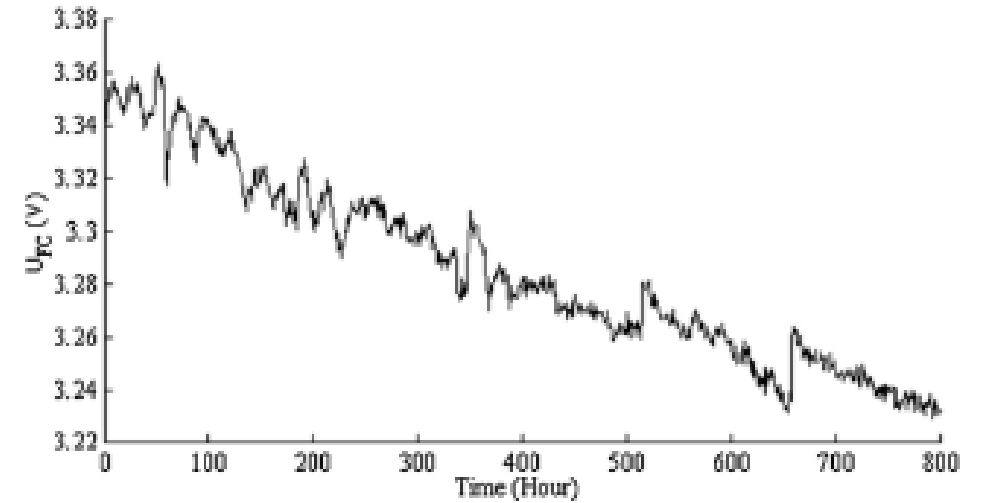
Degradation Data: Sequentially related Time Series data

Degradation:

- unknown, non-linear varying dynamics
- sensor data: non-stationary → trend, seasonality, cyclic etc.
- depends on qualitative+ quantitative factors.



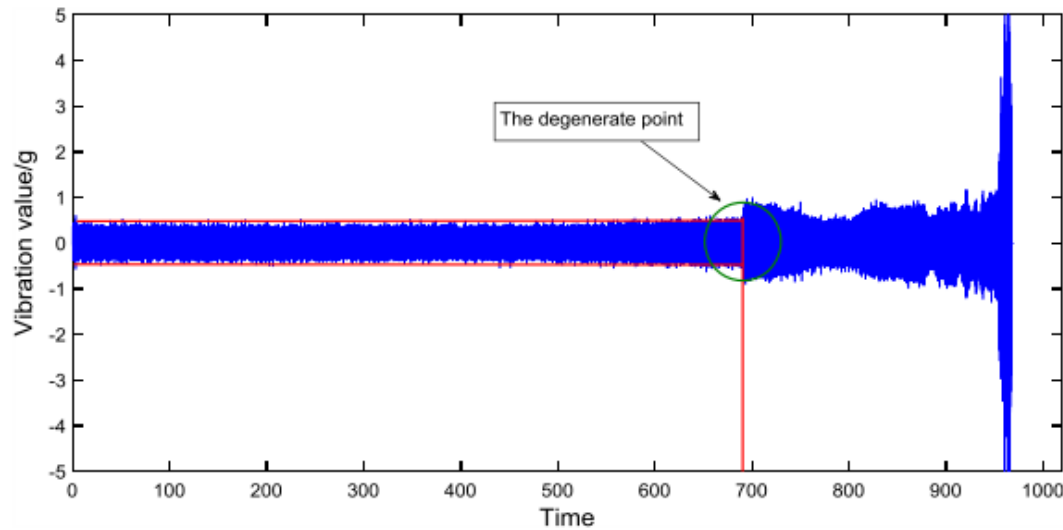
Roller bearing degradation (PRONOSTIA platform)



PEM Fuel Cell degradation (Jha et al. 2016)

Degradation Data

- Degradation:
 - unknown, non-linear varying dynamics
 - sensor data: non-stationary process → trend, seasonality, cyclic etc.
 - depends on qualitative+ quantitative factors.
- Raw degradation data → Hidden features / representation:
 - Spatially varying
 - Temporally varying
 - Multimodal characteristics



Roller bearing degradation (PRONOSTIA platform)

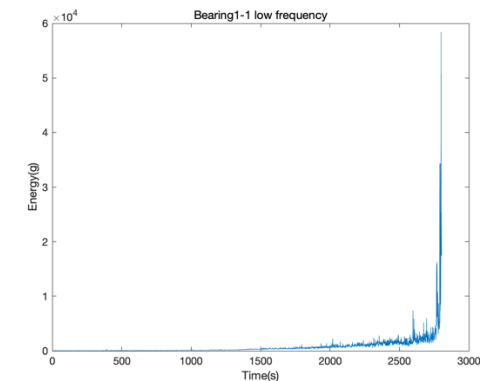
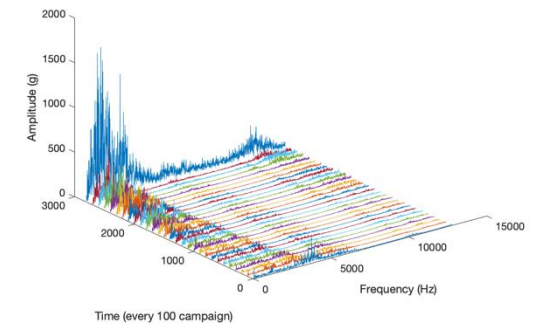
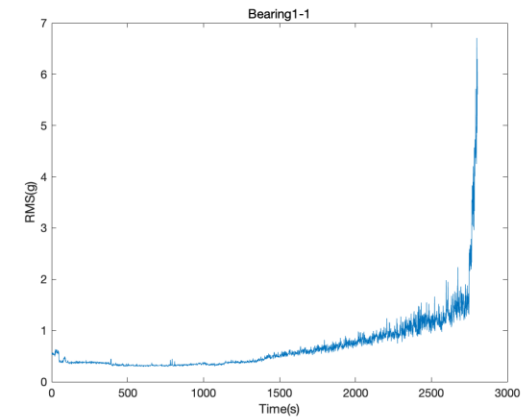


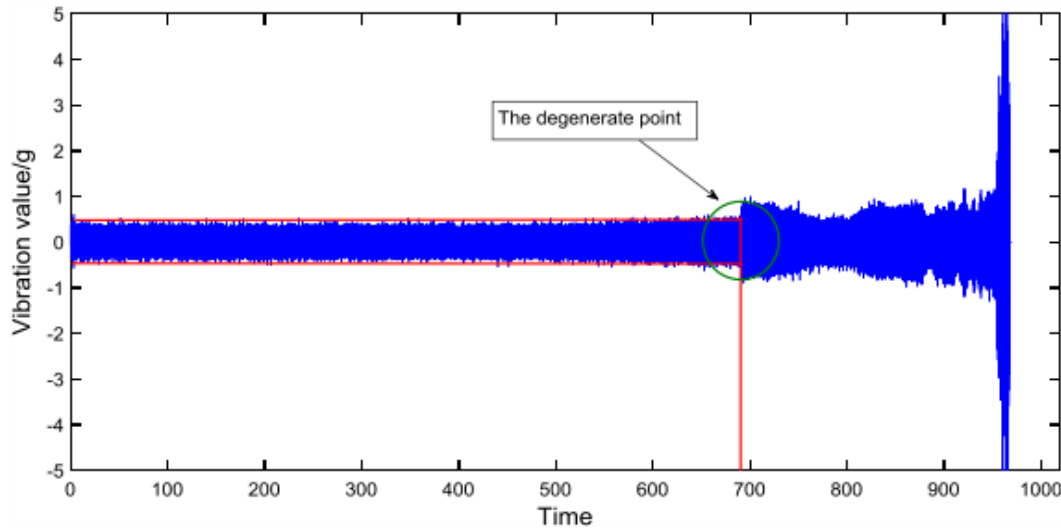
Photo: Report of Jha

Prognostics and Deep Learning (Supervised Setting)

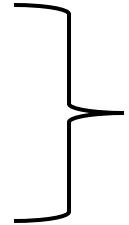
Convolutional Neural networks (CNNs)

Degradation Data

- Degradation:
 - unknown, non-linear varying dynamics
 - sensor data: non-stationary process → trend, seasonality, cyclic etc.
 - depends on qualitative+ quantitative factors.
- Raw degradation data → Hidden features / representation:
 - Spatially varying
 - Temporally varying
 - Multimodal characteristics



Roller bearing degradation (PRONOSTIA platform)



CNNs

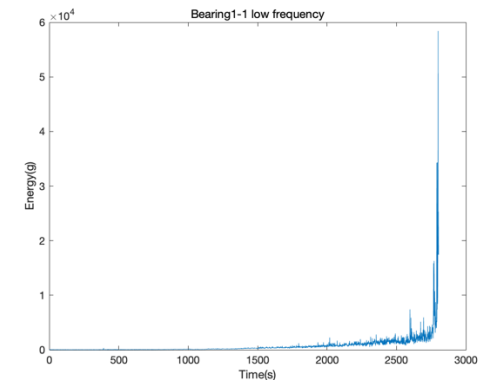
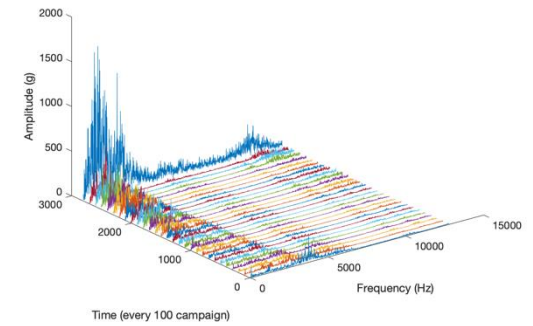
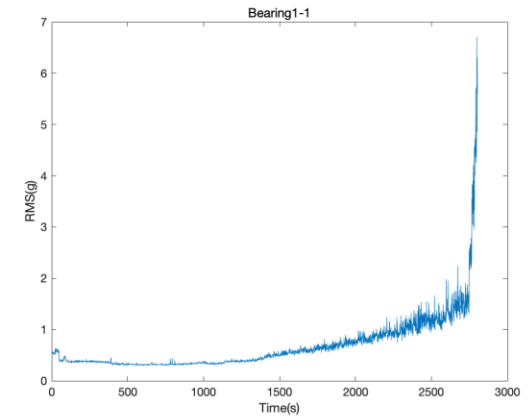
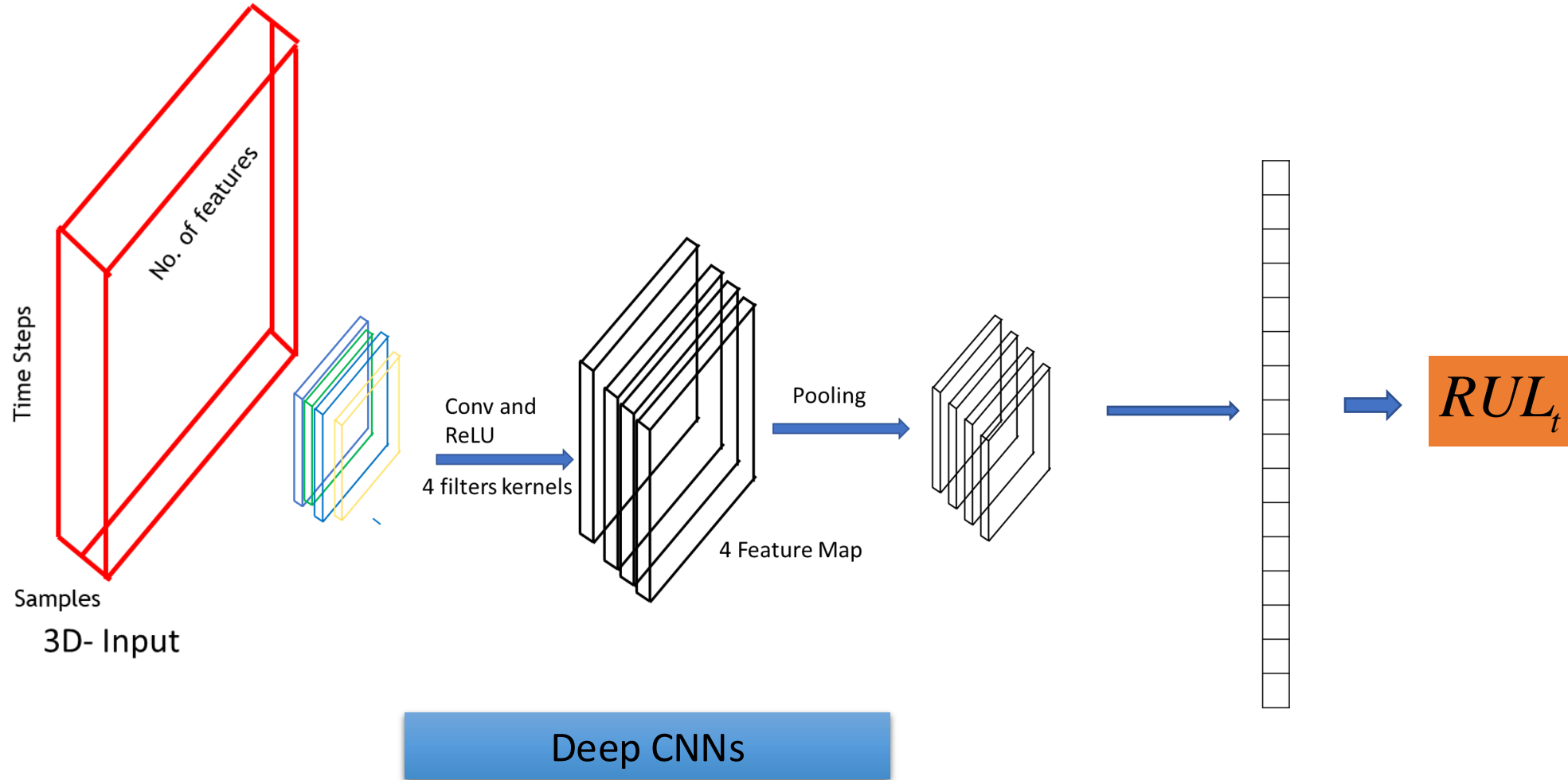


Photo: Report of Jha

CNNs for Prognostics

- CNNs → Traditionally, 2D-3D structured data for face/object recognition
- Prognostics → 3D structured topology for sequence data



CNNs for Prognostics

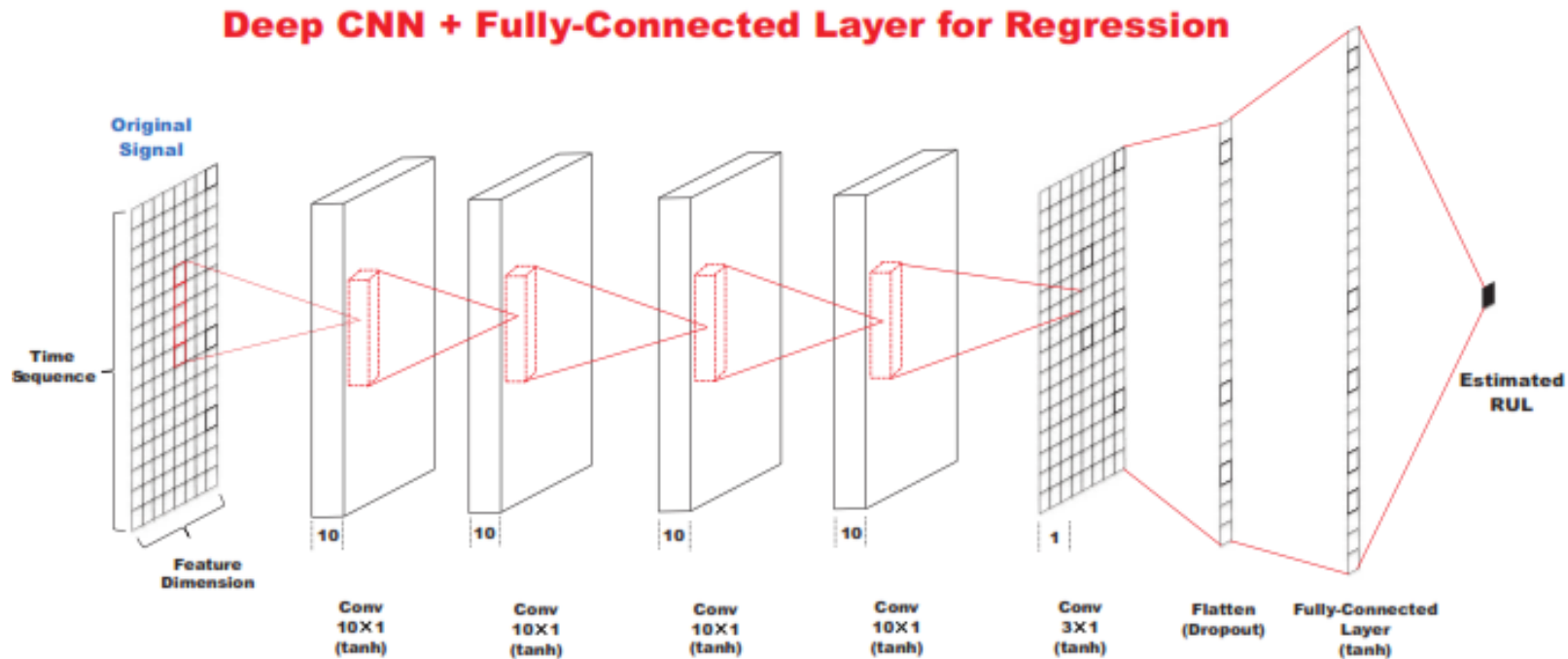
- Automatically learn feature representation, hidden multimodal distributions

[Liu et al., 2017] [Jing et al., 2017] [Li et al., 2018]

&

- Efficient learning with multi-variate sequential (time series) data.

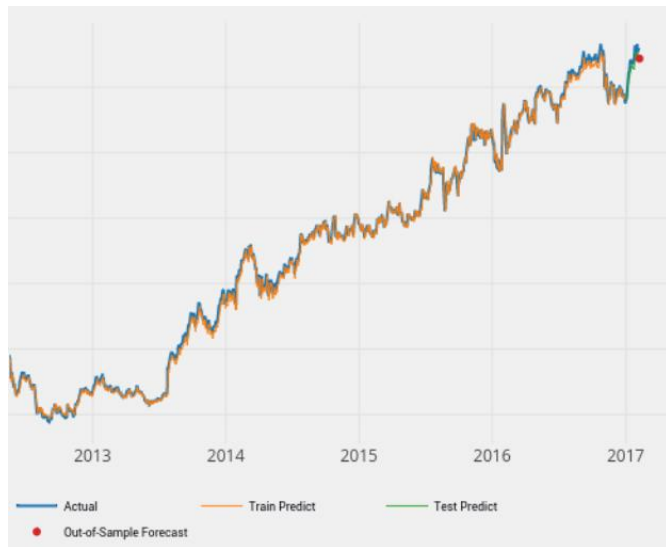
[Babu et al., 2016]



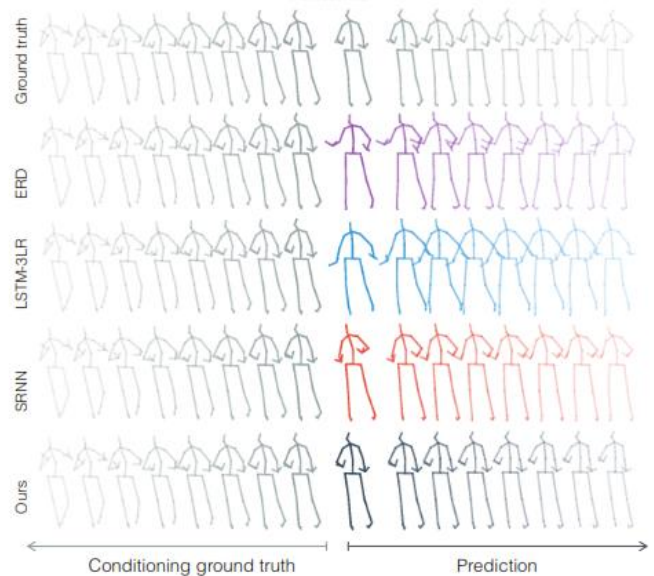
[Liu et al., 2017]

Sequence modelling : Motivations

- Sequential data:
 - time series forecasting,
 - motion prediction (human, self driving cars)
 - sensor data: machine health monitoring/prediction
 - text processing/prediction
 - machine translation



Financial market prediction (Dixon et al.)

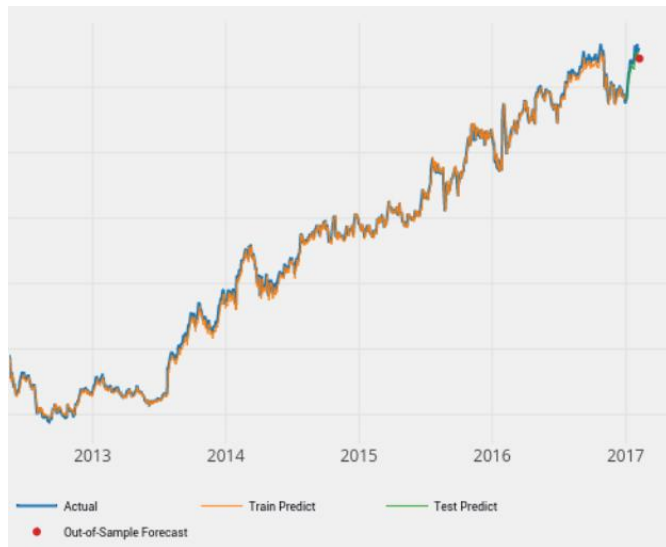


Human Motion Prediction

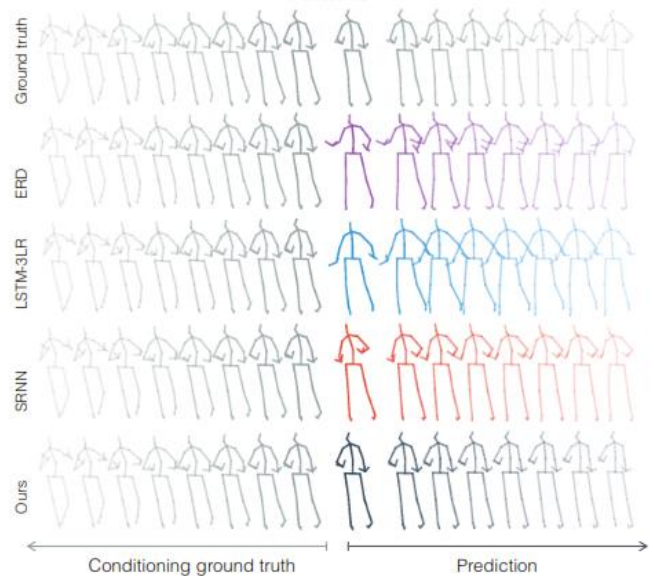
Martinez et al., 2016

Sequence modelling : Motivations

- Sequential data:
 - time series forecasting,
 - motion prediction (human, self driving cars)
 - sensor data: machine health monitoring/prediction
 - text processing/prediction
 - machine translation

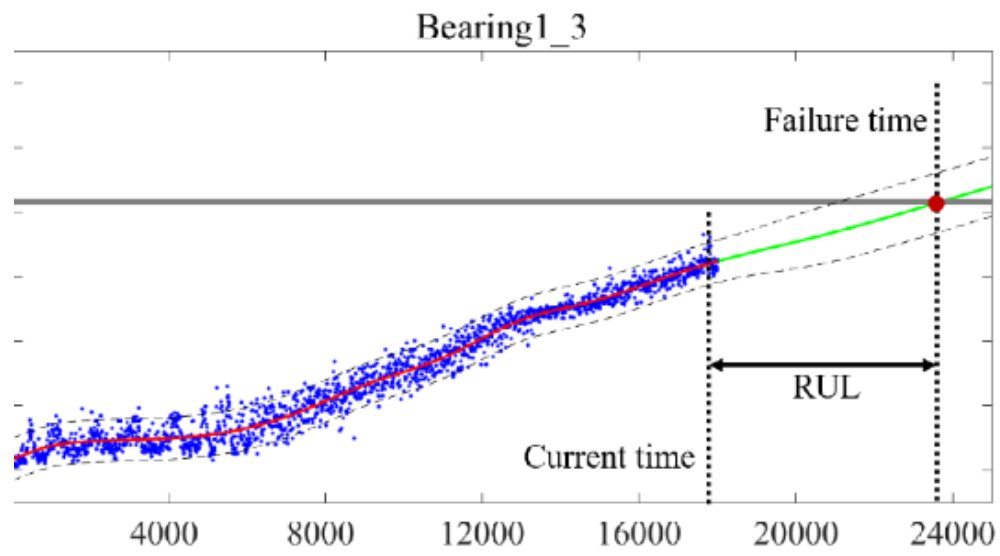


Financial market prediction (Dixon et al.)



Human Motion Prediction

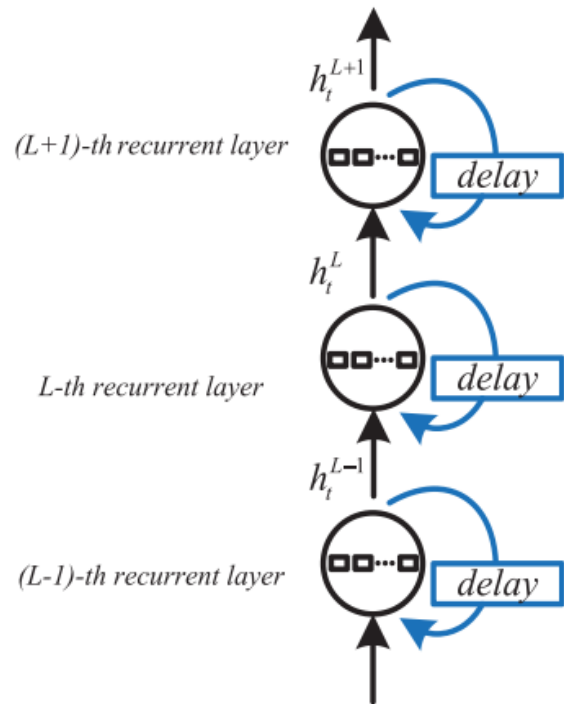
Martinez et al., 2016



Component Failure Prediction

(Yoo et al., 2018)

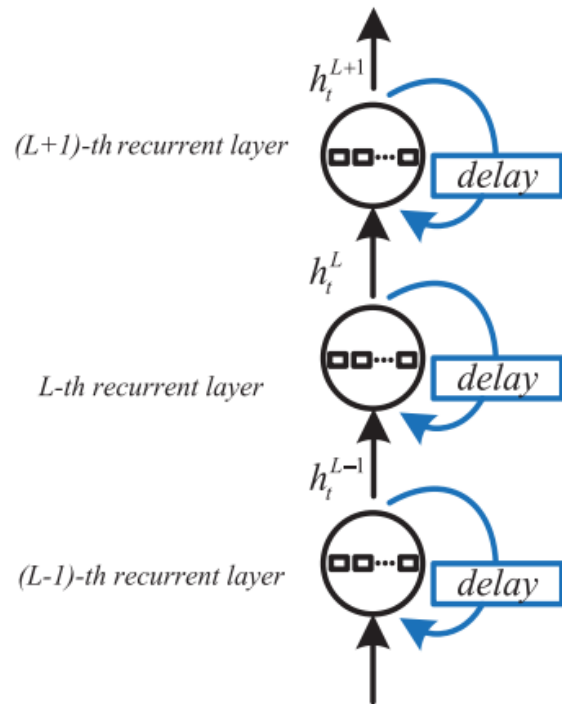
Deep (Stacked) LSTMs (Fernández, Graves, & Schmidhuber, 2007):



Deep (Stacked) LSTMs (Fernández, Graves, & Schmidhuber, 2007):

LSTM Variants:

- Peephole connections
- Gated Recurrent Units (GRUs) (Cho et al. 2014), Bi-LSTMs....



LSTM Variants:

- Peephole connections
- Gated Recurrent Units (GRUs) (Cho et al. 2014)
- etc.

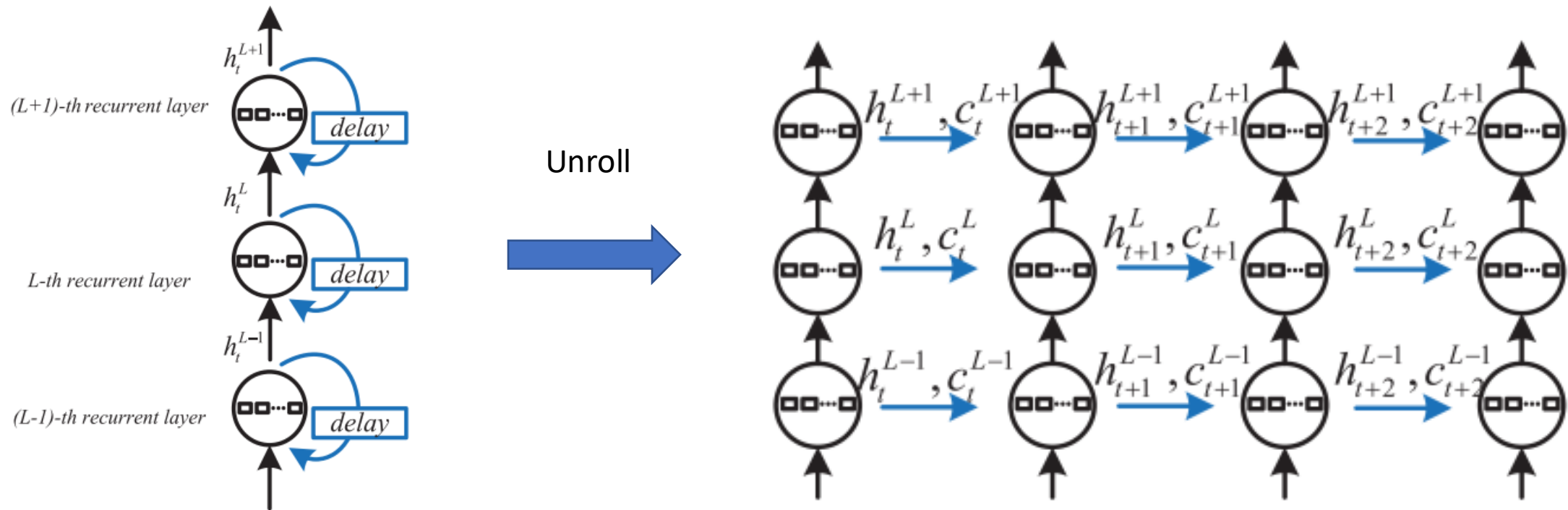


Image credits: Fernández, Graves, & Schmidhuber, 2007

Data Preparation for RUL prediction

- Degradation data → Time Series sequence → segmented into sliding windows.
- Each sliding window is assigned a target RUL value [Zeng et al. 2017]

$X = [X_1, X_2, \dots, X_t, \dots, X_{T-1}]$ to estimate RUL_{T-1}

$X = [X_1, X_2, \dots, X_t, \dots, X_{T-2}]$ to estimate RUL_{T-2}

Data Preparation for RUL prediction

- Degradation data → Time Series sequence → segmented into sliding windows.
- Each sliding window is assigned a target RUL value [Zeng et al, 2017]

$X = [X_1, X_2, \dots, X_t, \dots, X_{T-1}]$ to estimate RUL_{T-1}

$X = [X_1, X_2, \dots, X_t, \dots, X_{T-2}]$ to estimate RUL_{T-2}

Many variants exist!

$$[X_t, X_{t-1}, \dots, X_{t-d+1}], \in \mathbb{R}^d$$

$$[RUL_{t+L}, RUL_{t+L+1}, \dots, RUL_n]$$

Training tuples:

$$([X_t, X_{t-1}, \dots, X_{t-d+1}], RUL_{t+L})$$



$$\widehat{RUL}_{t+L} = \phi(X_t, X_{t-1}, \dots, X_{t-d+1})$$

Loss Calculation : Error based cost function

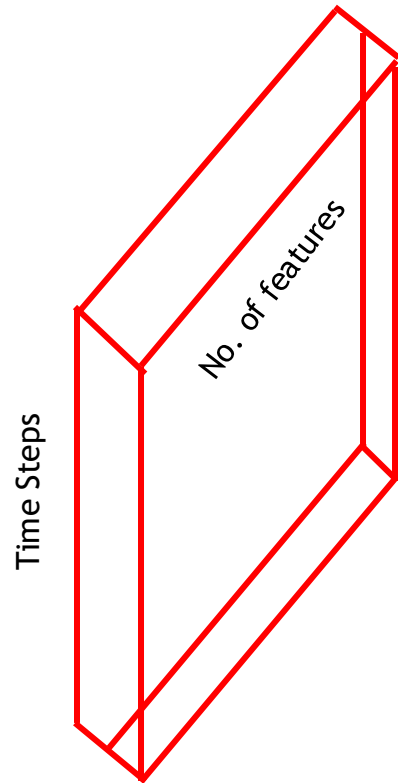
$$J = \sum_t \| (RUL_{est}^t - RUL_{calc}^t) \|^2$$

Some issues:

- Independent Windows → to assure assumption of i.i.d
- Dependent windows → claim more realistic.

Deep LSTMs for Prognostics

Basic Architecture



Samples
3D- Input

Deep LSTMs for RUL prediction

Basic Architecture

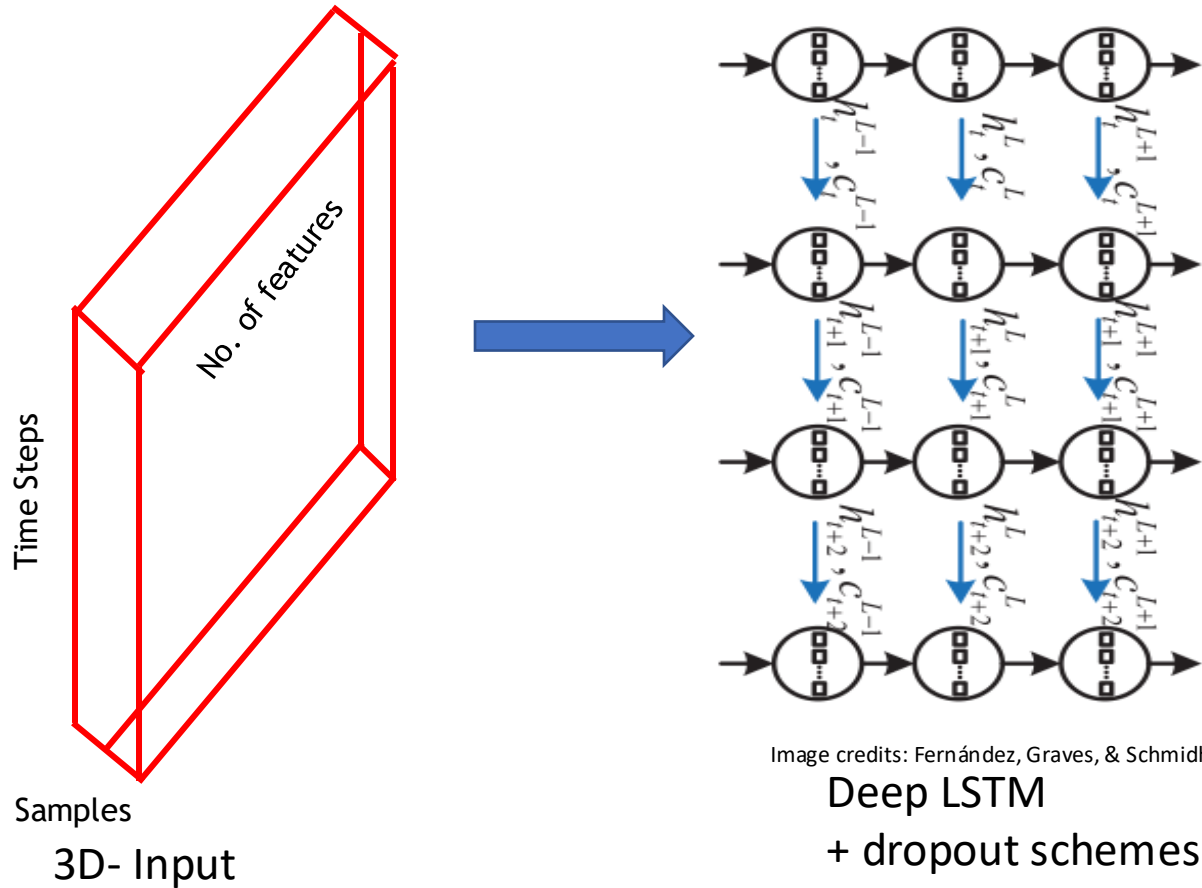


Image credits: Fernández, Graves, & Schmidhuber, 2007

Deep LSTMs for RUL prediction

Basic Architecture: LSTMs: Temporal features + FNNs: Map features in RULs

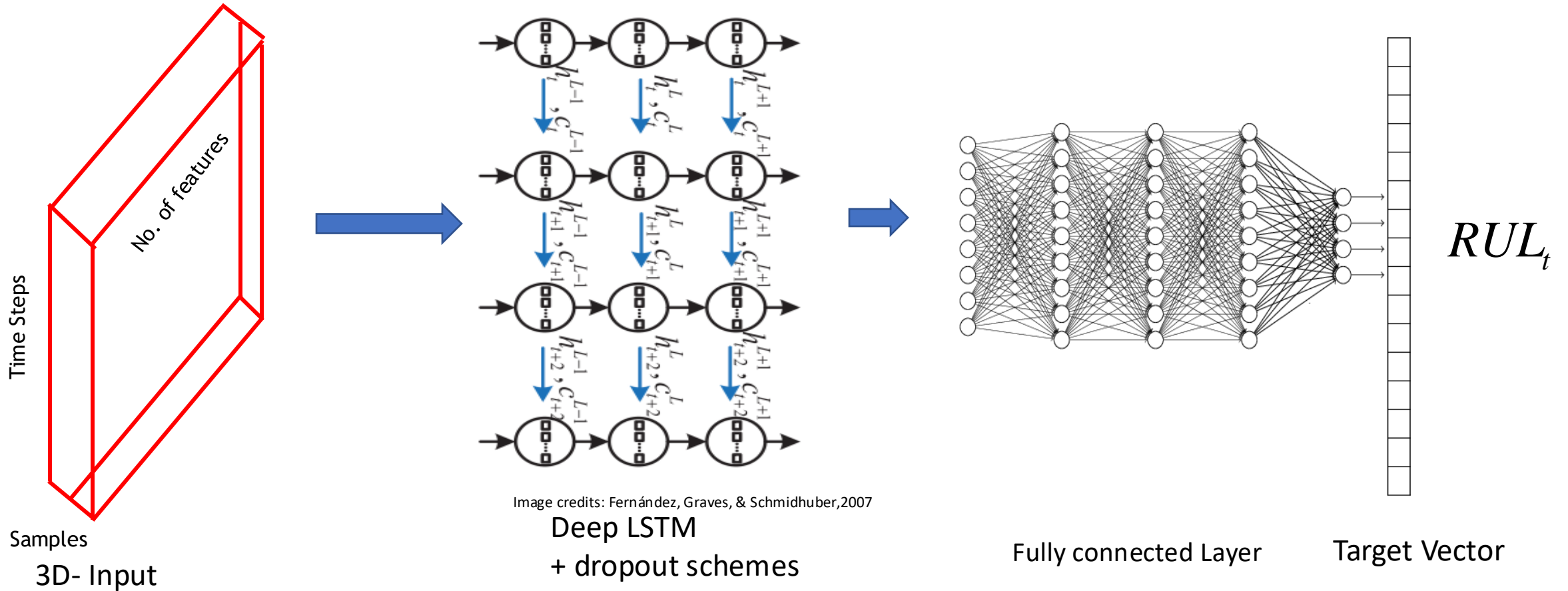
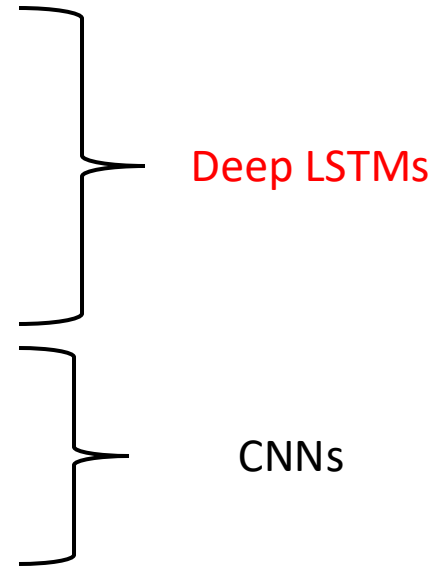


Image credits: Fernández, Graves, & Schmidhuber, 2007

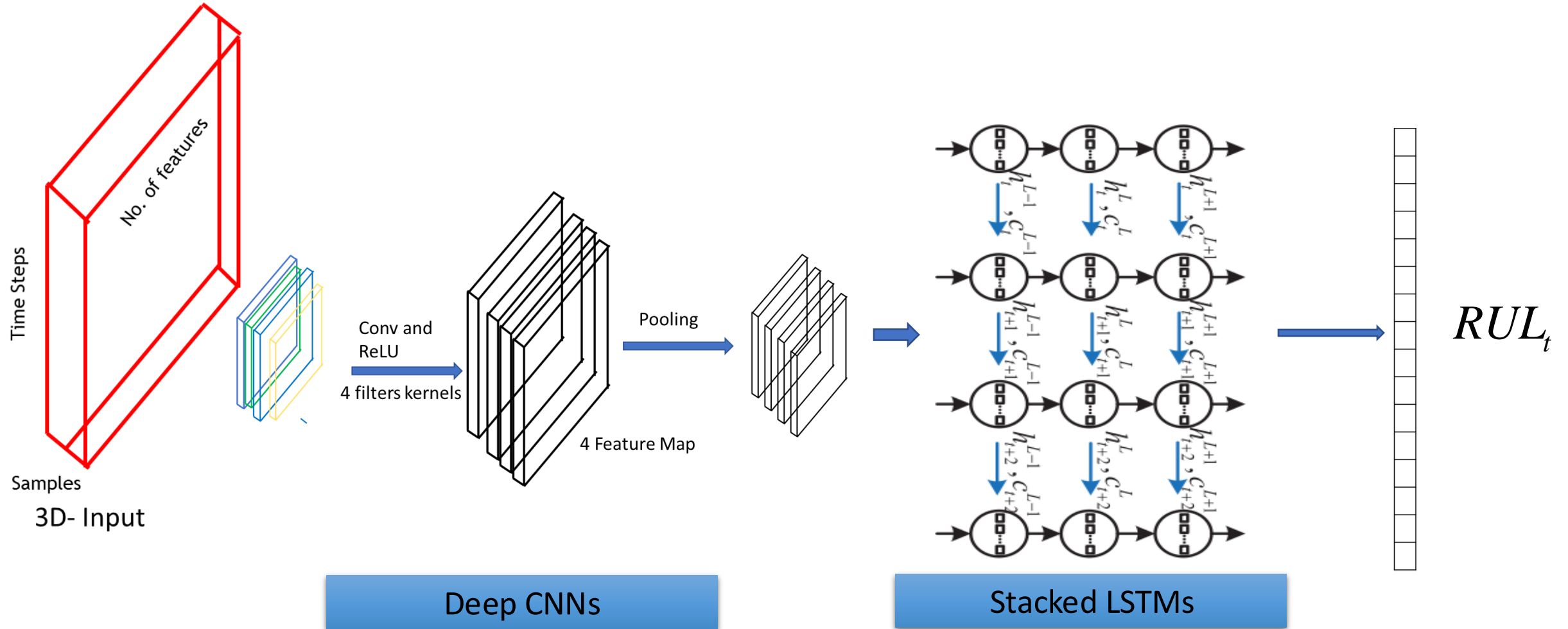
Degradation Data

- Degradation:
 - unknown, non-linear varying dynamics
 - sensor data: non-stationary process → trend, seasonality, cyclic etc.
 - depends on qualitative+ quantitative factors.
- Raw degradation data → Hidden features / representation:
 - Spatially varying
 - Temporally varying
 - Multimodal characteristics



CNNs for Prognostics

- CNNs → Traditionally, 2D-3D structured data for face/object recognition
- Prognostics → 3D structured topology for sequence data



CNNs+LSTMs for Prognostics

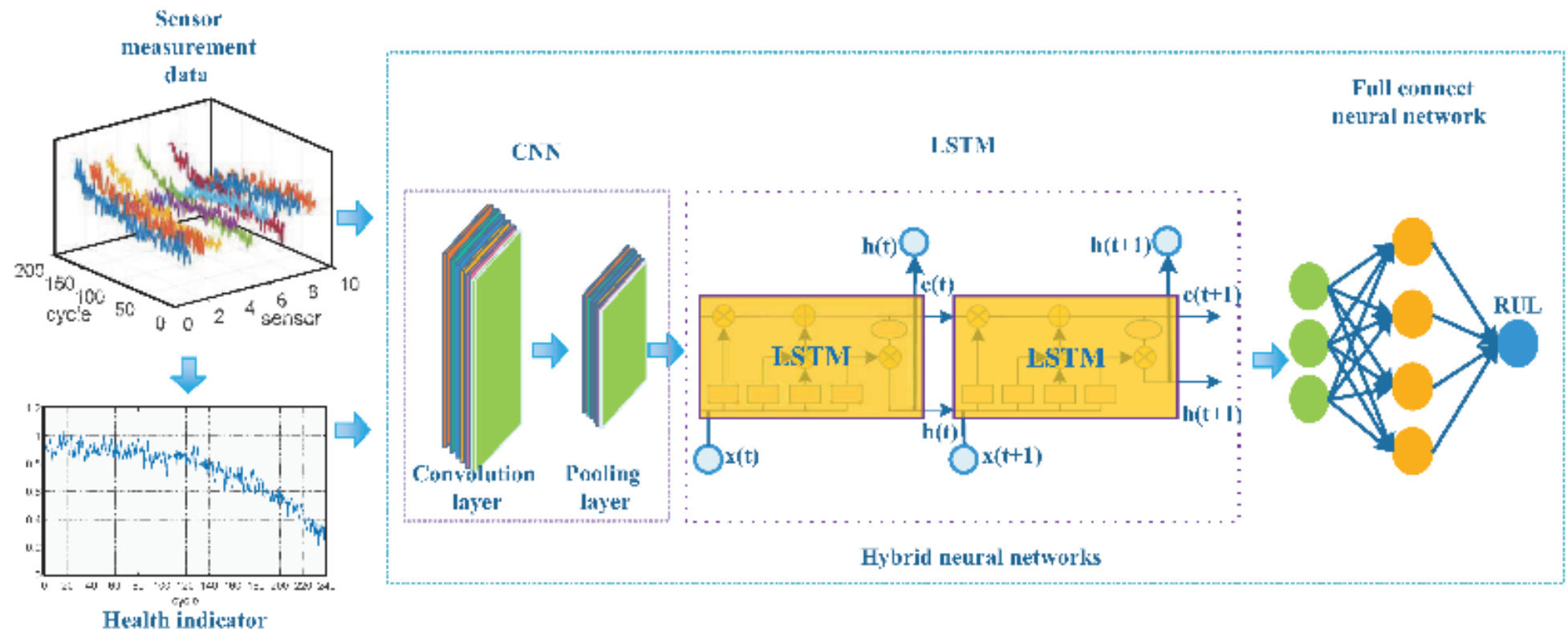
- Automatically learn feature representation, hidden multimodal distributions

[Liu et al., 2017] [Jing et al., 2017] [Li et al., 2018]

& Efficient learning with multi-variate sequential (time series) data.

[Babu et al., 2016]

Hybrid structure



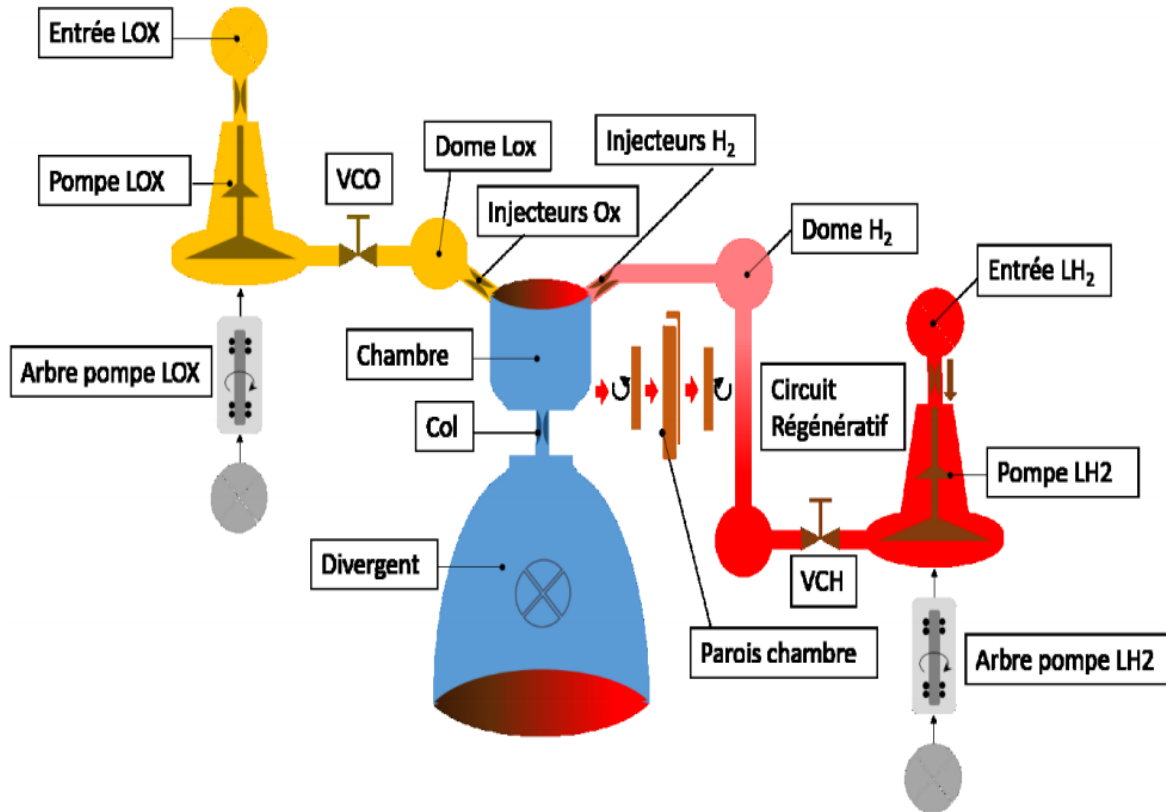
[Kong et al. 2019]

Deep Learning based Prognostics (supervised)

Dr. Mayank JHA, Prof. Didier Theilliol



System of Interest: Reusable Liquid Rocket Engine



Simulation Engine: CNES RT-NT-2510000-CNES

01

LOX LH2 engine with 10 kN thrust
thrust with liquid propellant supply

02

Main components of a liquid ergol engine the fuel system and a combustion chamber

03

Typical engine life profiles :
a. flight engines

04

Variables controlled :
Chamber pressure
Mixing ratio

Unsupervised Prognostics through Physics Informed Data Augmentation

Collaborators:

Dr. Martin Herve deBeaulieu (Phd @ CRAN/Dassault Av., **Most Slides Credit**)

Prof. Hugues Garnier (CRAN)

Dr. Farid Cerbah (Dassault Aviation)



FALCON 6X



POLYTECH
NANCY



UNIVERSITÉ
DE LORRAINE



Challenges:

First challenge: RUL-labeled data limitation

- RUL-labeled data hardly available in real-life applications [Chaoub et al., 2022]
- Limiting reliance on measured RUL-labeled data for model training.

Second challenge: *A priori* knowledge and physics integration

- Leverage existing system knowledge
- Use physics of degradation
- Strengthen the AI-based prognostics

Proposed approach:

Step 1: Data Augmentation

Step 2: Health Index Extraction

Step 3: Remaining Useful Life Prediction

- ▶ Dassault Aviation data from Falcon 6X [Hervé de Beaulieu et al., 2023]
 - New generation of aircraft with increased in-flight data collection capabilities (sensor time series from all embedded systems)
 - First test flight in 2021
 - Only historical nominal data available (i.e. no measured degradation)
 - Focus on the cockpit temperature control system

Global Schema:

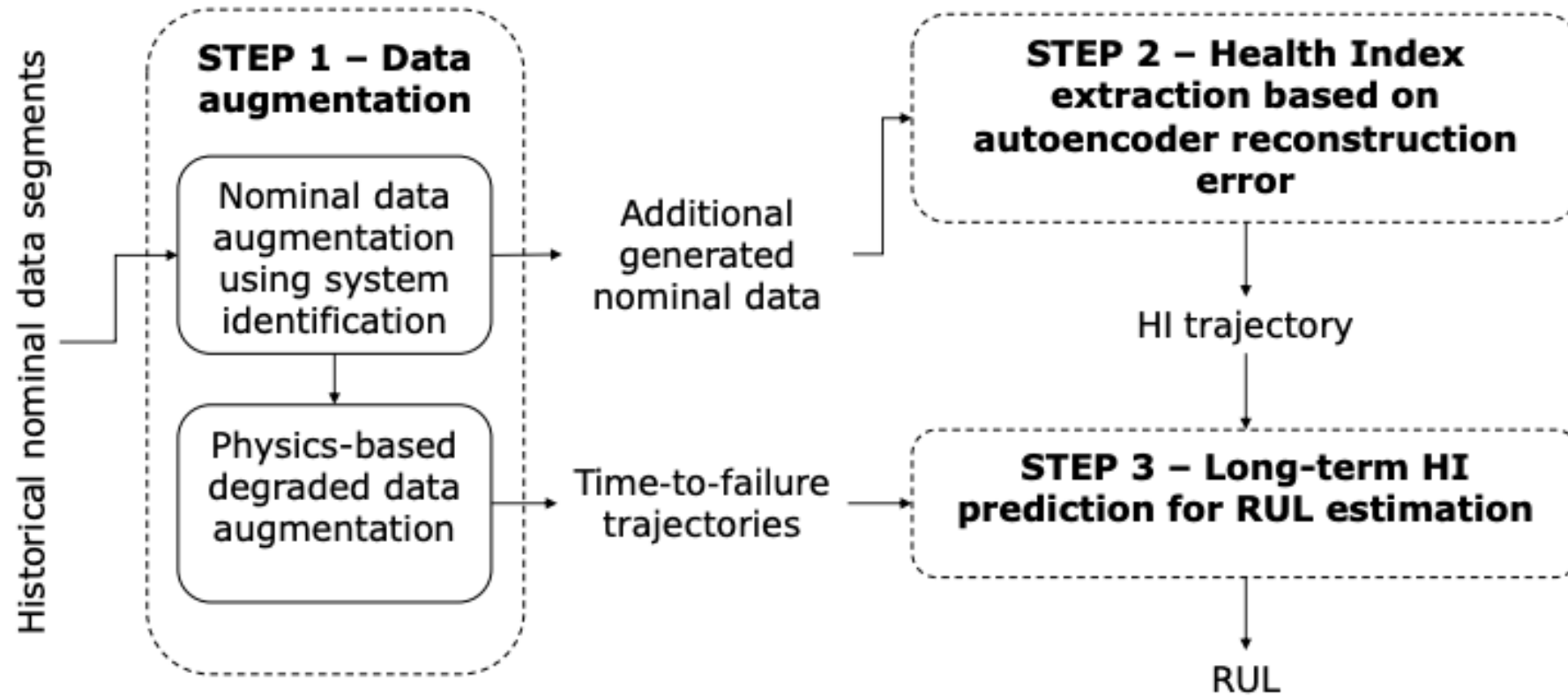


Figure: Overall proposed approach.

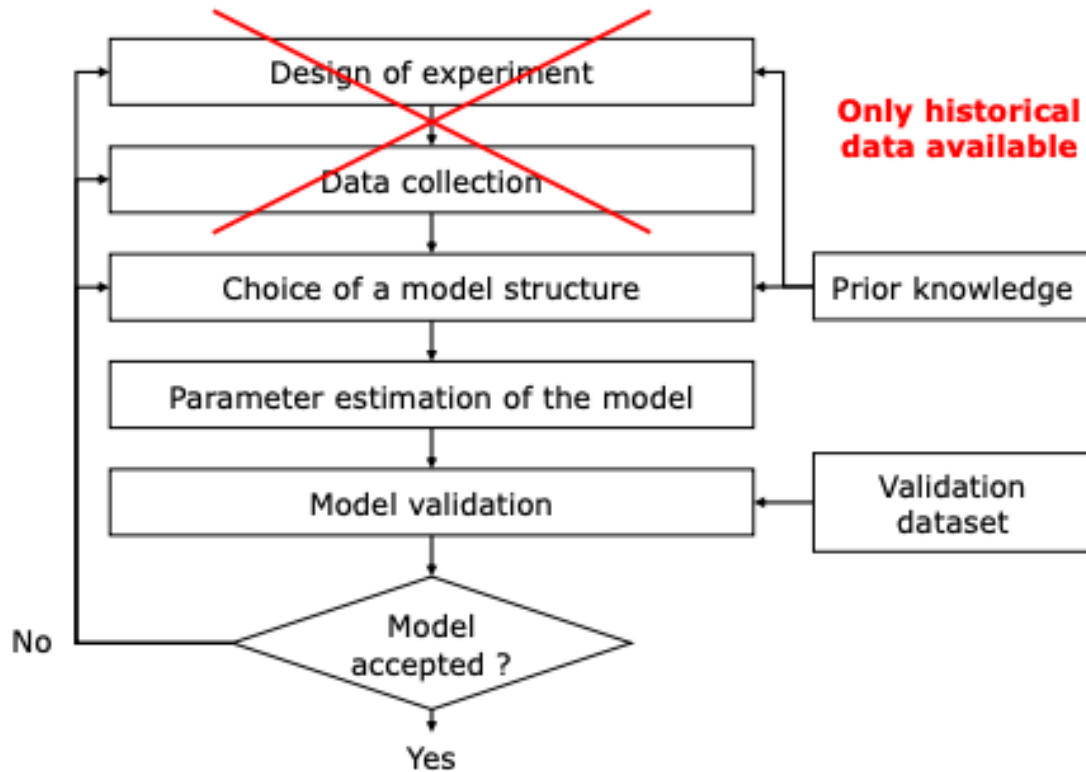
Step 1: Data Augmentation

Step 1: Data Augmentation

Objective

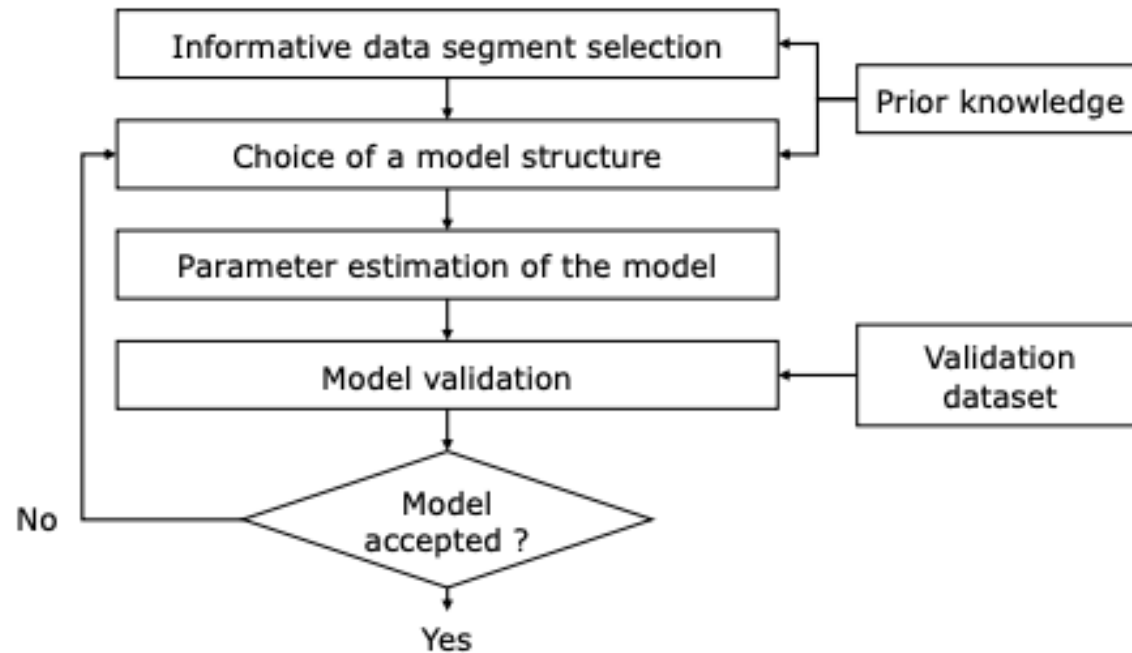
- Compensate for the lack of data
 - Both nominal and degraded data augmentation
-
- Generate more training samples from existing ones in order to improve the performance of a prediction made by a neural network.

Historical Data available. NOT Design of Experiment!!



- Experiment design is not possible

Historical Data available. NOT Design of Experiment!!



- Experiment design is not possible
- Limited amount of data only from historical flights.
- Only a few and not sufficiently informative changes of the setpoint.

Example: Historical Dataset

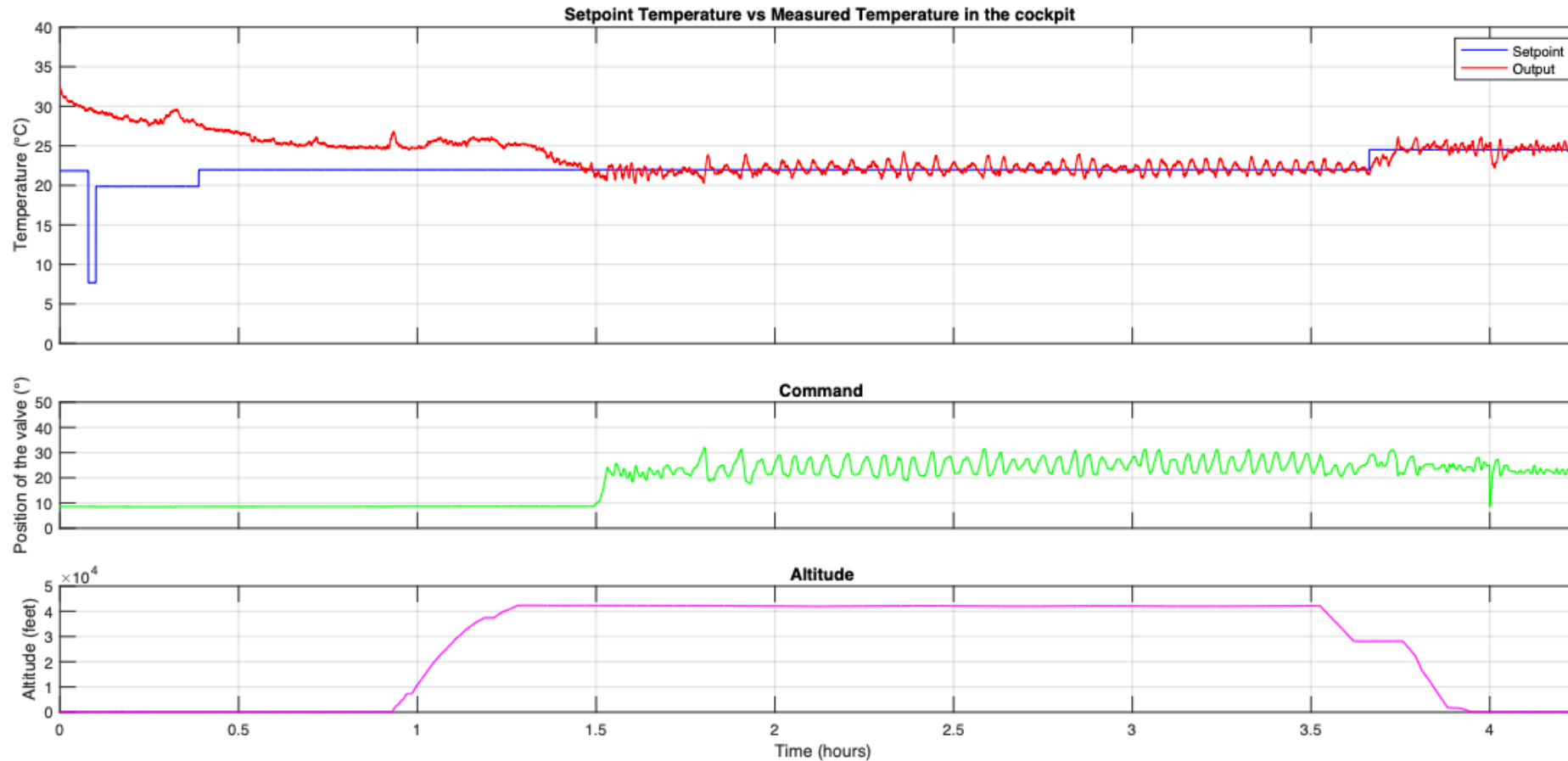


Figure: Recording of test flight of September 27, 2021.

System: Cockpit Temperature Control System

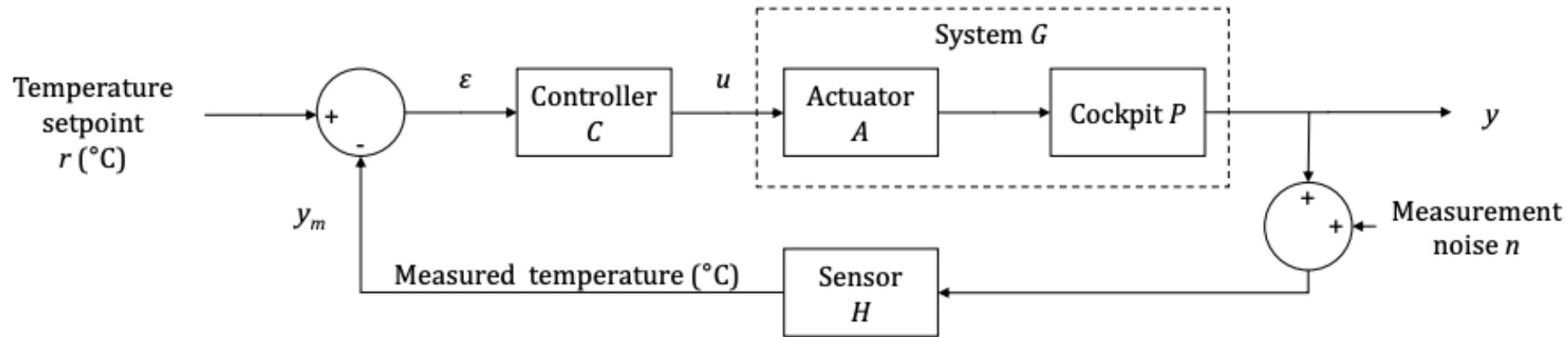
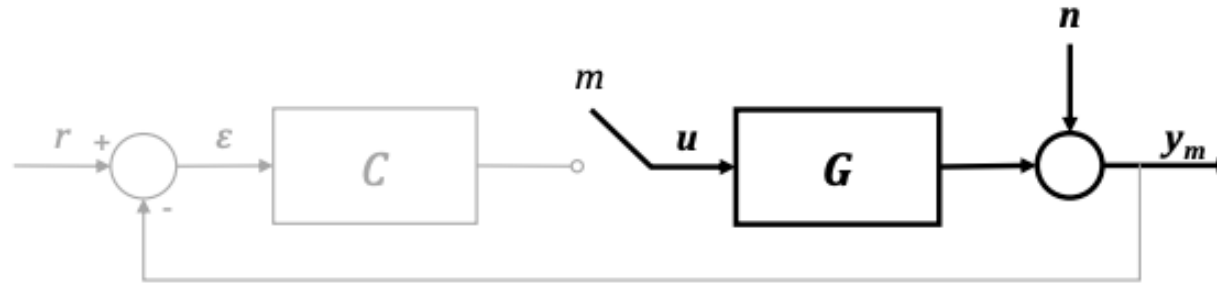


Figure: Block diagram of the cockpit temperature control system

- C and G must be identified
- Closed-loop system
- Setpoint r mostly around 22°C
- Continuous-time linear system identification

Step 1.1 : Identification of Plant model (G)



“Manual mode”

- Open-loop behavior
- Variation on command u
- Identification of G

$$y_m = Gu + n$$

(2)

Step 1.1 : Identification of Plant model G

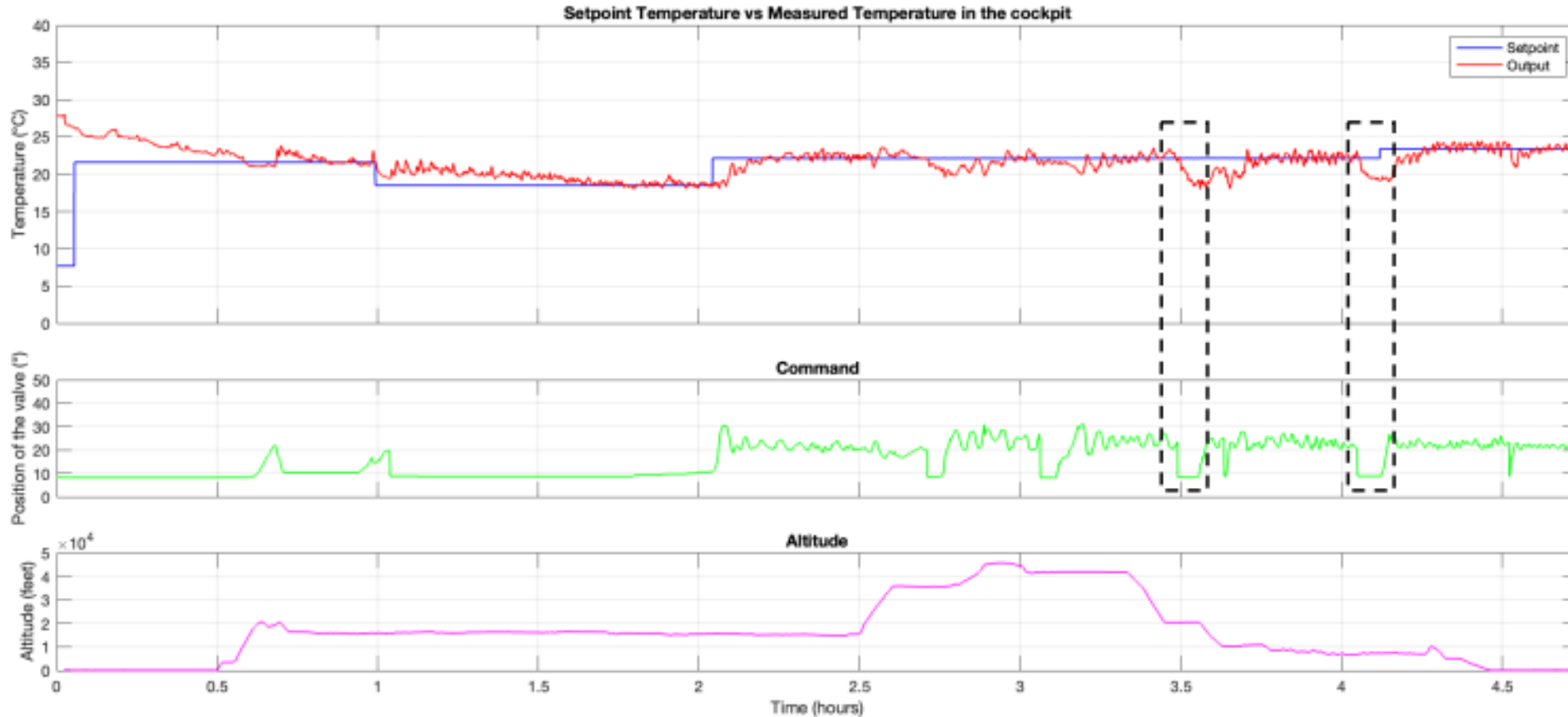
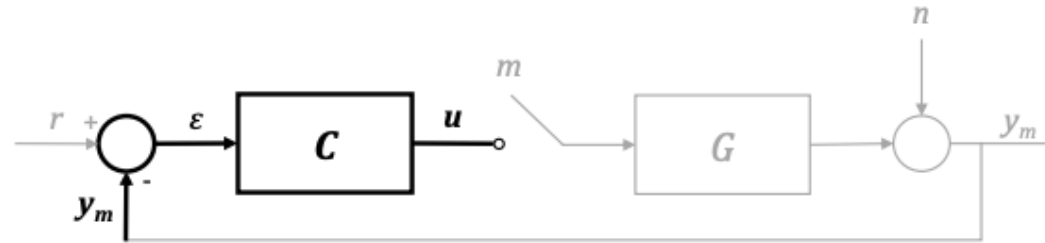


Figure: Flight of October 5, 2021, Aircraft 3.

Step 1.2: Identification of the controller C



“Auto mode”

- Closed-loop behavior
- Setpoint r remains constant
- Identification of the inverse of the controller [MacGregor and Fogal, 1995, Huang and Kadali, 2008]

$$y_m = -\frac{1}{C}u \quad (3)$$

Step 1.2: Identification of the controller C

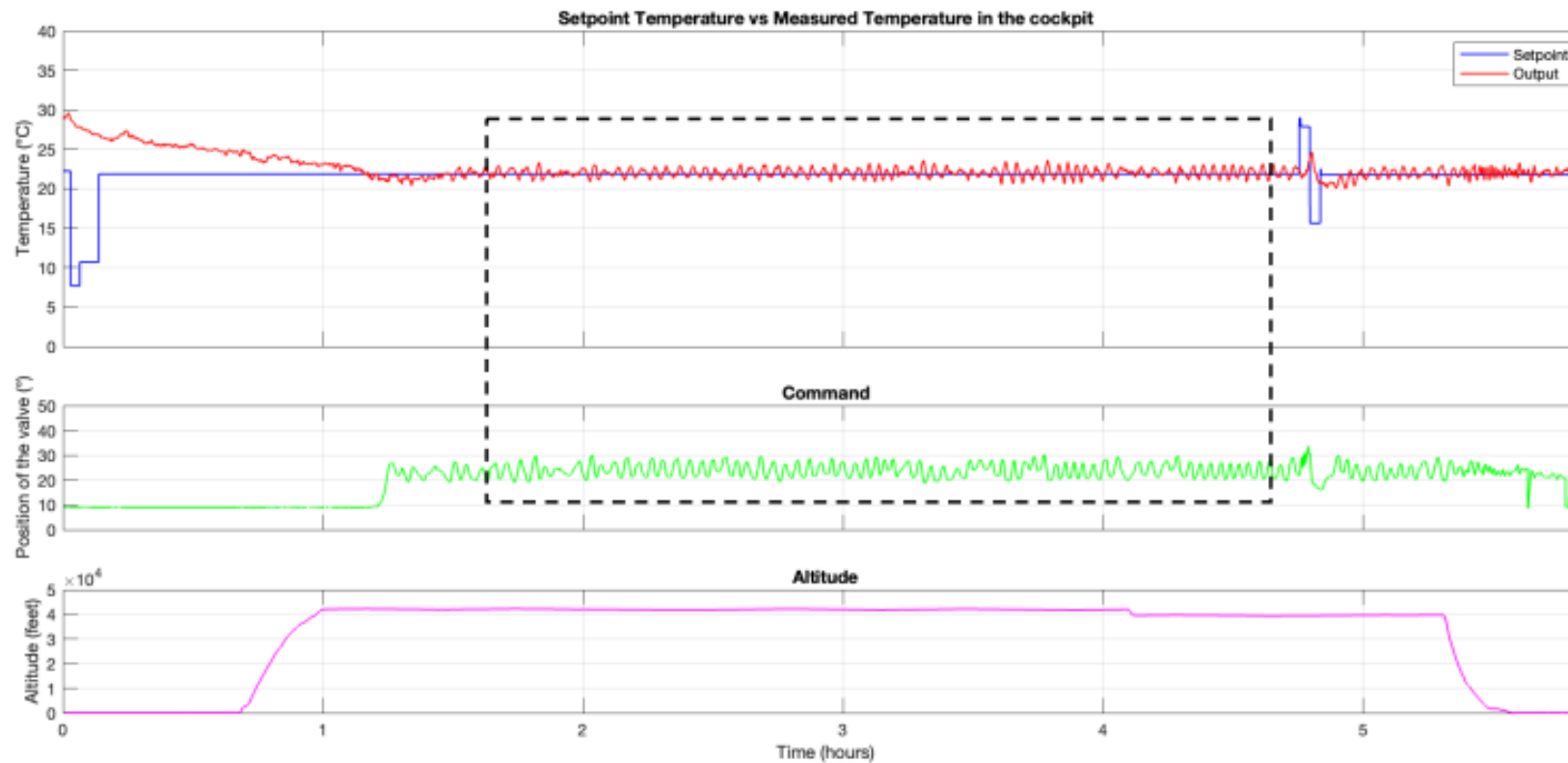
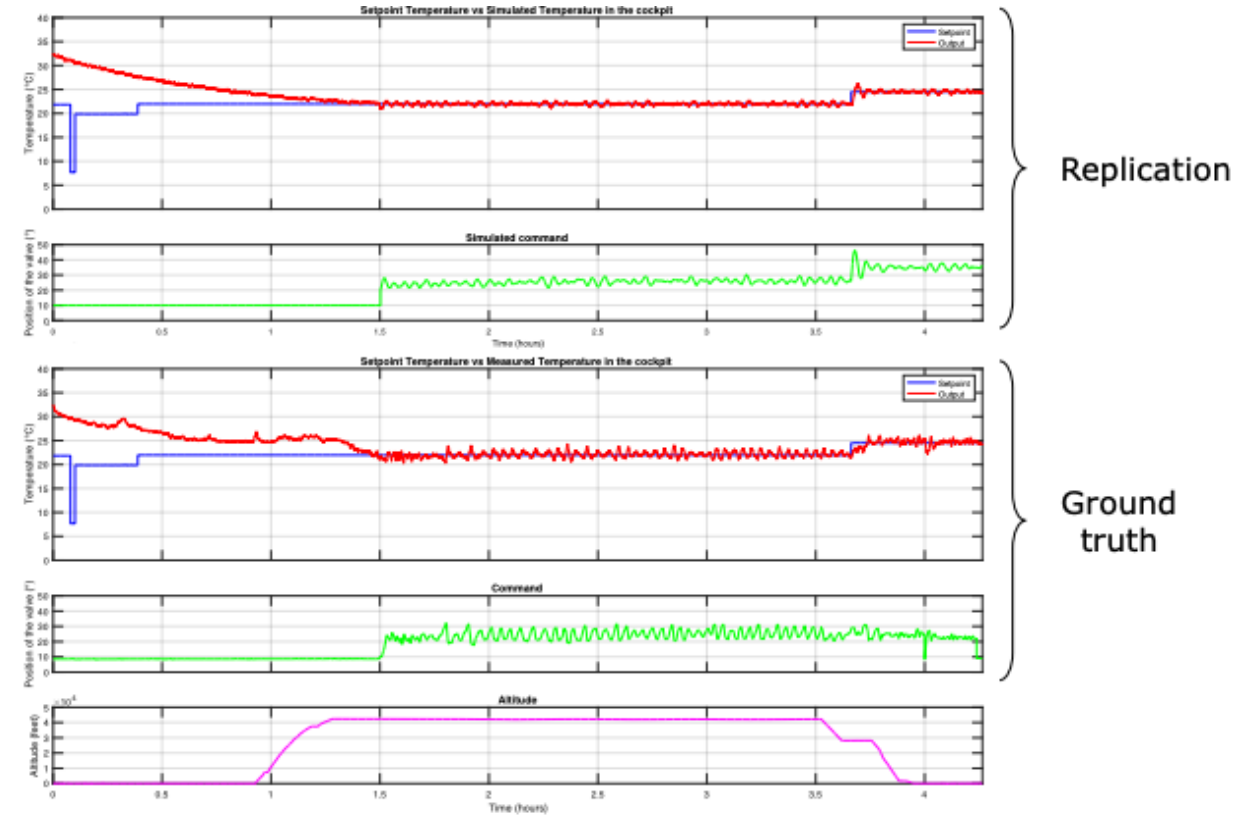
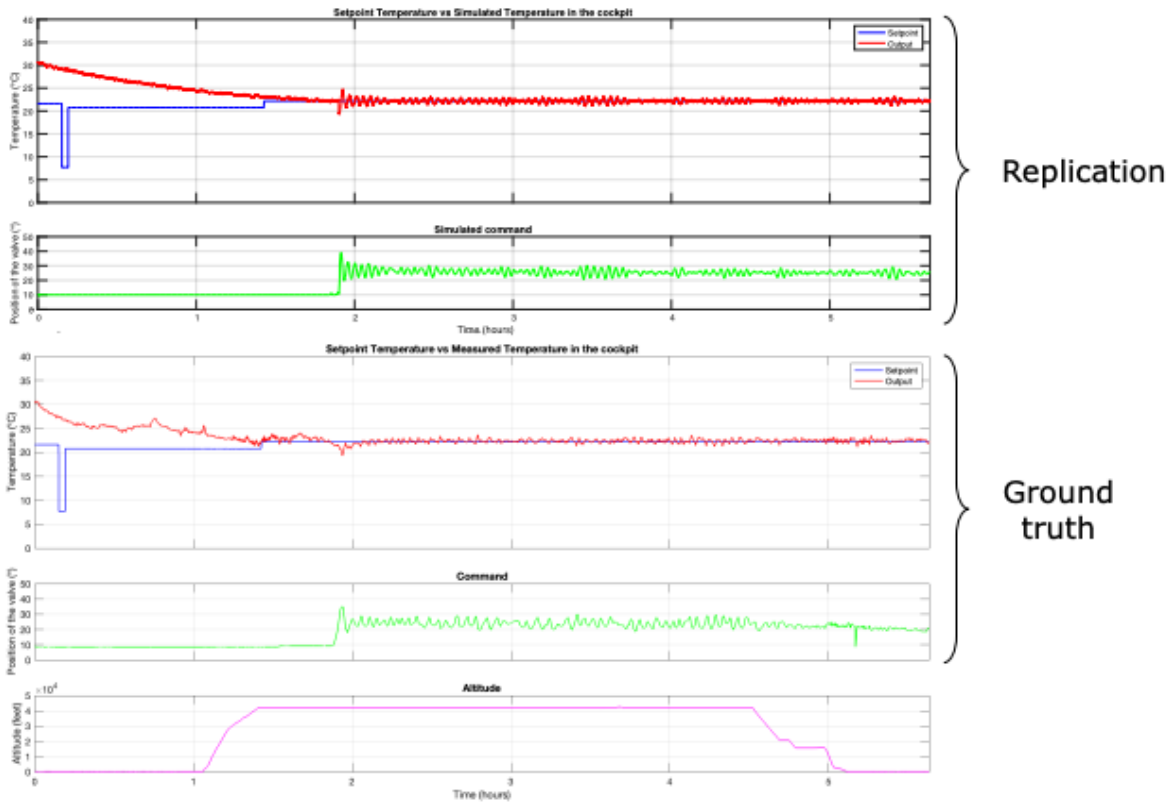


Figure: Flight of September 29, 2021, Aircraft 3.

1.3 Validation: Replicate different - existing flights!



Step 1.5: Nominal Data Augmentation

- **Nominal data augmentation**

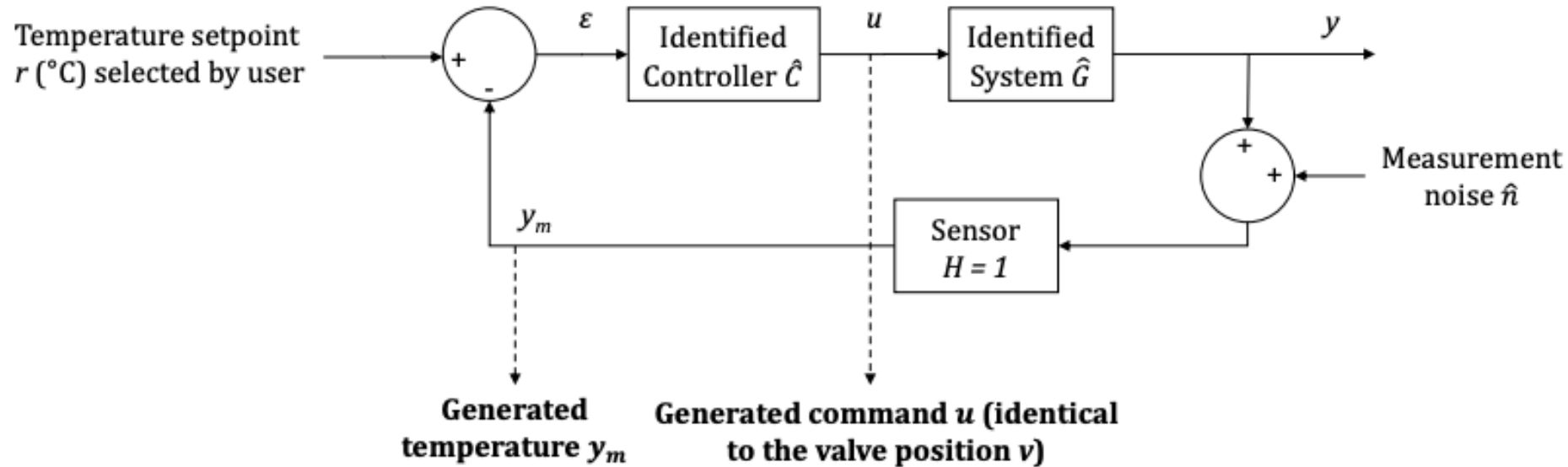


Figure: Global air distribution system model used to generate additional nominal data.

Step 1.6 Physics Based Degraded Data augmentation

Hybrid process: data-driven models supplemented by a physics-based degradation model.

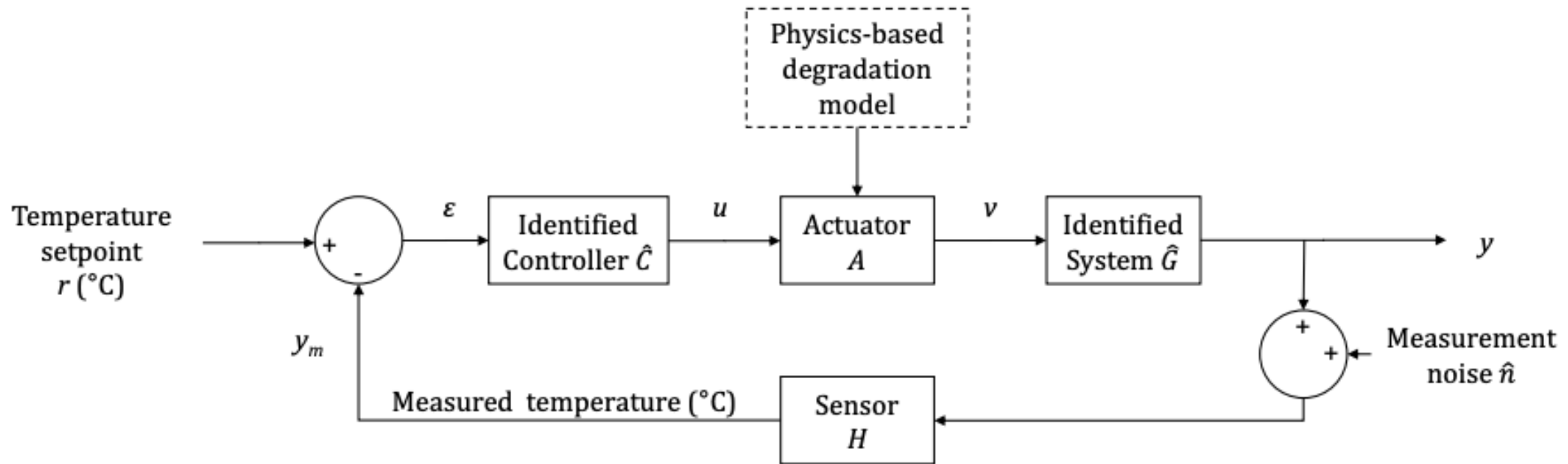


Figure: Injection of non-linear effects of degradation in the actuator.

Step 1.6 Physics Based Degraded Data augmentation: Valve Stiction

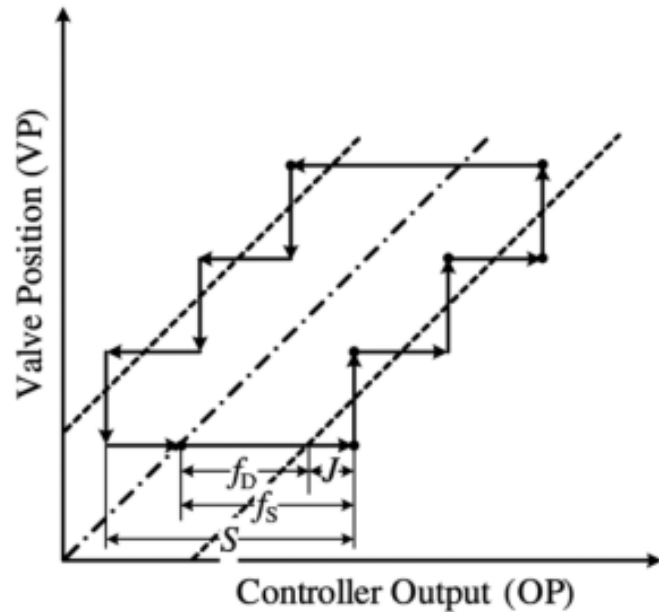


Figure: Valve stiction modeling
[He and Wang, 2010].

Stiction model [Siraskar, 2021, Choudhury et al., 2004]:

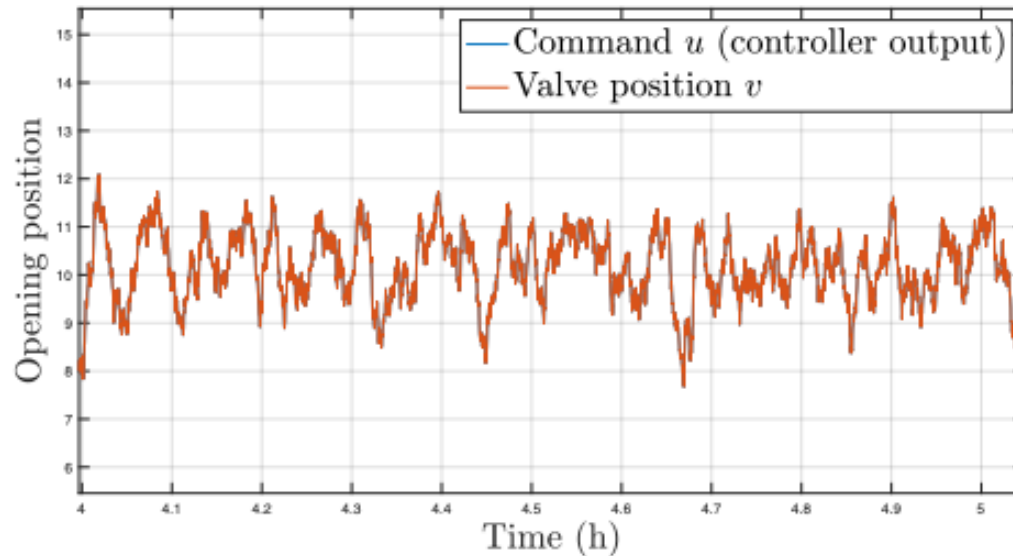
$$x_k = \begin{cases} x_{k-1} + (e_k - \text{sign}(e_k)f_D), & \text{if } |e_k| > f_S \\ x_{k-1}, & \text{if } |e_k| \leq f_S \end{cases} \quad (4)$$

with $e_k = u_k - x_{k-1}$, f_S and f_D the static and dynamic stiction parameters.

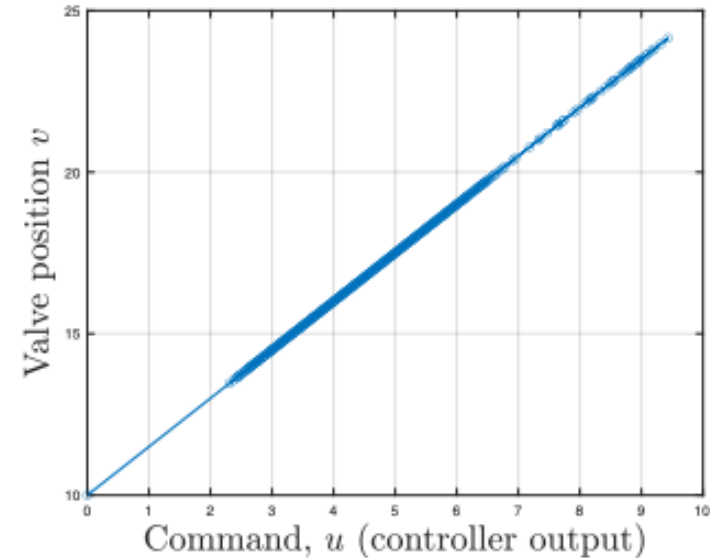
Step 1.6 Physics Based Degraded Data augmentation: Degradation Modelling

Simple failure mode: increasing the value of the parameter f_S alone, following a time t -dependent exponential degradation model.

$$f_S = \beta e^{\alpha t} \quad (5)$$



(a) Command (from the controller) and valve position when $f_S = 0$.

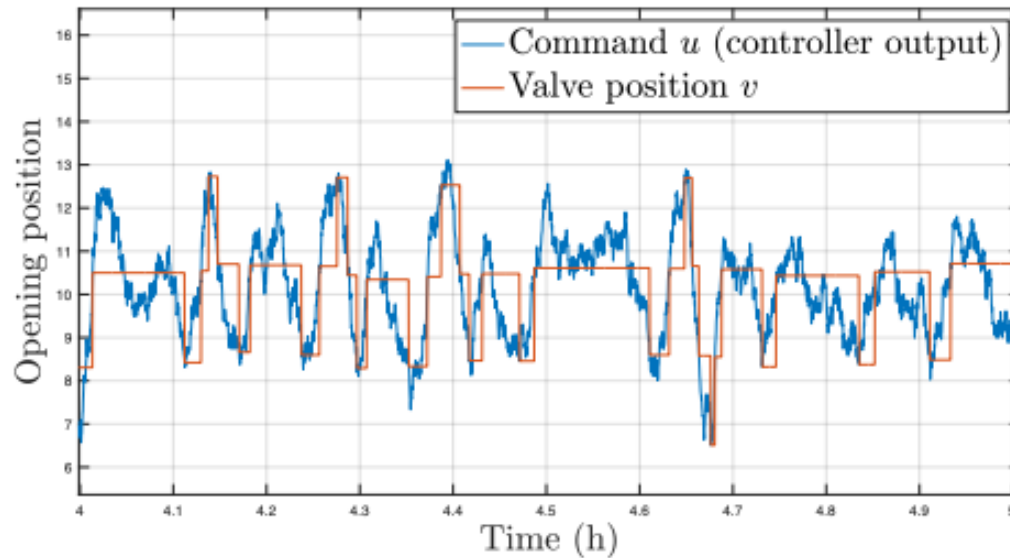


(b) Valve characteristic when $f_S = 0$.

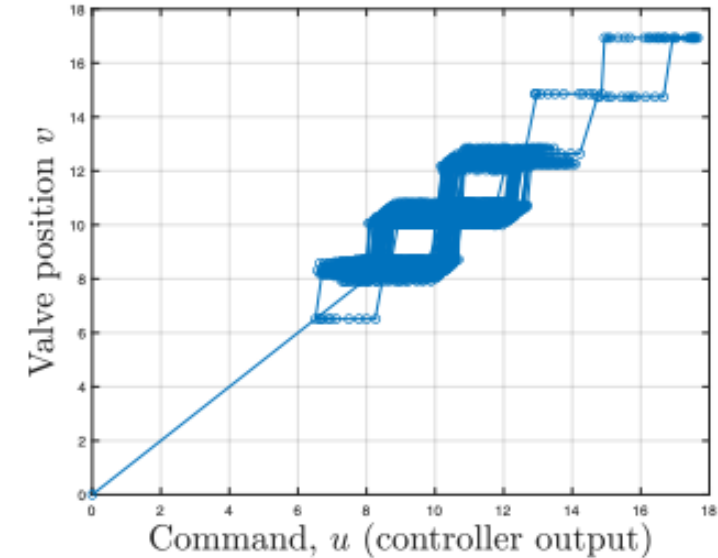
Step 1.6 Physics Based Degraded Data augmentation: Degradation Modelling

Simple failure mode: increasing the value of the parameter f_S alone, following a time t -dependent exponential degradation model.

$$f_S = \beta e^{\alpha t} \quad (5)$$



(c) Command (from the controller) and valve position when $f_S = 15$.



(d) Valve characteristic when $f_S = 15$.

Step 1.6 Physics Based Degraded Data augmentation: Time to Failure Trajectory generation

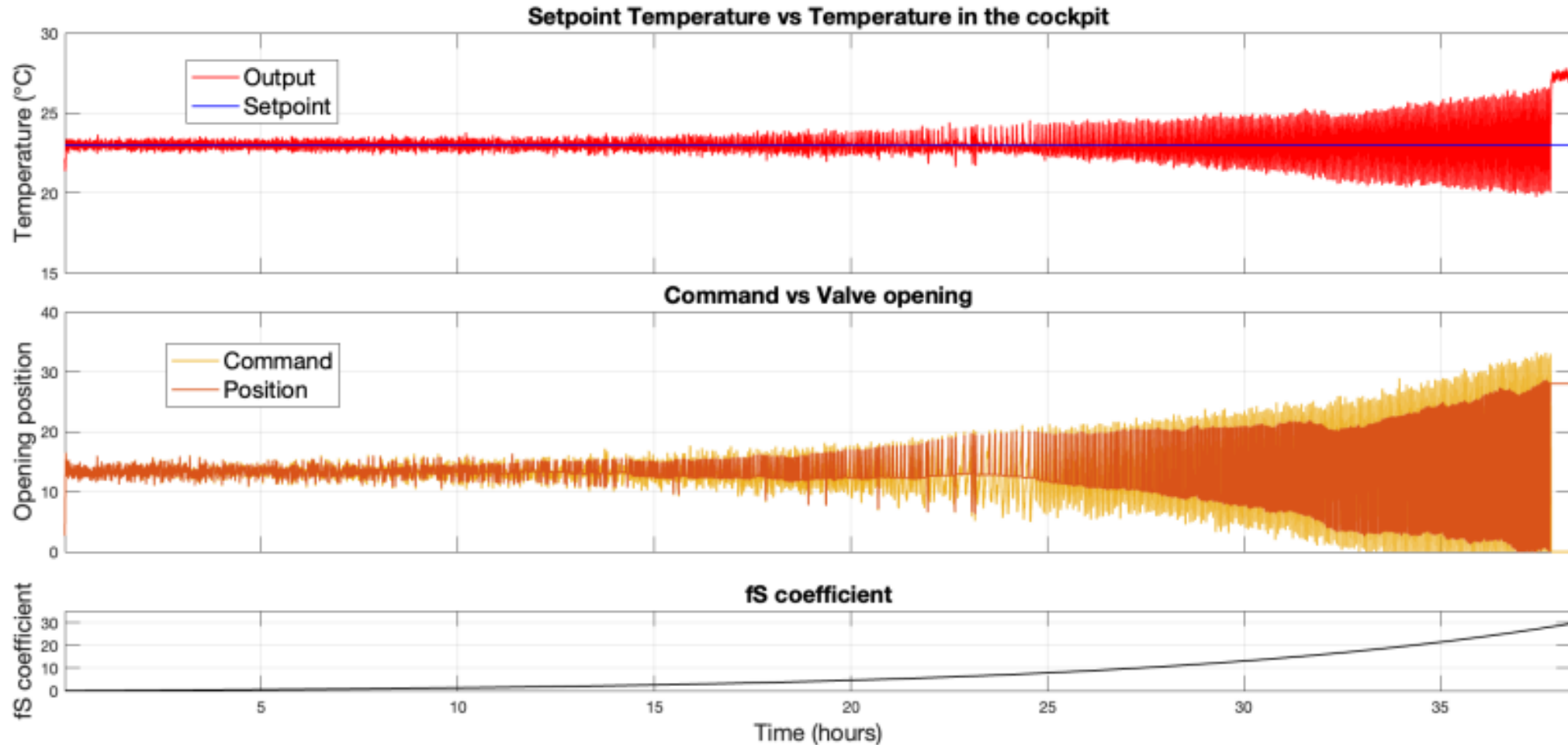


Figure: Time to Failure (TTF) trajectory generation.

Step 2: Health Index Extraction

Step 2: Health Index Extraction

Objective

- Extract Health Index (HI) from raw sensor data
 - Using nominal data only (i.e. without degradation)
-
- Unsupervised method
 - Fusing multiple sensor signals into one variable
 - Autoencoders
 - ▶ Unsupervised
 - ▶ Very efficient at extracting features from raw sensor data [Gensler et al., 2016, Hu et al., 2016]
 - ▶ Data-related : Able to extract relevant features only from data within similar distribution to training set

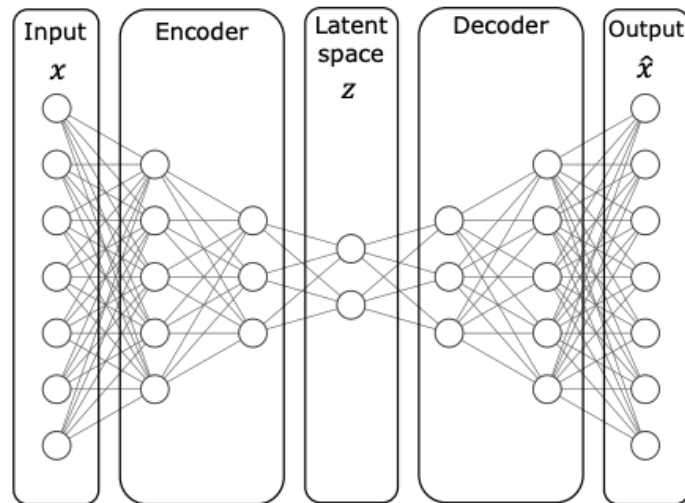


Figure: Autoencoder structure.

$$z = f_{\theta_e}(x) \quad (6)$$

$$\hat{x} = g_{\theta_d}(z) \quad (7)$$

$$\hat{x} = g_{\theta_d}(f_{\theta_e}(x)) \quad (8)$$

$$J_{AE}(\theta_e, \theta_d) = \sum L(x, g_{\theta_d}(f_{\theta_e}(x))) \quad (9)$$

Step 2: Health Index Extraction: Reconstruction Error

Consider a nominal training domain:

$$D_N = \{\mathbf{X}_N^i\}_{i=1}^{N_N} \quad (10)$$

where each sample \mathbf{X}_N^i belongs to a *nominal feature space* \mathcal{X}_N .

Training on nominal data samples

$$E(t_w) = \|\mathbf{X}_N^i(t_w) - g_{\theta_d}(f_{\theta_e}(\mathbf{X}_N^i(t_w)))\| \quad (11)$$

where

$$\mathbf{X}_N^i(t_w) = \{X_{t_k}^i\}_{k=w}^{w+\Delta} \quad (12)$$

with t_w as the start time step of the window and Δ as its total duration.

Leading to optimal parameters θ_e^* and θ_d^*

Step 2: Health Index Extraction: Reconstruction Error

Consider now a system under degradation: \mathbf{X}_D^i belongs to a *degraded feature space* \mathcal{X}_D

Degraded feature space

The distribution of data samples in \mathcal{X}_D drifts increasingly from the distribution of nominal samples as the system approaches its EOL.

$$P(\mathbf{X}_N^i) \neq P(\mathbf{X}_D^i). \quad (13)$$

With parameters derived from nominal data:

$$E_{total}(t_w) = \sum_{k=w}^{w+\Delta} \left\| \mathbf{X}_D^i(t_k) - g_{\theta_d^*}(f_{\theta_e^*}(\mathbf{X}_D^i(t_k))) \right\| \quad (14)$$

Health Index

Due to the distribution shift in $P(\mathbf{X}_D^i)$, E_{total} continues to grow until the system fails completely. This time varying, certainly increasing reconstruction error is used as HI.

Step 2: Health Index Extraction: Autoencoder Structure

Autoencoder made of Fully Connected Layer (FCL)

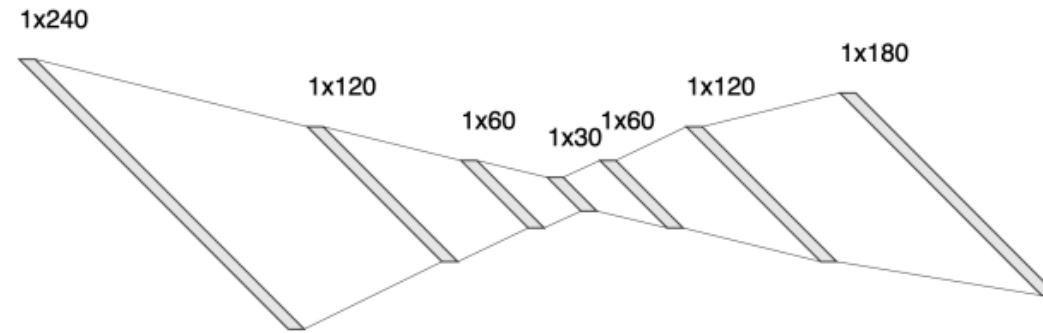


Figure: Autoencoder structure for signals reconstruction.

Training:

$$\widehat{\text{vec}(\mathbf{X}_N^i(t_w))} = g_{\theta_d}(f_{\theta_e}(\text{vec}(\mathbf{X}_N^i(t_w))))$$

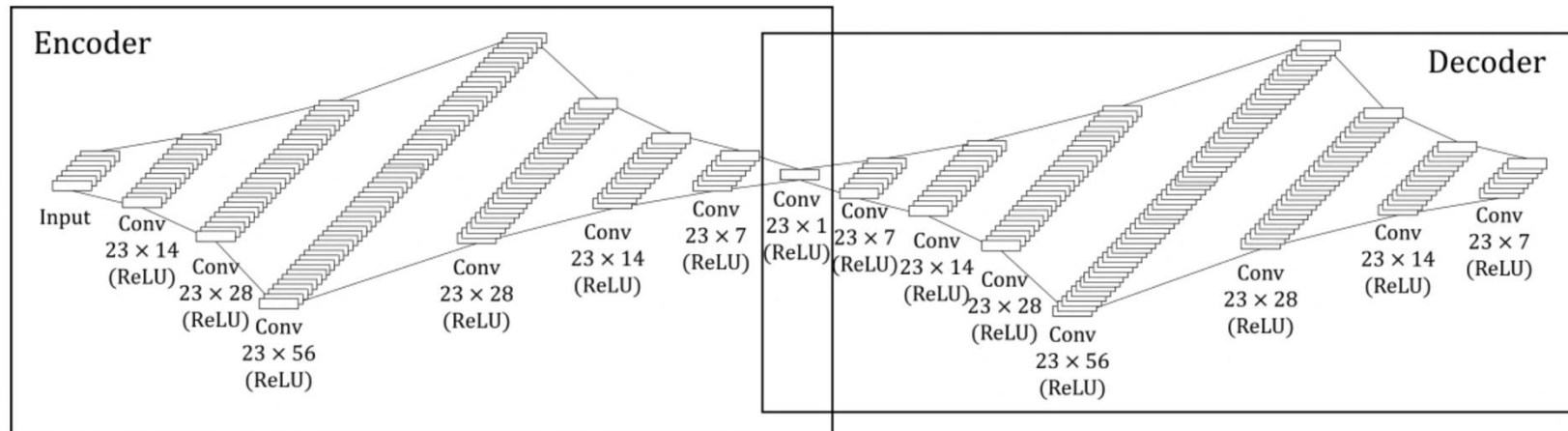


Figure 2. Proposed deep CNN autoencoder structure for VHI extraction.

Step 2: Health Index Extraction

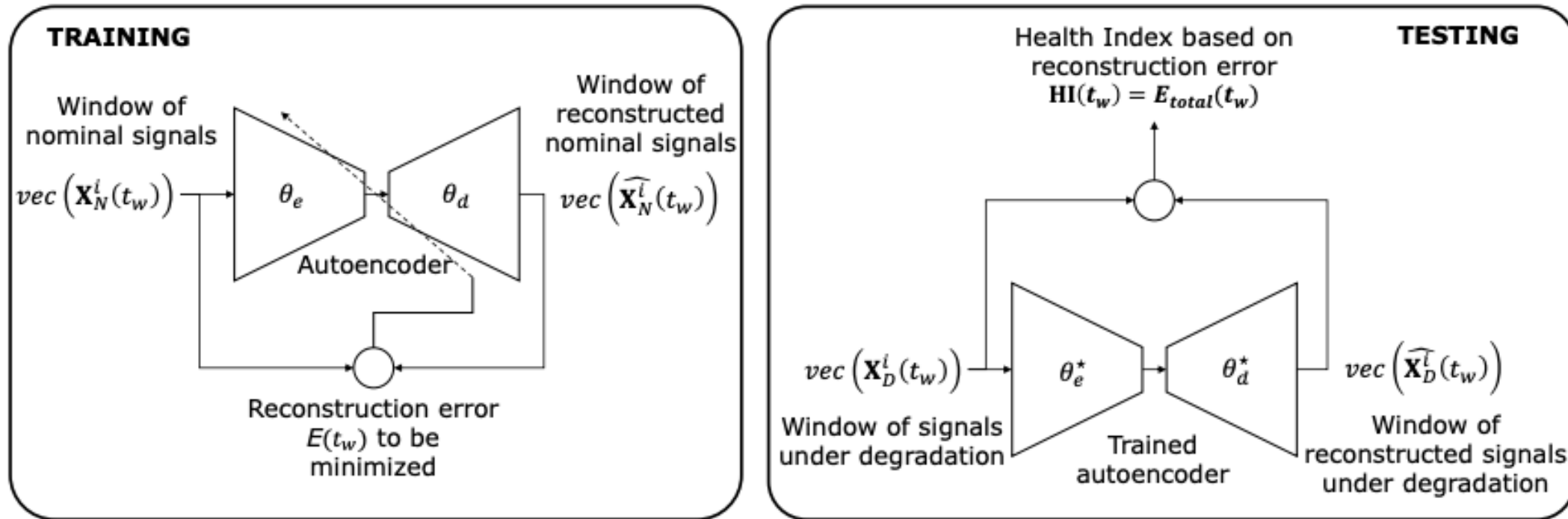


Figure: Extracting HI from sensor data using the reconstruction error of an autoencoder.

Step 2: Health Index Extraction:

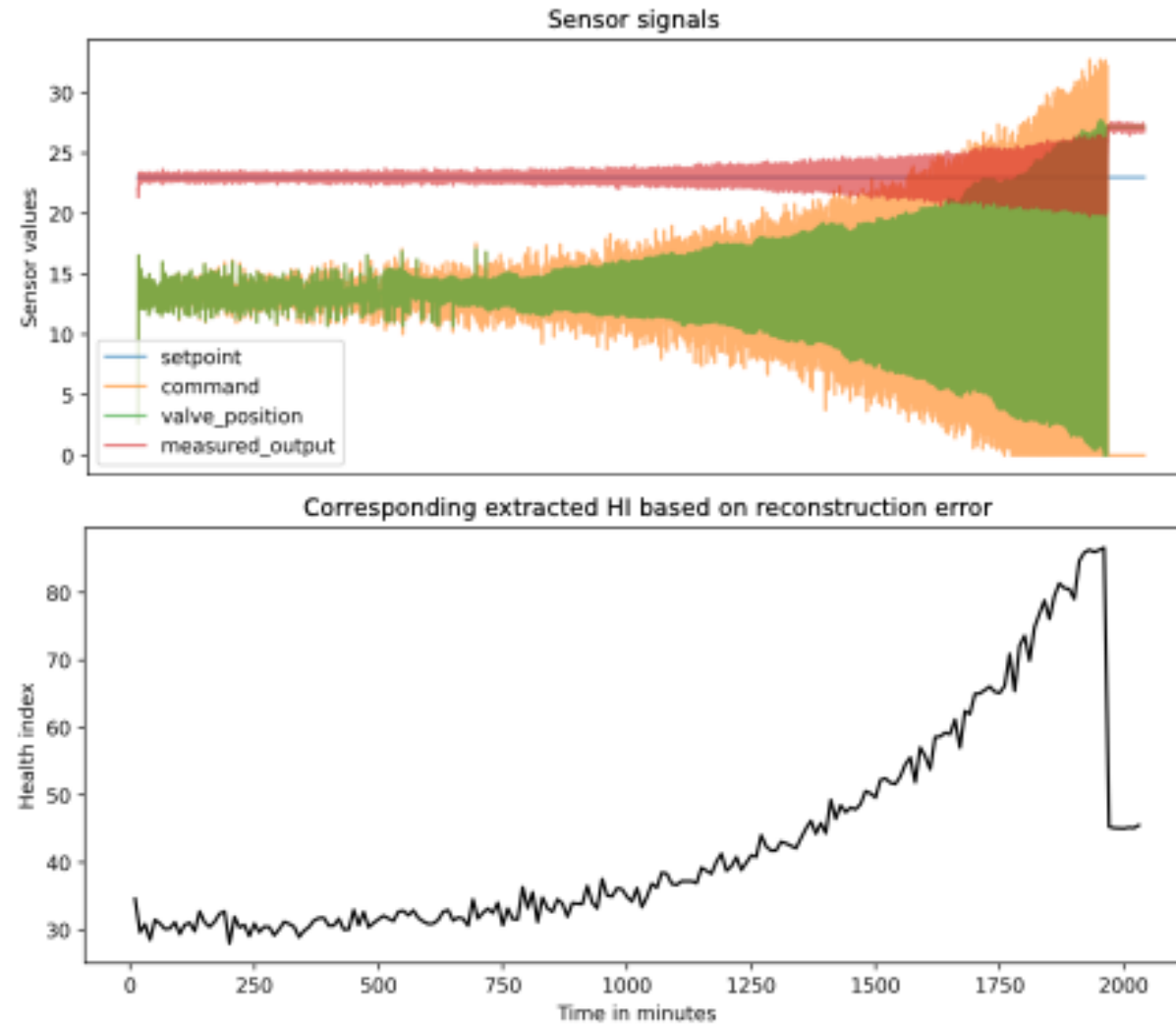


Figure: Example of HI extraction based on reconstruction for one TTF trajectory.

Step 2: Health Index Extraction: Conclusions

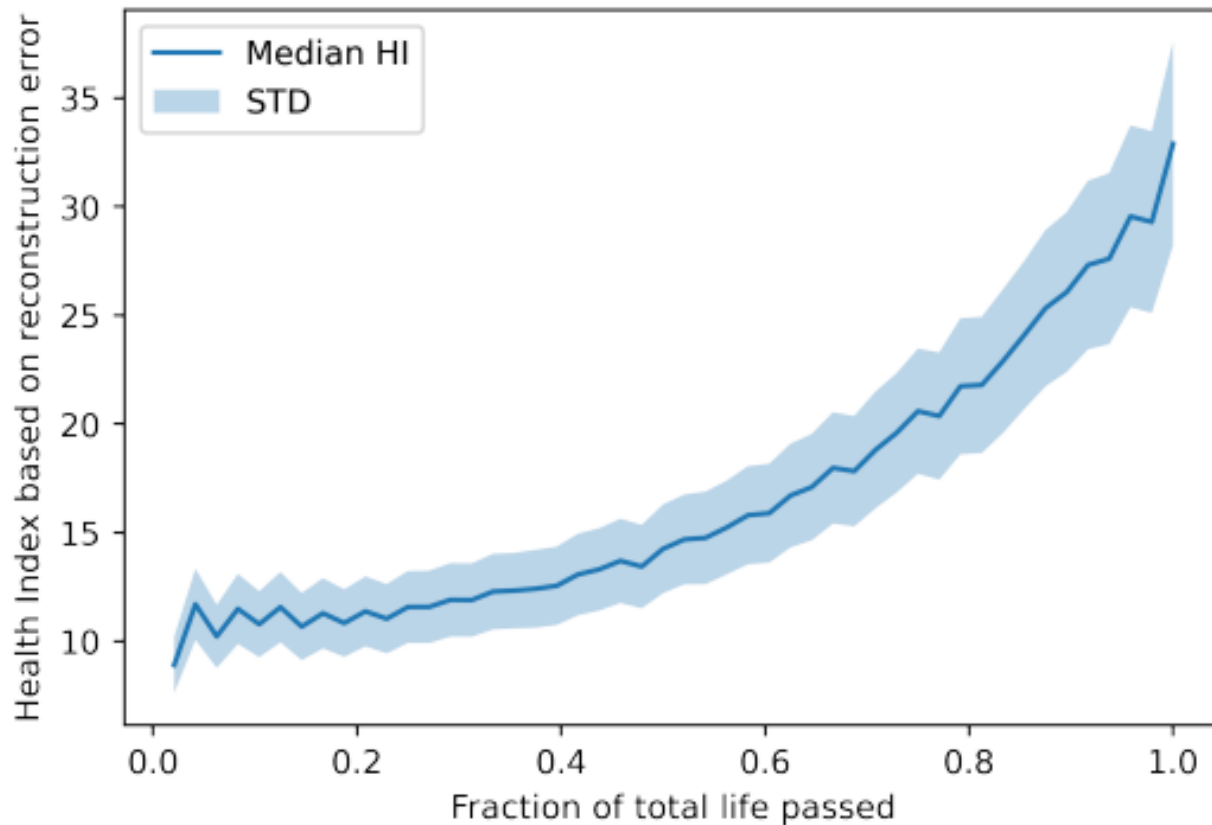


Figure: Median HI trajectory based on reconstruction error, w.r.t. fraction of total life passed.

Contribution to research challenges

- Training based exclusively on nominal data
- Fully unsupervised
- Excellent generalization capabilities as it only relies on the nominal system behavior (potential to detect any degradation)

Step 3: RUL Prediction

Step 3: RUL Prediction

Objective

Predicting Remaining Useful Life (RUL) without using RUL-labeled data

- Using degraded augmented data (Step 1)
- Long-term HI prediction
- Extrapolation - Cumulative prediction error
- Until End of Life (EOL) detection
- Leading to RUL deduction

Step 3: RUL Prediction: A Sequence to Sequence Prediction Problem

- Sequence prediction [Sun and Giles, 2001]:

$$\left[X_{t_{k=1}}, \dots, X_{t_{k=\Delta_{input}}} \right] \mapsto \hat{X}_{t_{k=\Delta_{input}+1}} \quad (17)$$

- Sequence-to-sequence prediction [Brownlee, 2017]:

$$\left[X_{t_{k=1}}, \dots, X_{t_{k=\Delta_{input}}} \right] \mapsto \left[\hat{X}_{t_{k=\Delta_{input}+1}}, \dots, \hat{X}_{t_{k=\Delta_{input}+\Delta_{pred}}} \right] \quad (18)$$

- Chained sequence-to-sequence prediction:

$$\begin{aligned} \left[X_{t_{k=1}}, \dots, X_{t_{k=\Delta_{input}}} \right] &\mapsto \left[\hat{X}_{t_{k=\Delta_{input}+1}}, \dots, \hat{X}_{t_{k=\Delta_{input}+\Delta_{pred}}} \right] \\ \left[\hat{X}_{t_{k=\Delta_{input}+1}}, \dots, \hat{X}_{t_{k=\Delta_{input}+\Delta_{pred}}} \right] &\mapsto \left[\hat{X}_{t_{k=\Delta_{input}+\Delta_{pred}+1}}, \dots, \hat{X}_{t_{k=\Delta_{input}+2\Delta_{pred}}} \right] \\ &\text{etc.} \end{aligned} \quad (19)$$

with Δ_{input} , Δ_{pred} the lengths of input and output sequences and \mapsto the mapping model (which can typically be an RNN or its variants).

Step 3: RUL Prediction: A Sequence to Sequence Prediction Problem

- Reusing previous predicted output sequences as input for future predictions
- Cumulative prediction error
- Overlapping concept proposed to improve continuity between windows
- Careful selection of hyperparameters Δ_{input} , Δ_{pred} and δ .

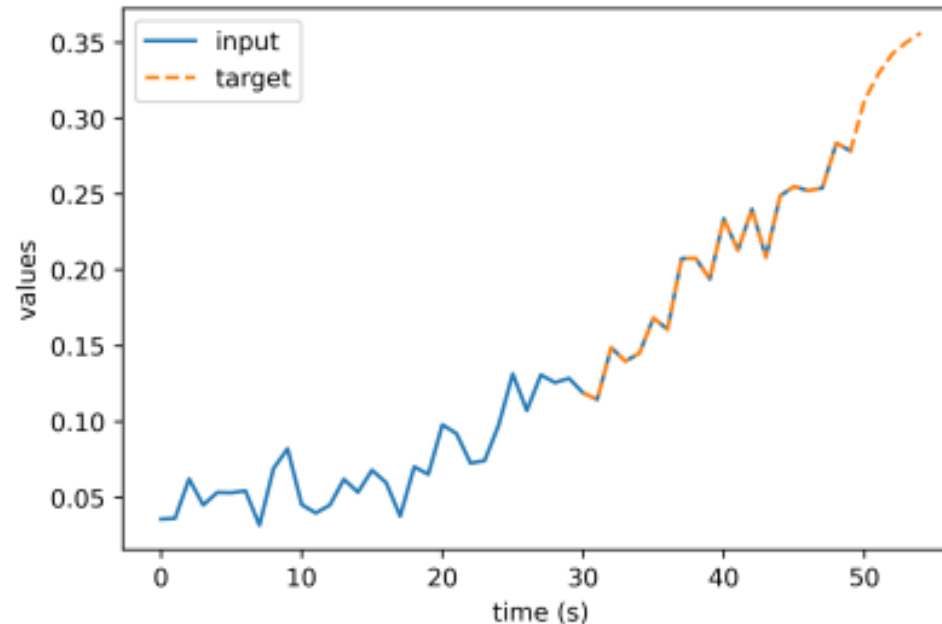


Figure: Overlapping sequences.

Step 3: RUL Prediction: A Sequence to Sequence Prediction Problem

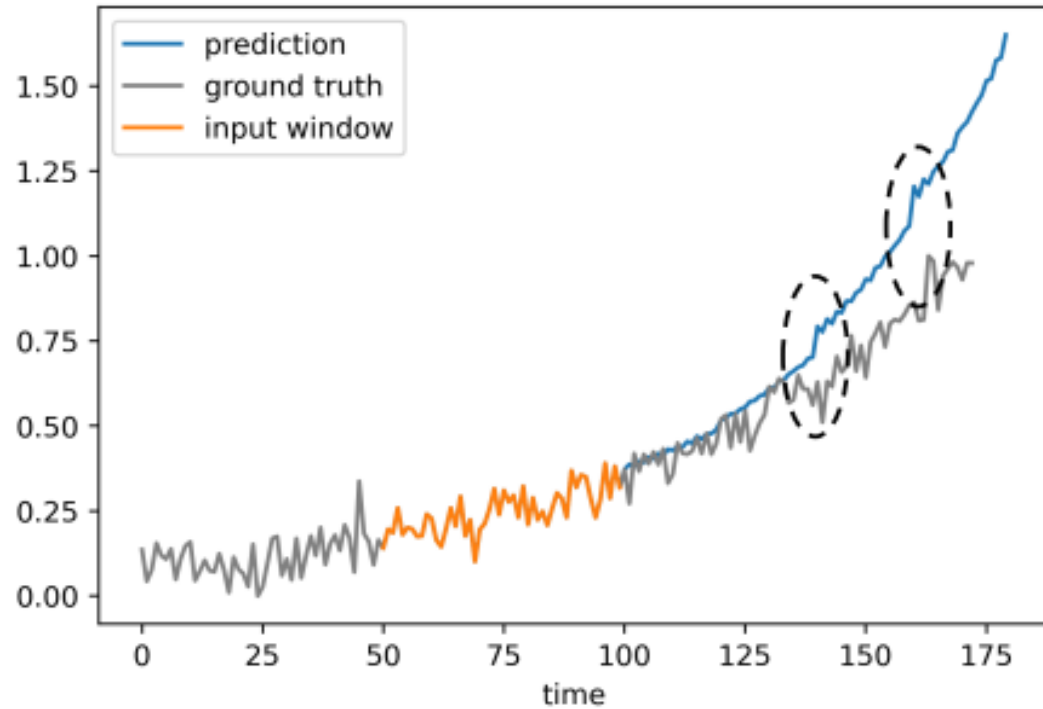


Figure: Without overlapping.

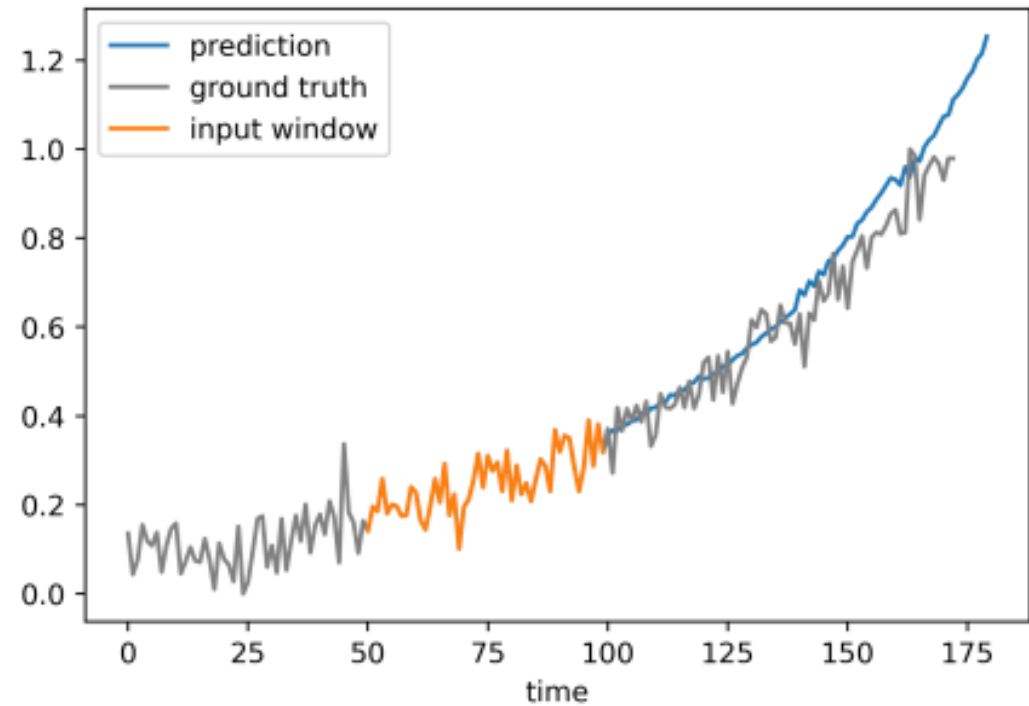


Figure: With overlapping δ .

Step 3: RUL Prediction: Deep LSTM Structure

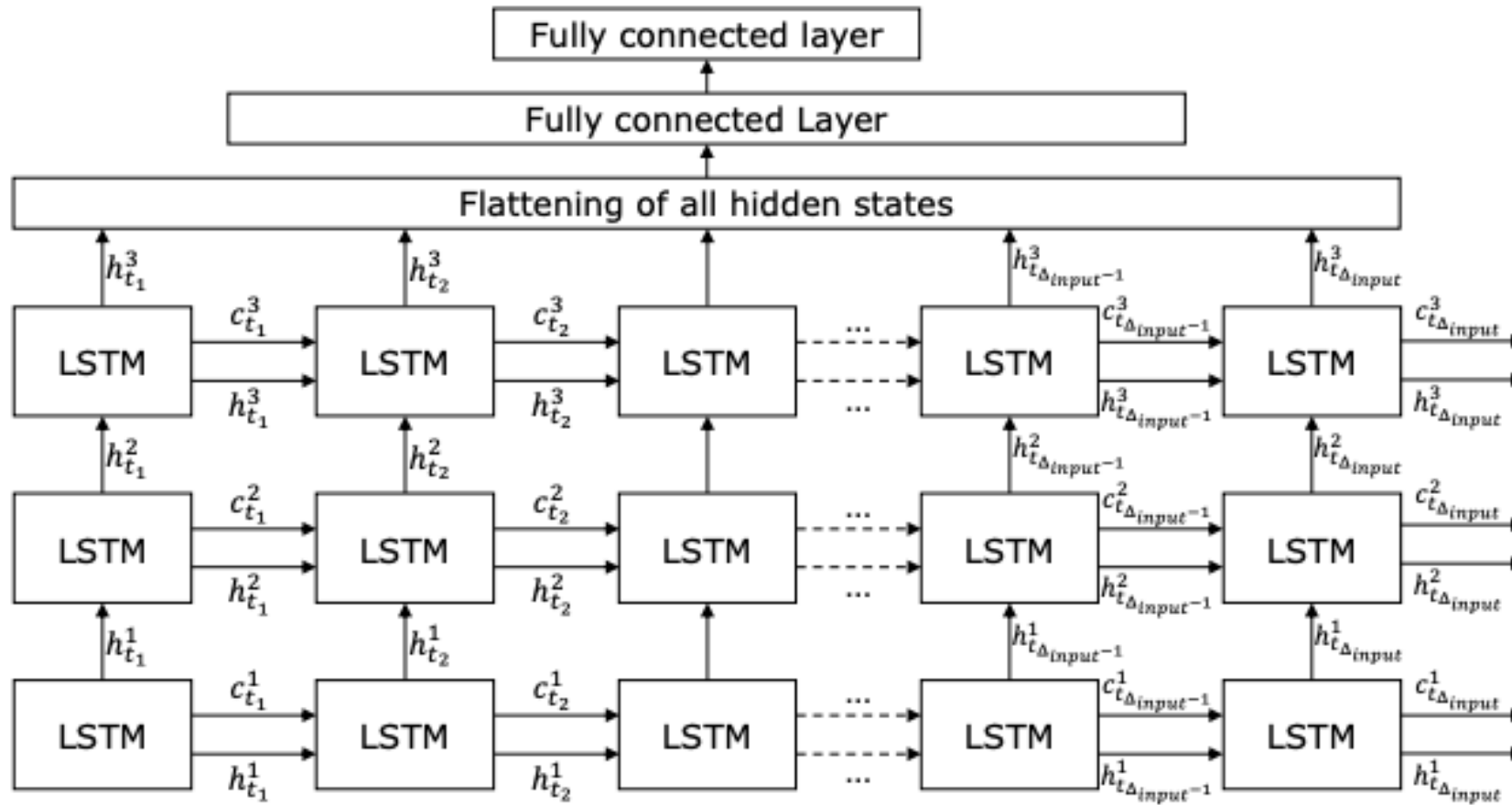


Figure: 3-layered stacked-LSTM network.

Step 3: RUL Prediction: EOL Detection

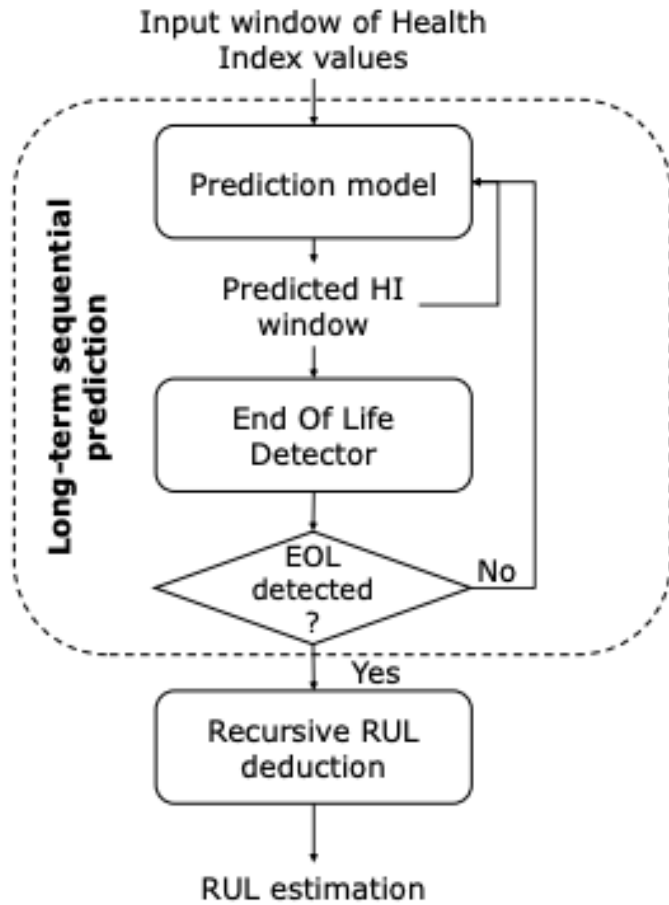


Figure: Overview of step 3 - prediction.

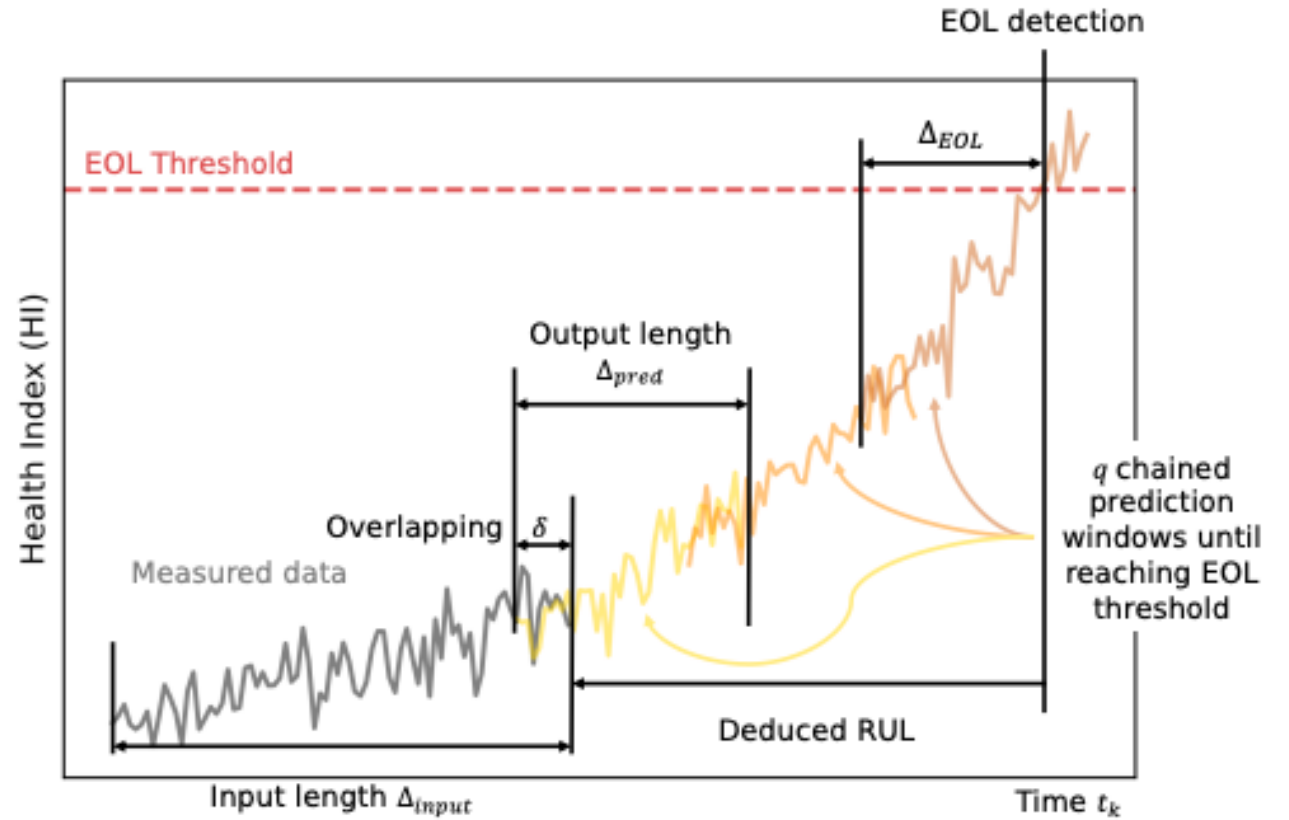


Figure: EOL detection by threshold overshooting strategy.

Step 3: RUL Prediction: HI Prediction

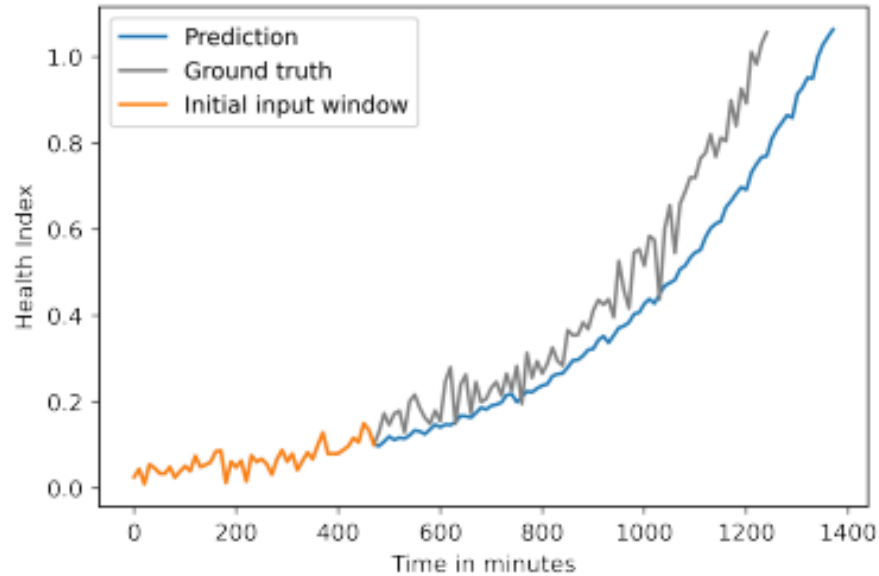


Figure: HI prediction for one TTF test trajectory, starting from $t_{k=480}$ minutes.

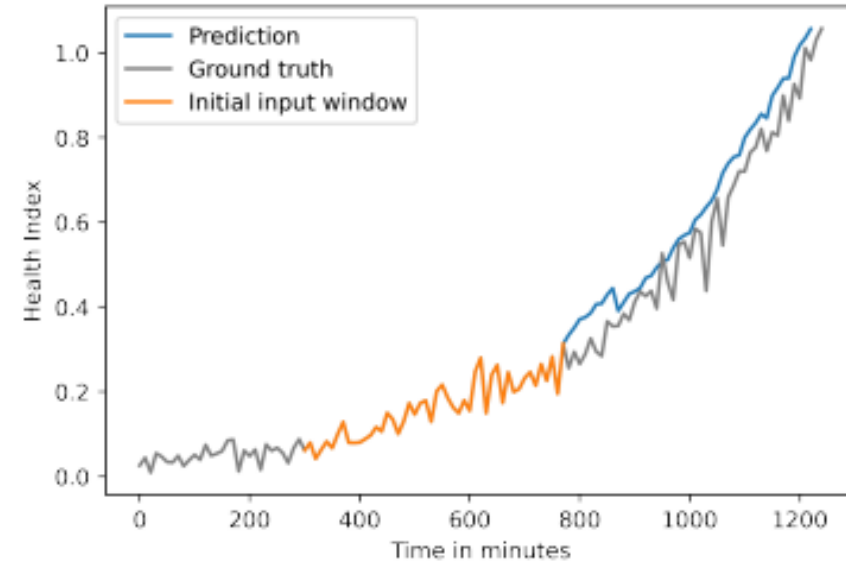


Figure: HI prediction for one TTF test trajectory, starting from $t_{k=800}$ minutes

Accumulation of prediction error leading to lower accuracy for early predictions.

Step 3: RUL Prediction: RUL Prediction

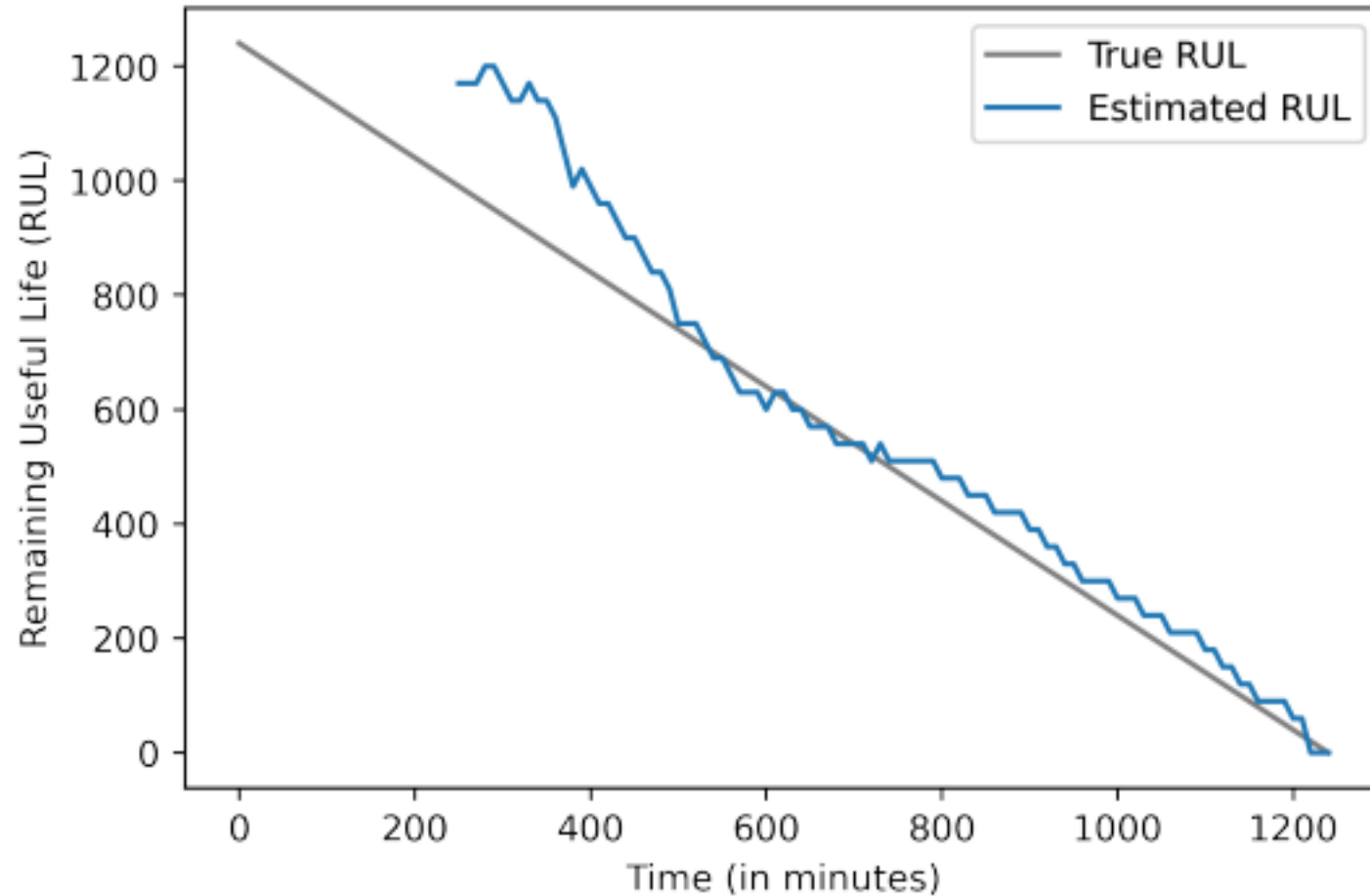


Figure: One complete predicted RUL trajectory for one TTF test trajectory.

Step 3: RUL Prediction

Sequence-to-sequence prediction:

- Key parameters: Δ_{input} , Δ_{pred} and δ
- Overlapping always improves the performance of RUL prediction (all other hyperparameters being equal)
- $\Delta_{input} > \Delta_{pred}$
- Avoid excessive extrapolation

Stacked-LSTM model:

- Key parameters: Number of layers L size of the hidden state $|h_{t_k}|$
- Model complexity

Contribution to research challenges

- No use of RUL-labeled data
- Increase in prediction performance as EOL approaches

Conclusions

- Deep NNs based Prognostics
 - Powerful approach under supervised conditions
 - Excellent generalisation capability under diverse, rich conditions.
 - Good capacity in presence of qualitative, quantitative data (non stationary, nonlinear dynamics etc.)
- Availability of True Labelled target (output) a problem in real Industrial contexts
- Unsupervised Prognostics → still in nascent stage
- First contributions in this direction using system identification + deep autoencoders + LSTMS.

References to work:

- de Beaulieu, M. H., Jha, M. S., Garnier, H., & Cerbah, F. (2024). Remaining Useful Life prediction based on physics-informed data augmentation. *Reliability Engineering & System Safety*, 252, 110451.
- De Beaulieu, M. H., Jha, M. S., Garnier, H., & Cerbah, F. (2022, July). Unsupervised remaining useful life estimation based on deep virtual health index prediction. In *7th European Conference of the Prognostics and Health Management Society, PHME22*.
- Herve de Beaulieu, M., Jha, M., Garnier, H., & Cerbah, F. (2022). Long range health index estimation based unsupervised RUL prediction using encoder-decoders. In *11th IFAC Symposium on Fault Detection, Supervision and Safety for Technical Processes. Pafos, Cyprus*.

Bibliography

- Learning algorithms for classification: A comparison on handwritten digit recognition. *Neural networks Stat Mech Perspect* 261:276
- Simonyan K, Zisserman A (2015) VERY DEEP CONVOLUTIONAL NETWORKS FOR LARGE-SCALE IMAGE RECOGNITION. *ICLR* 75:398–406. doi: 10.2146/ajhp170251
- Lin M, Chen Q, Yan S (2013) Network In Network. 1–10. doi: 10.1109/ASRU.2015.7404828
- He K, Zhang X, Ren S, Sun J (2015) Deep Residual Learning for Image Recognition. *Multimed Tools Appl* 77:10437–10453. doi: 10.1007/s11042-017-4440-4
- Khan, A., Sohail, A., Zahoor, U. *et al.* A survey of the recent architectures of deep convolutional neural networks. *Artif Intell Rev* 53, 5455-5516 (2020)
- Glorot X, Bengio Y (2010) Understanding the difficulty of training deep feedforward neural networks. In: *Proceedings of the thirteenth international conference on artificial intelligence and statistics*. pp 249–256
- Hochreiter, Sepp, and Jürgen Schmidhuber. "Long short-term memory." *Neural computation* 9.8 (1997): 1735-1780.
- Richard, A., Mahé, A., Pradalier, C., Rozenstein, O., & Geist, M. (2019). A Comprehensive Benchmark of Neural Networks for System Identification.
- Woo, J., Park, J., Yu, C., & Kim, N. (2018). Dynamic model identification of unmanned surface vehicles using deep learning network. *Applied Ocean Research*, 78, 123-133.



Bibliography

- Rueckert, E., Nakatenus, M., Tosatto, S., & Peters, J. (2017, November). Learning inverse dynamics models in $o(n)$ time with lstm networks. In *2017 IEEE-RAS 17th International Conference on Humanoid Robotics (Humanoids)* (pp. 811-816). IEEE.
- Fernández, S., Graves, A., & Schmidhuber, J. (2007b). An application of recurrent neural networks to discriminative keyword spotting. In *Proceedings of the International Conference on Artificial Neural Networks* (pp. 220–229). Berlin: Springer
- Liu, N., Li, L., Hao, B., Yang, L., Hu, T., Xue, T., & Wang, S. (2019). Modeling and simulation of robot inverse dynamics using LSTM-based deep learning algorithm for smart cities and factories. *IEEE Access*, 7, 173989-173998.
- Gugulothu, N., TV, V., Malhotra, P., Vig, L., Agarwal, P., & Shroff, G. (2017). Predicting remaining useful life using time series embeddings based on recurrent neural networks. *arXiv preprint arXiv:1709.01073*.
- *Systems*. Springer, Cham, 2017. 233-270 Jha, Mayank-Shekhar; 2017. "Algorithm Architectures for Intelligent Communications, Control and Monitoring Systems, **Rolls Royce University Technology Centre Sheffield**."
- Jha, Mayank Shekhar, et al. "Particle filter based hybrid prognostics of proton exchange membrane fuel cell in bond graph framework." *Computers & Chemical Engineering* 95 (2016): 216-230.
- Jha, Mayank S., Geneviève Dauphin-Tanguy, and B. Ould-Bouamama. "Particle Filter Based Integrated Health Monitoring in Bond Graph Framework." *Bond Graphs for Modelling, Control and Fault Diagnosis of Engineering* .

Bibliography

- Zheng, S., Ristovski, K., Farahat, A., & Gupta, C. (2017, June). Long short-term memory network for remaining useful life estimation. In *2017 IEEE international conference on prognostics and health management (ICPHM)* (pp. 88-95). IEEE.
- Zeiler, M. D., & Fergus, R. (2014, September). Visualizing and understanding convolutional networks. In *European conference on computer vision* (pp. 818-833). Springer, Cham.